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AD

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ANALYTICAL STUDY OF HELICOPTER GUST RESPONSE AT HIGH FORWARD SPEEDS

By

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U. S. ARMY AVIATION MATERIEL LABORATORIES FORT EUSTIS, VIRGINIA

CONTRACT DA 44-177-AMC-308(T)
BELL HELICOPTER COMPANY
FORT WORTH, TEXAS





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The present military design specification for helicopter gust loads, MIL-S-8698(ASG), relegates helicopter design practice to that of a specialized fixed-wing case offering no gust load alleviation at rotor disc loadings of six pounds per square foot and above. Although very conservative, this criterion poses no design restrictions for the low-speed flight regime because other maneuver load factors are more critical.

Recent advancements in rotorcraft forward speed capability together with higher disc loadings have increased the importance of gust design criteria. Thus, the program was initiated to analytically determine the gust response of helicopter rotor/fuselage systems for both loaded and unloaded rotors at high forward speeds. A computer program for determining the response of a helicopter free to pitch, roll, yaw, and translate vertically while penetrating a gust environment was developed. This program, universally applicable to single-, tandem-, and tilt-rotor configurations, was used to run case studies for investigating such parameters as rotor hub restraint, disc loading, rotor thrust coefficient-solidity ratio, advancing tip Mach number, forward speed, and gust profile on gust response. The intent was to digest these findings and to make recommendations to improve and expand military specifications for helicopter gust load design.

The decision to develop a single computer program universally applicable to a myriad of VTOL configurations did impose limitations on computer storage and running time. These limitations precluded a more rigorous approach to the analysis, particularly a more realistic rotor wake representation, provision for more than four rotor blades, and the inclusion of torsional flexibility with full aeroelastic coupling.

Among the major conclusions of this study are:

- The use of a rotor-mass ratio to determine gust alleviation by analogy with fixed-wing practice is unsatisfactory.
- 1. Rotor thrust coefficient-solidity ratio is among the most influential parameters on gust alleviation.
- Consideration of the aircraft to be penetrating the gust environment at a finite speed has such a profound influence on gust alleviation that for a sine-squared gust profile, the effect of nonsteady aerodynamics is insignificant.

The conclusion that unsteady aerodynamics is a second-order influence is supported by an independent effort, "Dynamic Response of a Helicopter to a Gust", sponsored by the U. S. Naval Air Systems Command under Contract NOa(s) 53-318c, wherein individual rotor blades of 2-, 3-, and 4-bladed rotors are considered to penetrate a gust gradient.

Task 1F162204A14608 Contract DA 44-177-AMC-308(T) USAAVLABS Technical Report 69-1 September 1969

ANALYTICAL STUDY OF HELICOPTER GUST RESPONSE AT HIGH FORWARD SPEEDS

BHC Report 299-099-106

Ву .,

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Prepared by

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for

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SUMMARY

An analytical study of helicopter gust response at high forward speeds is presented. A digital computer program describes the rigid-body aircraft motions in space and gives an aeroelastic representation of two rotors. The rotors can be positioned to form main-and-tail, tandem, or side-by-side configurations. Many types of rotors (articulated, semirigid, and rigid) can be evaluated. Compounding with auxiliary propulsion, using wings to unload the rotor, and converting from lifting to prop-rotor conditions can be simulated. Starting with specified trimmed flight, any feasible maneuver can be performed while subjecting the aircraft to gusts or other external influences.

For this study, a number of refinements which specifically pertain to gust response were included in the program. The most important of these appears to be the consideration of gradual gust penetration. Effects of nonsteady aerodynamics are also included in a simplified form.

The study results cover a wide range of forward speeds and rotor and blade loadings for many current VTOL configurations. Variations were made to study the effects of gust shape, rotor type, and advancing-blade-tip Mach number on response to gusts. In a group of compound single-rotor helicopter configurations, variation in wing lift allowed a study of the effect on response of rotor unloading by the wing. Dynamic effects from rotor blade flexural motions were also considered. Several cases with special devices for reducing gust response of the rotor were computed. The effect of Lock number was determined by comparison of several cases where all other principal parameters were held constant. Three hundred and three cases were evaluated in the study. A simple empirical expression, based on 50-ft/sec sine-squared gust cases, was developed that will adequately predict the rotor gust-load ratio, AT/Thover, for a wide range of helicopter and compound designs:

$$\frac{\Delta T}{T_{\text{hover}}} = \frac{0.057}{(C_{\text{T}}/\sigma)_{\text{hover}}} + 0.85 \frac{L_{\text{W}}}{T_{\text{hover}}} - C$$
 (1)

A principal finding is that the present MIL-S-8698 (ASG) requirements are not adequate and are too severe for modern high-speed helicopters. Recommendations for an improved design specification and future investigation are included in this report.

FOREWORD

An analytical investigation of gust responses of helicopters at high forward speeds was conducted at the Bell Helicopter Company (BHC) under U. S. Army Contract DA 44-177-AMC-308(T) (Task 1F162204A14608) from June 24, 1965 to April 26, 1967. The program was sponsored by the U. S. Army Aviation Materiel Laboratories (USAAVLABS), Fort Eustis, Virginia. Mr. J. H. McGarvey was the technical representative for USAAVLABS.

Technical information concerning articulated rotors was provided by Kaman Aircraft Company. In addition to the authors of this report, principal Bell Helicopter Company personnel associated with the project were Messrs. B. Bird, G. Brooks, and G. Weber.

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LIST OF SYMBOLS

Α .	vector of allowable errors in trim solution
$^{\Lambda}$ a $_{f x}$	change in forward acceleration (g)
Δ a $_{f z}$	change in vertical acceleration (g)
^a l	rotor flapping coefficient, fore-and-aft component (rad)
В	coefficients in rotor blade bending-moment analysis
Ъ	number of blades for rotor
C	constant
[c]	structural damping matrix
$c_\mathtt{L}$	lift coefficient for blade segment
\mathtt{C}_{T}	rotor thrust coefficient
CF	centrifugal force (lb)
С	rotor blade chord (in.)
cg	center of gravity
D	rotor diameter (ft); aerodynamic drag force (lb)
DL	rotor disc loading: weight/rotor area (lb/sq ft)
đ	distance from the origin to the point considered (ft)
E	error vector for one trim iteration
Ē	vector of error magnitudes for a trim iteration
EI	section bending stiffness (lb-in.2)
e	flapping hinge offset (ft)
F	aerodynamic force (lb)
Ť	net applied force vector in general equation of motion
F_{H}	internal horizontal force at flapping hinge (lb)

Fv	internal vertical force at flapping hinge (1b)
$F_{o}(\psi)$	applied force in flapping equation (1b)
$ \begin{bmatrix} F_1 \\ F_2 \\ F_3 \end{bmatrix} $	force matrices for stopped- or trailed- rotor analysis
ं	net applied moment vector in general equation of motion
g	acceleration due to gravity (ft/sec^2)
g _{HOR}	horizontal acceleration (g)
g _ο (Ψ)	coefficient of $\boldsymbol{\beta}$ in the flapping equation of motion
Нg	gust ramp length (ft)
ৰ্ম	angular momentum vector (slug-It2/sec)
h _o (ψ)	coefficient of $d\beta/d\psi$ in rotor flapping equation
I(D)	product of Wagner function and Buettiker function
ITORS	total torsional inertia of the drive system (lb-insec2)
1 x	mass moment of inertia about the x-axis (1b-insec2)
Ixz	product of inertia about the y-axis (lb-insec2)
I _y	mass moment of inertia about the y-axis (1b-insec2)
Iz	mass moment of inertia about the z-axis (lb-insec2)
ī	unit vector along x-axis of respective coordinate system
j	unit vector along y-axis of respective coordinate system
K	spring constant for rotor hub (ft-lb/rad)

Кg	gust-alleviation factor
Kgadj	adjusted gust-alleviation factor for tandem configuration
$\kappa_{ t g_{ t r}}$	gust-alleviation factor for a rotor
Kgw	gust-alleviation factor for a wing
k	variables in induced velocity equation
[k]	structural stiffness matrix
k	unit vector along z-axis of respective coordinate system
L	applied moment about the x-axis (ft-lb); aerodynamic lift force (lb)
ΔL	change in wing lift (1b)
$\mathbf{L}_{\mathbf{W}}$	total wing lift (1b)
M	applied moment about the y-axis (ft-1b)
$M_{B_{\dot{1}}}$	beamwise bending moment at ith station of blade (upper surface in compression) (inlb)
MC _i	chordwise bending moment at ith station of blade (trailing edge in compression) (in1b)
$\begin{bmatrix} M_{\mathbf{C}_1} \\ M_{\mathbf{C}_2} \end{bmatrix}$	cosine components of applied moment on rotors 1 and 2 for maneuver rotor equations (ft-lb)
M _{GUST}	blade bending moment due to a gust (inlb)
MP	moment at center of rotor hub (ft-lb)
MS ₁	sine components of applied moment on rotors l and 2 for maneuver rotor equations (ft-lb)
MS ₂	blade bending mement at them (in alb)
MSTEADY	blade bending moment at trim (inlb)
^M t	advancing blade-tip Mach number
m	mass $(lb-sec^2/ft)$

[m]	structural mass matrix
N	applied moment about the z-axis (ft-lb)
Δn	<pre>gust-load factor; change in normal acceleration (g)</pre>
$\overline{\Delta n}$	incremental rotation of coordinate system (rad)
$\Delta {\mathsf n}_{f r}$	change in normal acceleration due to rotor (g)
0	origin of moving coordinate system
δ	origin of fixed reference system
ō	vector from $\overline{0}$ to 0
PCG	prop-rotor collective-pitch governor
P(x,y,z)	a point in the (x,y,z) system
P	roll rate in body coordinates (rad/sec)
Q	vertical shear at rotor hinge point (lb)
$Q_{\mathbf{R}}$	torque required in drive system equation (ft-lb)
Q_S	torque supplied in drive system equation (ft-lb)
q	pitch rate in body coordinates (rad/sec)
R	radius of rotor (ft)
r	yaw rate in body coordinates (rad/sec)
r ₁ }	coefficients in Wagner Function
S	area of rotor or wing (ft ²)
SHP	shaft horsepower (hp)
S_{B_i}	beamwise shear at ith blade station (lb)
Sci	chordwise shear at ith blade station (lb)
TRSWC	tail-rotor sidewash coefficient
[T]	coordinate transformation matrix

Δ T .	change in thrust (lb)
$^{\mathrm{T}}$ hover	rotor thrust in hover (1b)
U _P	wind velocity component perpendicular to blade-span axis and to U_T (ft/sec)
$\mathbf{u}_{\mathbf{T}}$	wind velocity component perpendicular to blade-span axis and to axis of no feathering (ft/sec)
V	forward velocity of rotorcraft (ft/sec)
v _c	velocity of origin of moving system (ft/sec)
$v_{\mathbf{g}}$	vertical gust velocity (ft/sec)
$\mathtt{v}_\mathtt{i}$	induced velocity (ft/sec)
v_p	<pre>velocity of a point relative to fixed reference (ft/sec)</pre>
$\Delta v_{\mathbf{p}}$	dynamic out-of-plane velocity (ft/sec)
V _s	velocity of main-rotor swashplate (ft/sec)
Δ V $_{f T}$	dynamic in-plane velocity (ft/sec)
$v_{\mathbf{x}}$	intermediate velocity component (ft/sec)
W	weight (lb)
X	force applied in x-direction (lb)
$\left\{\mathbf{x}\right\}$	structural displacement vector
x_{B}	body system x-coordinate
$\mathbf{x}_{\mathbf{F}}$	fixed system x-coordinate
$x_{i,j}$	state variables at jth blade station
* _P	${f x}$ -position of any point on rotorcraft relative to fixed reference
Y	force applied in y-direction (lb)
y _B	body system y-coordinate
y _F	fixed system y-coordinate

Z	force applied in z-direction		
\mathbf{z}_{B}	body system z-coordinate		
$\mathbf{z}_{ extsf{F}}$	fixed system z-coordinate		
zo	state vector in trim iteration procedure		
GREEK LETTERS			
α	angle of attack of the airfoil (rad)		
α _C	angle of attack of the swashplate (rad)		
$\Delta lpha_{f r}$	change in angle of attack on the rotor (rad)		
β	rotor flapping angle (rad)		
β_{0}	coning angle of the rotor (rad)		
Y	Lock number		
Δ	prefix indicating increment		
δο }			
δ ₁	coefficients for nondivergent-drag equation (dimensionless, /deg, /deg2)		
δ ₂	(dimensionless, /deg, /deg-)		
δ3	angle determining pitch-flap coupling (deg)		
θ	rotor blade pitch angle (deg,rad)		
$\Delta oldsymbol{ heta}/\Delta oldsymbol{ heta}$ n	blade pitch change rate due to bobweight (deg/g)		
$\boldsymbol{\theta}_{\mathrm{D}}$	dynamic pitch change (rad)		
$^{oldsymbol{ heta}_{\mathbf{T}}^{oldsymbol{ heta}}}$	total blade twist (rad)		
θο	geometric blade pitch at the root (rad)		
λ	inflow ratio		
$\overrightarrow{\lambda}$	average inflow ratio		
μ	rotor advance ratio		
μg	mass ratio		
ρ	air density (slug/ft ³)		

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	DIST OF SIMBOLS - Continued
P	vector from cg to a point on the body
σ	rotor solidity
Φ(s)	Wagner Function
φο	out-of-plane slope at blade root (rad)
X	induced velocity angle correction for rear rotor of tandem configuration (rad)
ψ	azimuth angle (deg)
$\Omega_{\mathbf{i}}$	angular speed of ith rotor (rad/sec)
$\hat{\boldsymbol{\omega}}$	angular speed of body (rad/sec)
OPERATORS	
D	differentiation with respect to time in body reference
D	differentiation with respect to time in fixed reference
(·)	differentiation with respect to time
(')	differentiation with respect to azimuth angle
SUBSCRIPTS	
В	body
С	moving reference origin
D	dynamic
F	fixed
g	gust
Н	horizontal
R	rotor
S	swashplate
v	vertical
W	wir

CONFIGURATION TYPES

CSRH compound single-rotor helicopter

PSRH pure single-rotor helicopter

SSH side-by-side helicopter

TRH tandem-rotor helicopter

GUST TYPES

RFTP rooftop-gust shape; function of space but not

of time (implies gradual penetration by rotorcraft); gust velocity is vertical

RMPV vertical ramp-gust shape (spatial function)

SEDV sharp-edged vertical-gust shape (spatial function)

SSQH sine-squared horizontal-gust shape (spatial

function); Vg is directed aft

SSQL sine-squared horizontal-gust shape (spatial

function); V_g is lateral

SSQV sine-squared vertical-gust shape (spatial

function)

SUDH sudden horizontal gust; gust velocity is the

same at all points on the rotorcraft at any time (function of time but not of space--no penetration is implied); Vg is directed aft

SUDL sudden lateral gust (time function only)

SUDV sudden vertical gust (time function only)

ROTOR HUB TYPES

AR articulated rotor

RR rigid rotor

SR semirigid or teetering rotor

LIST OF CASES

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71-110	CSRH, SR, Variable Speed 160	192
111-116	CSRH, SR, Variable Speed 162	194
117-122	CSRH, SR, Variable Speed 164	194
123-128	CSRH, SR, Variable Speed 164	196
129-134	CSRH, SR, Variable Speed 164	196
135-138	CSRH, AR, Variable C $_{ m T}/\sigma$ 164	196
139-142	CSRH, AR, Variable $C_{ m T}/\sigma$ 166	196
143-146	CSRH, AR, Variable C_{T}/σ 166	196
147-150	CSRH, RR, Variable C_{T}/σ 166	198
151-154	CSRH, RR, Variable C_{T}/σ 166	198

LIST OF CASES - Continued

Case		Description Page	Results Page
155-158	CSRH, RR, Variable ${ m C_T}/\sigma$. 166	198
159-162	CSRH, AR, Variable ${ m C_T}/\sigma$. 166	198
163-166	CSRH, AR, Variable ${ m C_T}/\sigma$. 168	198
167-168	Omitted		
169-170	CSRH, AR, Speed = 250 Kt .	. 168	198
171-174	CSRH, RR, Variable $C_{\overline{T}}/\sigma$. 168	200
175-178	CSRH, RR, Variable C_{T}/σ	. 168	200
179-180	Omitted		
181-182	CSRH, RR, Speed = 250 Kt .	. 168	200
183-186	TRH, Variable $C_{\overline{\mathbf{T}}}/\sigma$. 174	204
187-190	TRH, Variable $C_{ m T}/\sigma$. 174	204
191-194	Trailed Rotor, Variable Speed	. 179	73
195-198	Stopped Rotor, Variable Speed	. 178	73
199-200	SSH, Helicopter Mode, Variabl Speed	e • 176	206
201-204	SSH, Transition Mode, Variabl	e 176	206
205-214	SSH, Airplane Mode, Variable Speed	. 176	206
215-216	Omitted		
217-218	PSRH, SR, Speed = 200 Kt .	. 154	186
219-220	PSRH, RR, Speed = 200 Kt .	. 154	. 186
221-222	PSRH, AR, Speed = 200 Kt .	. 154	186
223-226	CSRH, SR, Variable Speed .	. 168	200
227-230	CSRH, RR, Variable Speed .	. 170	200

LIST OF CASES - Continued

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Case	Description Page	Results Page
231-234	CSRH, AR, Variable Speed 170	200
235-237	PSRH, SR, Speed = 200 Kt 154	186
238-240	CSRH No. 2, SR, Speed = 150 Kt . 172	202
241-242		202
243-249	PSRH, SR, Variable Speed 154	186
250-262	CSRH No. 2, SR, Speed = 150 Kt . 172	202
263-264		188
265-268	PSRH, RR, Speed = 120 Kt 156	188
269	CSRH No. 2, SR, Speed = 150 Kt . 172	202
270	PSRH, SR, Speed = 120 Kt 156	
271	Omitted	188
272	TRH, Neutral cg, Speed = 200 Kt 174	201
273	Omitted	204
274	TRH, Forward cg, Speed = 200 Kt 174	
275-277	CSRH No. 2, SR, Speed = 150 Kt . 172	2 04
278-289	PSRH. AR Vaniable grant	202
290-301	PSRH SR Vaniable and	188
302-313		190
- 320	PSRH, RR, Variable Speed 158	190

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INTRODUCTION

Rotary-wing aircraft experience milder reactions to gusts than do most fixed-wing aircraft. One of the earliest reports of this difference, a paper by Focke (1), presents qualitative reactions of two pilots on a dual flight, one in a helicopter with side-by-side rotors and the other in a fixed-wing airplane. A similar test was conducted later by NACA (2) with instrumentation to measure normal forces in the aircraft flying through turbulent air.

The relatively mild reaction of the rotary-wing aircraft is not substantiated by the simple theoretical expressions currently in use, particularly those that evolved from fixed-wing experience. Figure 1 shows an example of gust-load factors due to sharp-edged gusts, computed by NACA's Charts for Estimation of Longitudinal Stability Derivatives for a Helicopter Rotor in Forward Flight (3). This procedure neglects stall and compressibility effects and assumes instantaneous changes in rotor angle of attack, induced velocity, and blade flapping.

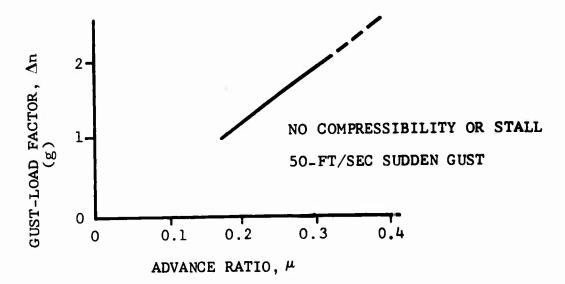


Figure 1. Gust-Load Factor Computed for the UH-1B Helicopter Using Linear Theory.

Current military design requirements (4) permit the use of an alleviation factor which is a function of rotor disc loading. However, this factor is unity for disc loadings greater than 6 pounds per square foot, as shown in Figure 2.

At high speeds and for disc loadings greater than 5 pounds per square foot, the computed gust-load factors are very high. When, in addition, maneuver loads are superimposed on gusts (as has occasionally been required in certain design studies), an

unrealistic design situation is created. The rapid development of compound aircraft and helicopters with higher forward speeds and disc loadings has made the current method of determining gust response prohibitively conservative.

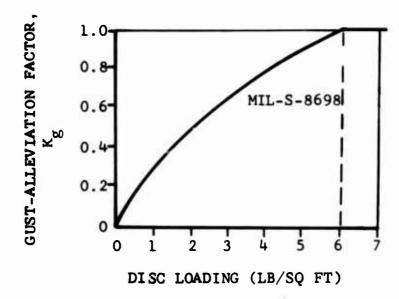


Figure 2. Gust-Alleviation Factor as Allowed by Military Specification.

On the other hand, recent studies indicate that the thrust capability of the rotor decreases with increasing advance ratio. The aerodynamic limit shown in Figure 3 is calculated by a digital method based on Gessow's development (5) and includes the effects of stall and compressibility. Also shown in Figure 3 is a practical limit based on flight test data (6). The practical limit is a result of oscillatory rotor loads and stall flutter effects, and is the controlling limit on rotor thrust capability at high advance ratios. This conclusion is supported by the findings of Ham and Young (7).

Unloading the rotor by adding a wing would give the rotor a greater margin to accept gusts. The advantage, however, is not as great as might be expected, because the rotor will usually assume the larger share of the lift increase resulting from gusts, as shown by tests with the AVLABS-Bell High-Performance Helicopter (6). The military design specification would allow a gust-alleviation factor that is unrealistically low for an unloaded rotor, illustrating again that a revision of the reduirements is necessary.

The desirability of a detailed study to bring the treatment of gust effects on rotary-wing aircraft up to par with that of fixed-wing technology was pointed out in 1965 (8). Sine-

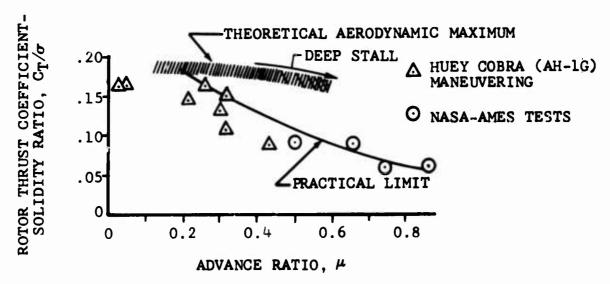


Figure 3. Rotor Limits as a Function of Advance Ratio.

squared gust shapes were considered instead of sharp-edged gusts, and a mass ratio replaced disc loading in the determination of the gust-alleviation factor. Figure 4 shows the result of that study. It indicates a considerable reduction of the gust-alleviation factor from the present requirements. The scope of that study, however, was insufficient to define new requirements for all contemporary types of rotary-wing aircraft. Furthermore, gradual penetration into the gust, nonsteady aerodynamics, and aeroelastic feedback were not considered.

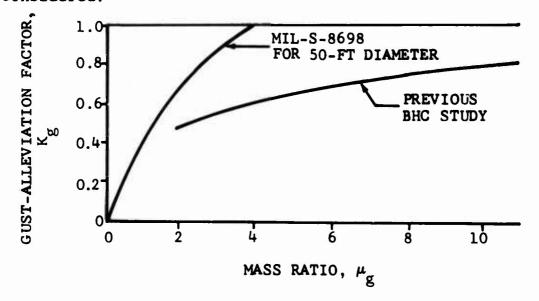


Figure 4. Results of a Previous Gust Study in Comparison With MIL Requirements.

These factors are considered and evaluated in this study. Recommendations for improved design criteria and future studies are presented herein.

Also included in this report are the basic mathematical equations and a discussion of the computational procedures used. A description of the analysis is presented in Program C81-11
Rotorcraft Flight Simulation (9), which was prepared in support of this study. Reference 9 is available at no charge upon request from Bell Helicopter Company, PO Box 482, Fort Worth, Texas 76101.

A magnetic tape library program providing data storage and retrieval of the time histories of 124 variables each for 94 maneuvers has been prepared. This program permits the examination of maneuver variables, some of which are not presented in this report, without recourse to computer reruns of the cases studied. This magnetic tape library program will be made available on a loan basis from the US Army Aviation Materiel Laboratories to investigators intent upon further studying the subject reported herein.

CONCLUSIONS

The universal maneuver computing program developed for this contract permits study of the gust response of a wide variety of VTOL aircraft configurations and rotor systems. Gust shape and intensity were varied, as were forward speed, disc loading, rotor thrust coefficient-solidity ratio, and advancing-tip Mach number. In all, 303 cases were investigated, from which the following principal conclusions are drawn:

- l. The gust-alleviation factors, K_g , computed in this study indicate that the requirements of MIL-S-8698 (ASG) do not adequately provide for the conditions of modern helicopters, and are in need of revision. The use of a rotor mass ratio, μ_g , to determine K_g by analogy with the fixedwing approach, as suggested in Reference 8, also does not give satisfactory results.
- 2. The most important result of the study, from a design and requirements point of view, is the finding that for all the helicopters and compounds investigated the rotor gust-load ratio, $\Delta T/T_{hover}$, can be expressed by a simple empirical expression as a function of the rotor thrust coefficient-solidity ratio in hover, CT/σ , and the wing lift ratio, LW/Thover, prior to the gust:

$$\frac{\Delta T}{T_{\text{hover}}} = \frac{0.057}{\left(C_{\text{T}}/\sigma\right)_{\text{hover}}} + 0.85 \frac{L_{\text{W}}}{T_{\text{hover}}} - C \tag{1}$$

This method gives reasonable accuracy with appropriate conservatism with $C \approx 0.2$ for semirigid (teetering) rotors and about 0.1 for rigid and articulated rotors.

For a compound helicopter the wing gust load may be determined separately, using conventional fixed-wing methods. An alleviation of the wing gust load, owing to the interaction with the rotor, was identified and found to be related to the rotor thrust coefficient, $C_{\rm T}/\sigma$. It is believed that this approach, after further refinement, presents a convenient basis for design rules and gust requirements.

- 3. The relative effects of various parameters on gust response can be summarized as follows:
 - Disc loading: Little influence
 - Rotor thrust coefficient-solidity ratio, C_T/σ : Major effect (see equation (1))

Compounding:

Considerable effect at high

values of C_T/σ due to lift

sharing with a wing

Rotor type:

Some effect, depends on dynamics

Number of blades:

Little effect

Number of rotors:

Increased effect for tandem

configuration

Forward velocity and advancing-tip

Mach number:

Little influence

Lock number:

Slight reduction of gust load with increased Lock number

Pitch-flap coupling:

Little effect

Pitch-cone coupling:

Appreciable effect

Bobweight in collective system:

Appreciable effect

RPM effects:

Not investigated

Rotor-blade

planform taper:

Not investigated

Rotor-blade cg-ac offset:

Not investigated

- Gradual gust penetration, nonsteady rotor aerodynamics and aeroelastic feedback proved to be the most influential factors for sharp-edged vertical gusts. For sine-squared gust shapes, the effects of gradual gust penetration appear to be most prominent. After various gust shapes were investigated (sharp-edged, sine-squared, ramp, rooftop, horizontal), a sine-squared gust with a maximum velocity of 50 feet per second and a ramp length of 90 feet was selected as the best representation for the detailed analysis.
- Gust effects on tilt-rotor configurations, during conversion and in the high-speed airplane mode, were evaluated. Gust loads on the stopped-rotor and trailed-rotor configurations were investigated in a separate analysis. Flapping stability at high advance ratios in relation to gust disturbances was studied briefly. Although no general conclusions are formulated in regard to these various subjects, important information is presented in this report for specific design conditions.

RECOMMENDATIONS

- 1. A broad range of configurations and parameters was investigated using a sophisticated mathematical model developed as a part of the study. This approach produced gross answers to questions of gust response for a wide variety of rotarywing VTOL aircraft. This broad approach, however, would not permit detailed studies of key parameters without undue expansion of the scope of the work. Yet it is of interest to make small incremental changes in a number of specific parameters (Lock number, ratio of wing lift to rotor lift, gross weight, etc.). Therefore, further studies, supplementing the present results, are recommended.
- 2. New gust requirements, differing from those of MIL-S-8698 (ASG), and applicable to all pure and compound helicopters, should be formulated. These requirements should relate the maximum rotor gust load directly to the hovering thrust coefficient-solidity ratio, CT/σ , and to the ratio of wing lift to hovering thrust prior to the gust. Conservative values of the maximum wing gust load can be calculated conventionally, and possibly adjusted by using a rotor-interference factor.
- 3. Considerable nose-up pitching was computed for the tandem cases with aft cg. For the forward cg case, the configuration is stable and the gust response agrees with the thrust change formula of the preceding section. The stability characteristics of the chosen design examples are uncertain. A more thorough investigation, with emphasis on the parameters relating to pitch stability, is desirable.
- 4. Future analytical studies should include statistical methods for considering the effects of random gusts.
- 5. The conclusions of this study should be verified experimentally, particularly for the range of configurations and parameters of current production rotorcraft.

APPROACH AND SCOPE OF THE PROGRAM

Adequate treatment of the helicopter gust-response problem requires a degree of mathematical refinement which was impractical for engineering studies before the advent of large, high-speed computers. Although restraint is still necessary to keep computer time and storage requirements within reason, a considerable advancement of the state of the art is now possible. The development of a computing procedure to handle the detailed gust-response analysis was a principal part of the work done for this investigation.

One of the major goals of this study was to consider the effects of gradually penetrating a gust shape, as opposed to all points on the rotorcraft sensing a given gust velocity at the same time. To denote the cases where gradual penetration was used, reference will be made to a specific gust shape, such as sharpedged, sine-squared, or ramp. For cases where gradual penetration was not used (i.e., instantaneous immersion of the entire aircraft), the disturbance will be referred to as a sudden gust.

The aim of the study was to establish a practical method for determining gust-response design requirements for rotorcraft. A procedure involving two steps was originally planned: first, the calculation of response to a sudden gust using a minimum of analytical refinement; second, the use of a factor to account for effects not included therein. The simplified analysis would replace the response formulas given in References 10 or 11, and the factor would be similar in application to the gust-alleviation factor discussed in Reference 11. In general, the gust response for each combination of physical parameters and flight conditions was computed both with and without the added, detailed refinements. A gust-alleviation factor due to the refinements was determined for each combination by a comparison of the results. Although this approach was followed throughout the study, an overall review led to the derivation of a rule for rotorcraft gust response which can be used without any preliminary analysis or additional factors.

Since the formulas developed for the calculation of fixed-wing gust response usually assume a sudden immersion in a gust, some comparisons with existing theory can be made for sudden-gust responses calculated with the simplified analysis.

Figure 1 (page 1) shows that the calculated load factor increases rapidly with forward speed when the method of Reference 3 is used. These results are obtained by assuming an instantaneous angle-of-attack change of

$$\Delta \alpha_{\mathbf{r}} = \tan^{-1} \frac{V_{\mathbf{g}}}{V} \tag{2}$$

It is assumed that $\Delta\alpha_r$ is applied suddenly and simultaneously over the entire rotor disc, and that induced velocity and blade flapping adjust instantaneously. Additionally, no effects of stall and compressibility are taken into account. It is obvious that each of these assumptions implies unrealistic situations. Removing the assumptions may have an important bearing on the results, but it will also quickly increase the computational complexities.

The theories of linear aerodynamics are entirely inadequate at the high forward speeds of interest to this study. Therefore, it is assumed that methods such as those developed by NACA (5) can be used to account for stall and compressibility effects as a part of the short-method baseline. The effect of this modification on the calculated gust-load factor for the case of sudden immersion in a gust is shown in Figure 5.

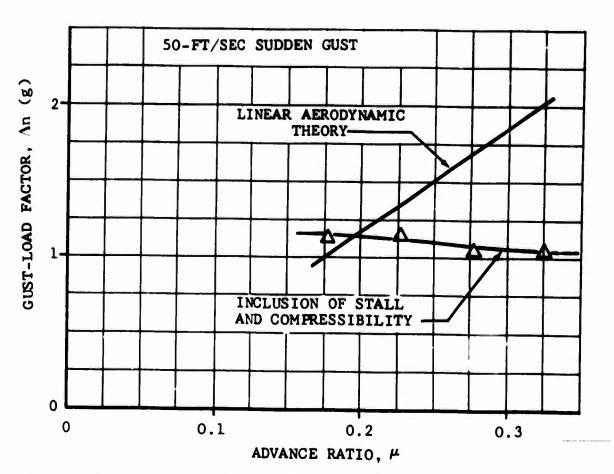


Figure 5. Gust-Load Factor for the UH-1B, Showing Importance of Using Improved Aerodynamic Methods Over Linear Theory.

For the simplified method, sudden immersion of the entire rotorcraft in a gust and steady-state aerodynamics are assumed. However, stall and compressibility effects on the rotor blades are included.

The possibility of using a stability derivative technique for gust response was considered. The equations and coefficient definitions given in Reference 12, Section 14, constitute an analytical basis for this method. Gust-response characteristics calculated from stability-derivative equations would not reflect effects of stall and compressibility. Only small perturbations about the trim point can be allowed because of the variations in stability-derivative values. At best, this technique would be more limited than the simplified method previously described. Early in the course of this study it was decided that the stability-derivative method would not be used.

The detailed analysis of gust response includes:

- gradual penetration,
- nonsteady aerodynamics,
- aeroelastic feedback, and
- a realistic gust-velocity function.

The gradual penetration effect is obtained by assuming that the gust velocity is a function of location along the zero heading axis. As the rotorcraft moves along this axis, gust-velocity values at different locations on the fuselage or rotors will not necessarily be the same at a given time. Pitching motion of the fuselage and rotor blade flapping are emphasized by simulating the rotorcraft penetrating a gust as a function of time. Gradual penetration is considered to be more realistic than the sudden immersion assumption.

The simplest way of handling aerodynamic variations is to assume that the situation under consideration can change from one steady-state condition to another instantaneously. Nonsteady (transient or time variant) aerodynamic effects were treated in an elementary way by Lucassen and Drees (13). The principal nonsteady aerodynamic effect on gust response included in this analysis is the behavior of lift following a change in blade (or other aerodynamic surface) angle of attack.

The effect of gust shapes was first treated in Reference 8. The most refined approach to date is probably that of Segel (14), but limitations on computer storage and run time precluded the use of that method. Instead, a simplified approach is used. By a gust-velocity function is meant a mathematical equation or table such that, given the position \mathbf{x}_p of any point on the rotorcraft, the gust velocity at that point can be obtained. It should be noted that, in general, \mathbf{x}_p is a function of time.

Figure 6 shows the individual effects, computed with the present program, of gradual penetration, nonsteady aerodynamics, and realistic gust-velocity functions. An appreciable variation is registered in each case.

FORWARD SPEED = 150 KT DISC LOADING = 5.6 LB/SQ FT

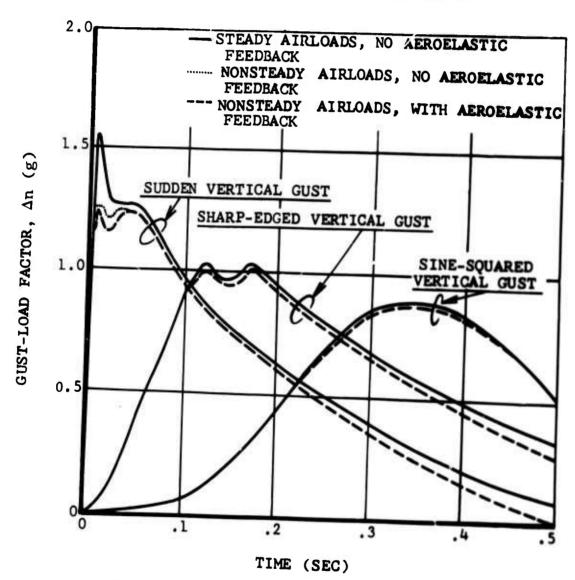


Figure 6. Effects of Gradual Penetration, Nonsteady Aerodynamics, Aeroelastic Feedback, and Gust Shape.

A summary of these effects is presented in Figure 7. It is shown that the nonsteady aerodynamics have a large influence if applied in the case of a sudden immersion. The effect of gradual penetration is more pronounced. The combination of nonsteady aerodynamics and gradual penetration shows that the nonsteady aerodynamics have become an insignificant influence. Adding the effect of a sine-squared gust produces another significant effect.

One more major item was investigated in connection with gust response: the inclusion of aerolastic feedback in the rotor aerodynamics. This was done by computing the velocities and pitch variations associated with blade elastic deformations and adding these to the components used for rigid blade aerodynamic analysis. This refinement has increased considerably the computer program complexity and running time, and the preparatory work required to arrive at feasible rotor systems that would not show undesirable resonances. Figures 6 and 7 show that aeroelastic feedback has a second-order effect on the gust-load factor. Another example of the effect of aeroelastic feedback is given in Figure 8. It is seen that the maximum rotor thrust is little affected, but that larger variations are found for the rotor blade-oscillatory bending moments.

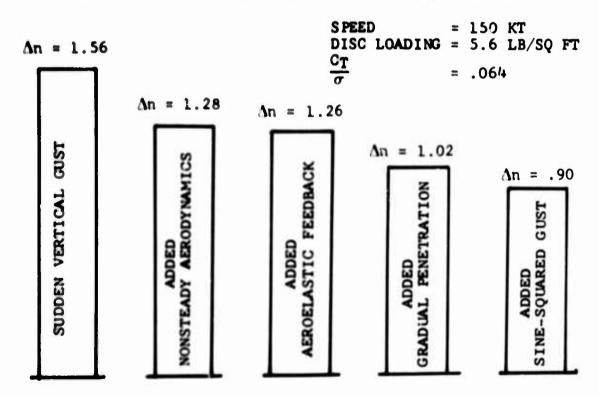


Figure 7. Bar Graph Illustrating the Relative Importance of the Most Influential Effects in the Detailed Analysis of Gust Response.

Legend: 1. Gradual Penetration, Without Aeroelastic Feedback 2. Gradual Penetration, With Aeroelastic Feedback

100 KT 324 RPM 6600 LB G.W.

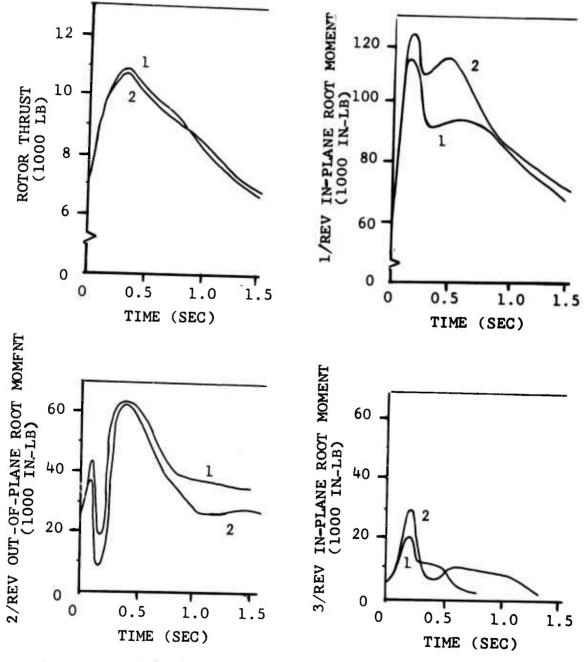


Figure 8. Calculated Time Histories of UH-1B Rotor Loads for 30-Ft/Sec Sharp-Edged Gust.

DEFINITION OF GUST-ALLEVIATION FACTOR

A main objective of this study was to determine for each configuration and condition the ratio of the maximum gust load due to a sine-squared gust to the maximum gust load due to a sudden gust. In this reference the maximum gust load due to a sudden gust was computed using the assumptions of the simplified analysis. The maximum gust load due to the sine-squared gust was computed using various combinations of effects from the detailed analysis.

A value of this ratio, called the gust-alleviation factor, would be given for a particular case by

$$K_g = \frac{\Delta n_{sine-squared}}{\Delta n_{sudden}}$$
 (3)

Since K_g may be dependent on one or more aspects of the configuration or condition, gust-factor functions, or variations of K_g with case parameters, will be discussed in a later section.

The gust-factor calculation using a sine-squared gust was considered in Reference 8, but gradual penetration and non-steady aerodynamics were not considered. It was proposed in Reference 8 that K_g might be a function of a mass ratio (see Figure 4, page 3),

$$\mu_{g_{rotor}} = \frac{4W/S}{\rho \pi Rg} \tag{4}$$

by analogy with fixed-wing practice, where the factor

$$\mu_{\text{g}_{\text{fixed-wing}}} = \frac{2W/S}{\text{mpcg}}$$
 (5)

is used.

As a result of the study, it became apparent that the massratio approach to determining a gust factor Kg does not lead to satisfactory results. Attempts were therefore made in the final analysis to seek a new way to arrive at useful rules for design requirements.

SCOPE OF THE GUST STUDY

The scope of the gust study is summarized as follows:

- Development of the mathematical tools necessary to handle the problem.

- Subjection of a wide variety of rotary-wing configurations to sudden and sine-squared gusts, both vertical
 and horizontal, while varying forward speed, disc loading, blade thrust coefficients, Lock number, etc.
 Table I and Appendix II summarize the cases considered,
 together with principal rotor and wing parameters, trim
 values, gust description, and response results. Rectangular planform rotor blades with linear twist and zero
 cg-ac offset were used in all cases.
- Development of design rules which may be used for future requirements.

	TABLE I. SUMMARY	RY OF CASES		
Configuration	Variable	Rotor	No. of Cases	Case Number
Pure Single- Rotor Helicopter	Mach Number	Semirigid	16	1 - 16
	Disc Loading and Thrust Coefficient	Semirigid	18	17 - 32 217 - 218
		Articulated and Rigid	4	219 - 222
	Gust Profile	Semirigid	7	33 - 34
	Gust Direction	Semirigid	4	35 - 38
	Rotor Type	Articulated and Rigid	32	39 - 70
Compound Single- Rotor Helicopter	Mach Number	Semirigid	04	71 - 110
	Disc Loading and Thrust Coefficient	Semirigid	28	111 - 134 223 - 226
		Articulated and Rigid	∞	227 - 234
	Rotor Type	Articulated and Rigid	1 11	135 - 166 169 - 178 181 - 182
Pure Tandem Helicopter	Gust Profile	Articulated	10	183 - 190 272, 274

	• of Case Cases Number	4 191 - 194	4 195 - 198	2 199 - 200	4 201 - 204	205 - 214	7 235 - 237 247 - 249 269	3 238 - 240	4 243 - 246	3 250 - 262	263 - 264	5 265 - 268 270	3 275 - 277	5 278 - 313
	No. of Rotor Case	7	7		7	10			7	, 13	2	υ,	3	36
TABLE I - Continued	Variable	Forward Speed	Forward Speed	Helicopter Mode	Transition Mode	Airplane Mode	Gust-Alleviation Devices	Gust Strength	Low Speed	Effects of Nonsteady Aero, Gradual Penetration and Aeroelastic Feedback	Horizontal Side Gust	Hub Spring	Blade Torsional Restraint	Lock Number
	Configuration	Trailing Rotor	Stopped Rotor	Tilt Rotor			Special Cases							

DEVELOPMENT OF MATHEMATICAL MODEL

GENERAL DISCUSSION

The principal mathematical tool used to compute the responses of VTOL aircraft to gusts is a further development of a previously available BHC computing program. References 8, 15, and 16 describe the early program, with its applications to a wide variety of problems, such as performance, stability and control, maneuvers, determination of structural loads in rotor blades, autorotational landings, and the effects of gusts on rotary-wing aircraft. The principal improvements in the mathematical representation of the aircraft that have been made during the course of this study are:

- Adding roll and lateral degrees of freedom, to complete the freedom of the rigid-body fuselage in space.
- Adding a second complete rotor system representation which can be oriented to act as a tail rotor, the aft rotor of a tandem helicopter, or the left rotor of a side-by-side rotorcraft configuration.
- Including aeroelastic feedback capability in the rotor-load calculations.
- Enlarging the boundary conditions to permit the evaluation of rigid, semirigid, and articulated rotors with two, three, or four blades.
- Refining the aerodynamic theory for rotors and fixed surfaces to include the effects of nonsteady aerodynamics.
- Refining the gust representation by including the effect of gradual immersion of the aircraft: first the front of the rotor, then the fuselage, and finally the elevator and tail rotor (in the case of a single-rotor helicopter).
- Adding planform taper to the rotor representation.

The various configurations that can be handled with this program are summarized in Table II. The most important built-in options are listed in Table III. Figure 9 presents the major building blocks of the program. A flow chart of the program is shown in Figure 10.

TABLE II. POSSIBLE CONFIGURATION VARIATION

- 1. Single-rotor helicopter with tail rotor
- 2. Counterrotating tandem-rotor helicopter
- 3. Counterrotating side-by-side-rotor helicopter
- 4. Propeller airplane (1 or 2 propellers)
- 5. Jet airplane (1 or 2 jets)
- Winged helicopter (any type)
- 7. Helicopter with 1 or 2 auxiliary propulsion units (props or jets)
- 8. Full compound helicopter (with wings and auxiliary propulsion)
- 9. Prop-rotor convertiplane
- 10. Tilt-wing convertiplane
- 11. Rigid, semirigid, or articulated rotors
- 12. 2, 3, or 4 blades on each rotor
- 13. Interconnect control couplings of swashplate with differential wing angle and elevator control. Rudder control through rotor control and/or fin lift control
- 14. Control features such as δ_3 , bobweights, etc.
- 15. Engine, rotor, and/or propeller governors

Most of the configuration variations are made possible by generalizations in the analysis. For example, for each rotor the location of the mast base or pivot point in three dimensions must be specified by input data. The mast length and inclination are also inputs. Thus the first three configurations can be included in one procedure. Provisions for differences in aerodynamic interference effects for these three types of rotorcraft are also controlled by input data.

Another technique used to change configurations is deletion logic. Having made provisions for two rotors, two propellers, two jet propulsion units, and wings, Configurations 4 through 8 of Table II can be constructed by deleting those items not required. The computer program contains conditional branches

TABLE III. AVAILABLE OPTIONS OF PROGRAM DETAIL

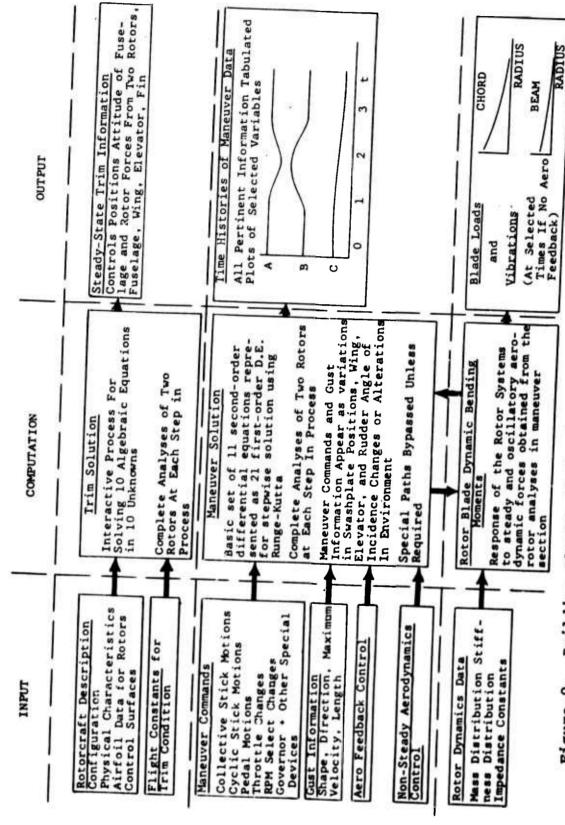
- la. Trim section only, providing performances, control position, stability derivatives
- 1b. Trim section and oscillatory rotor loads
- 2a. Basic maneuver section, not including rotor loads, aeroelastic feedback, or nonsteady aerodynamics. Permits study of aircraft reactions to displacements of pilot's controls and/or response to gusts and other external influences. Output includes aircraft position in space, rotor flapping, torque, rpm, etc.
- 2b. Add computation of rotor loads
- 2c. Add aeroelastic feedback
- 2d. Add nonsteady aerodynamics
- Documentation includes option to preserve data on library tapes

so that particular sections of the calculations can be skipped and quantities dependent on the skipped sections remain unchanged. For example, if no propellers are wanted, the propeller input data group is set to zero. Preceding entry into the subroutine for propeller analysis, the computer checks propeller data and reacts to the zero inputs by skipping that subroutine altogether. Propeller thrust and horsepower required remain at initialized values of zero and hence do not change the net forces and moments computed.

Other effects are generalized by branching to alternate procedures as required by the controlling input data. Rotor types and number of blades are examples. The convertiplane types (9 and 10 of Table II) are essentially different from the side-by-side-rotor helicopter only in rotor parameters and in capability of change in attitude of the rotor masts, either with or without accompanying change in wing incidence. These change capabilities are included in the data for the time-variant section.

The many features of the analysis and computer program pointed out in Tables II and III and Figure 8 are obtained by these techniques. The program, as Table III and Figure 9 indicate, has two major sections: (a) trim section and (b) maneuver section.

In the trim section the aircraft is brought to a stabilized trim, which becomes the initial condition for the maneuver



Building Blocks of the Rotorcraft Flight-Simulation Program. Figure 9.

section. Any realistic stabilized-flight condition can be specified by forward velocity, rate of climb, rpm, gross weight, etc. In the maneuver section the aircraft is subjected to a variation in conditions, which for this study was an external disturbance due to a gust.

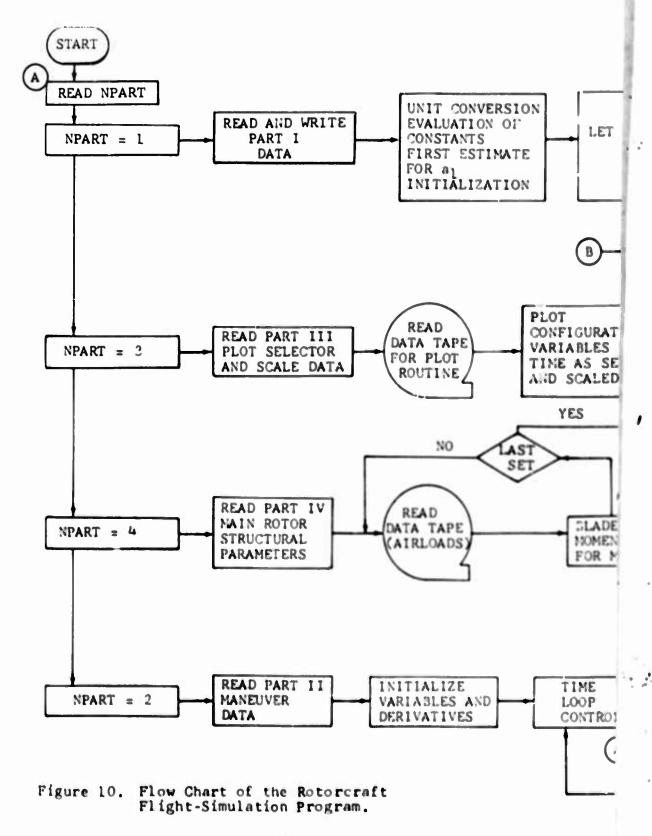
The operation of the program takes considerable skill, because the representation of the aircraft has become so detailed that it approaches the complexity of the actual rotorcraft. Specifically, for high forward speeds, a wrong elevator setting or a blade resonance owing to improper rotor dynamics will prevent the proper operation of the program. Furthermore, the many nonlinearities, such as those caused by rotor blade stall, may preclude finding a trim solution if the initial approximations require large iteration steps.

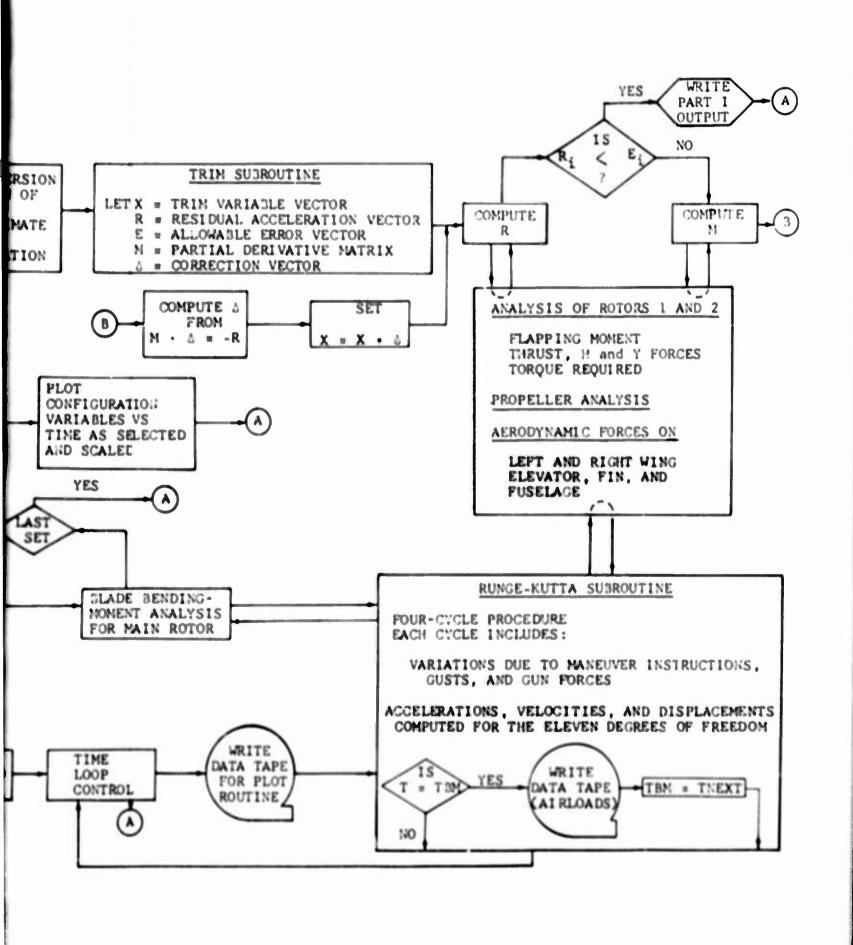
The running time of the program depends on the detailing options requested by the user. Approximate running times for an IBM 360 Model 65 computer, assuming that the trim condition is found within a reasonable number of iterations, are given in Table IV.

A condensed discussion of some of the topics and the organization of the program is given in this report. A detailed mathematical description of the program is given in Reference 9.

The effects of gusts on stopped and trailing rotors have been treated separately because the aerodynamic and dynamic analyses of the maneuver program are not believed to be applicable to the peculiar conditions that prevail for stopped rotor blades. The analytical approach is briefly described in a later section of this report. More detailed information is given in Reference 17.

TABLE IV. CO	MPUTING TIMES
Time to trim	2 min
100-time-points maneuver with- out rotor loads	4 min (includes trim)
100-time-points maneuver with rotor loads, no feedback	5.5 min (includes trim)
100-time-points maneuver with rotor loads and feedback	9 min (includes trim)
Inclusion of nonsteady air- loads	adds 2.5 min to above maneuver
Requesting loads on two rotors instead of one	adds 4 min



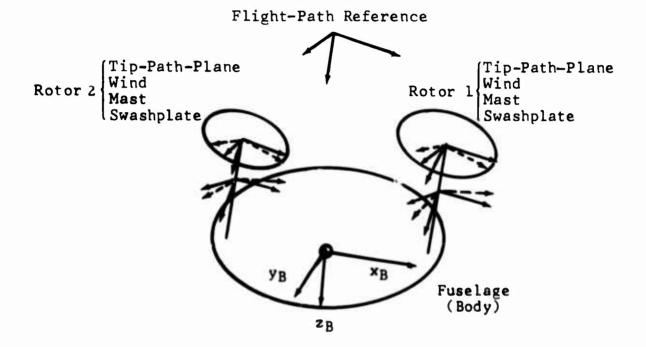


MANEUVER COMPUTING PROGRAM

Rigid motions of the rotorcraft can be fully described by the usual six body equilibrium equations, plus two flapping equations for each rotor and a drive-system rotation equation. The fuselage equations are written in body-axis reference as given by Etkin (12), to avoid variation in inertia parameters. The rotor equations are in tip-path-plane reference, and the drive-system rotation is referred to main (forward or right) rotor rpm for convenience. The ll basic equations state that for each degree of freedom the time derivative of momentum is equal to the sum of the relevant forces or moments.

For a trim solution, the momentum derivatives are zero and the equations are algebraic in the following control and attitude variables: the body Euler angles relative to a fixed reference system (three), rotor-flapping components relative to the swashplate (four), fore-and-aft and lateral cyclic stick position (two), collective-stick position (one), and pedal position (one). For maneuver considerations the conditions may be viewed as a set of second-order differential equations in displacements relative to the fixed reference. However, since velocity components in fuselage reference are important output items, a set of 21 first-order differential equations is used to simulate the rotorcraft's flight. The basic variables in this system are instantaneous linear and angular velocities of the body (six), instantaneous pitch and roll velocities of the rotors (four), the linear and angular displacements of the body relative to the fixed reference system (six), rotor attitude components relative to the swashplate axes (four), and the angular velocity of the drive system (one). Transformations of velocities from body to fixed reference and from tip-path-plane to swashplate reference are necessary as intermediate steps in the computational process.

The aerodynamic forces and moments acting on the rotorcraft are dependent on attitude and control-position displacements and velocities and variations in wind velocity. Generally, the aerodynamic forces are computed in one reference and are transformed to another for summing. For this reason, and because of the relationships among the mast, swashplate, and tip-pathplane, many transformations are necessary. Special subroutines were developed to handle passage from one to another of the following reference systems: fixed (one), body (one), flight path (one), mast (two), swashplate (two), tip-path-plane body (two), tip-path-plane wind (two), swashplate body (two), swashplate wind (two), and wind direction system at top of mast (two). These reference systems are shown schematically in Figure 11. The tip-path-plane-body reference system has its x-axis in the body xz-plane. The tip-path-plane-wind axis system has its x-axis in a plane normal to the tip-path plane and containing the wind vector.



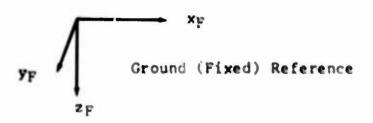


Figure 11. Schematic of Reference Systems.

Basic Equations of Motion

The equations of motion of a free body relative to a set of axes fixed to the body are derived in Reference 12 from the momentum-equilibrium expressions. The development is given in a more general form in Craig's dissertation on classical dynamics (Reference 18, Chapter XII). Using D and D to indicate differentiation with respect to time in the fixed and body reference systems respectively, the momentum equations may be derived as follows.

Consider a fixed coordinate system with origin $\overline{0}$ and a moving coordinate system (body reference system) with origin 0; x, y, z axes; and unit vectors \overline{i} , \overline{j} , \overline{k} . Let $\overline{0}$ be the radius vector from $\overline{0}$ to 0 and $\overline{\rho}$ the radius vector from 0 to a point P(x,y,z). The radius vector from $\overline{0}$ to P can then be written as $(\overline{0}+\overline{\rho})$. Let $\overline{\omega}$ be the rotational vector of the body coordinate system relative to the fixed system. Then

$$\overline{\mathbb{D}}(\overrightarrow{o} + \overrightarrow{\rho}) = \overline{\mathbb{D}}(\overrightarrow{o}) + \overline{\mathbb{D}}(\overrightarrow{\rho}) = \overline{\mathbb{D}}(\overrightarrow{o}) + \mathbb{D}(\overrightarrow{\rho}) + \overrightarrow{\omega} \times \overrightarrow{\rho}$$

Let $\overline{v_C}$ be the velocity of O relative to \overline{O} , and $\overline{v_p}$ the velocity of P relative to \overline{O} , and note that $D(\overline{\rho}) = 0$. Then

$$\vec{v}_{P} = \vec{v}_{C} + \vec{\omega} \vec{x} \vec{\rho}$$

and the angular momentum of the body is

$$\vec{h} = \int_{V} [\vec{\rho} x \vec{v}_{c} + \vec{\omega} x \vec{\rho}] dm$$

With F and G representing the net applied force and moment respectively, the momentum equations can be expressed as follows:

$$\vec{F} = \vec{D}(\vec{m}\vec{v}_{c}) = \vec{D}(\vec{m}\vec{v}_{c}) + \vec{m}\vec{\omega}\vec{x}\vec{v}_{c}$$

$$\vec{G} = \vec{D}(\vec{h}) = \vec{D}(\vec{h}) + \vec{\omega}\vec{x}\vec{h}$$
(6)

If $v_c, \overline{\omega}$, and $\overline{\rho}$ are expressed in terms of body reference components as

$$\vec{v}_{c} = U\vec{i} + V\vec{j} + W\vec{k}$$

$$\vec{\omega} = p\vec{i} + q\vec{j} + r\vec{k}$$

$$\vec{\rho} = x\vec{i} + y\vec{j} + z\vec{k}$$

the equations 4.4.3 and 4.4.4 of Reference 12 may be written directly from equation (6). The cross products of inertia involving lateral coordinates have been dropped due to the assumed symmetry of the body about an xz-plane. This reduces the components of h as follows:

$$\vec{h} \cdot \vec{i} = I_x p - I_{xz} r$$

$$\vec{h} \cdot \vec{j} = I_y q$$

$$\vec{h} \cdot \vec{k} = -I_{xz} p + I_z r$$

All other terms are retained.

In this analysis the center of gravity, the gross weight, and mass moments and products of inertia are assumed to include pylon and rotor blade weights. Variation in mast tilt is considered by computing a new cg location and new values of the inertia quantities. Rates of change in mass moments and products of inertia, which would appear in the components of $D(\bar{h})$, are not taken into account.

The drive-system rotation equation allows evaluation of Ω and Ω . The rotor angular velocities Ω_1 and Ω_2 are computed by applying the appropriate gear ratios to Ω . The rotor flapping equations are represented as the components of

$$I_{i} (\ddot{\beta}_{i} + \Omega_{i}^{2} \beta_{i}) = M_{i}, \quad i = 1, 2$$

where M_i and β_i are, respectively, applied moment and flapping angle viewed as harmonic series based on Ω_i , and the index i identifies the particular rotor.

The Euler-angle derivatives are introduced in Reference 12 by noting that an infinitesimal rotation Δn in time Δt can be written

$$\overline{\Delta n} = \overline{i}_3 \Delta \phi + \overline{j}_2 \Delta \theta + \overline{k}_1 \Delta \psi$$

where the subscripts indicate the axis system from which each component is obtained (Reference 12, Figure 4.2).

Then

$$\widehat{\Delta n} = \lim_{\Delta t \to 0} \frac{\widehat{\Delta n}}{\Delta t} = \widehat{i}_3 \dot{\phi} + \widehat{j}_2 \dot{\theta} + \widehat{k}_1 \dot{\psi}$$

Since

$$\vec{\omega} = p\vec{i} + q\vec{j} + r\vec{k}$$

$$[p, q, r] = [\vec{i} \cdot \vec{\omega}, \vec{j} \cdot \vec{\omega}, \vec{k} \cdot \vec{\omega}]$$

or

$$[p, q, r] = [\dot{\phi}, \dot{\theta}, \dot{\psi}] \begin{bmatrix} \vec{i} \cdot \vec{i}_3 & \vec{j} \cdot \vec{i}_3 & \vec{k} \cdot \vec{i}_3 \\ \vdots \cdot \vec{j}_2 & \vec{j} \cdot \vec{j}_2 & \vec{k} \cdot \vec{j}_2 \\ \vdots \cdot \vec{k}_1 & \vec{j} \cdot \vec{k}_1 & \vec{k} \cdot \vec{k}_1 \end{bmatrix}$$

The unit vector dot products are, by rows, the direction cosines for the Euler-angle velocity vectors relative to the body-axis system. Thus,

$$[p, q, r] = [\dot{\phi}, \dot{\theta}, \dot{\psi}] \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi & -\sin \phi \\ -\sin \theta & \cos \theta \sin \phi & \cos \theta \cos \phi \end{bmatrix}$$
(7)

These equations may be solved for $\dot{\phi}$, $\dot{\theta}$, $\dot{\psi}$, as given by equation 4.5.4 of Reference 12.

These relationships provide a means of determining the change in orientation of the body when p, q, and r are known. The rotor Euler-angle expressions are similarly derived except that ψ_i is assumed to be zero. The angular velocity $\mathbf{r_i}$, while not zero under this assumption, is small relative to Ω_i and is not included. Equations for ϕ_i and $\dot{\theta}_i$ can be read from Equation 7.

The Euler angular velocity expressions govern the orientation of the fuselage and rotors. The velocities in body reference (U, V, W) must be transformed into fixed reference components $(\dot{\mathbf{x}}, \dot{\mathbf{y}}, \dot{\mathbf{z}})$ to obtain distance traveled relative to the fixed system and heading and climb angles. The transformation matrix is given below for quick reference:

$$\begin{bmatrix} \cos\psi\cos\theta & \cos\psi\sin\theta\sin\phi & \cos\psi\sin\theta\cos\phi \\ -\sin\psi\cos\phi & +\sin\psi\sin\phi \\ \\ \sin\psi\cos\theta & \sin\psi\sin\theta\sin\phi & \sin\psi\sin\theta\cos\phi \\ +\cos\psi\cos\phi & -\cos\psi\sin\phi \\ \\ -\sin\theta & \cos\theta\sin\phi & \cos\theta\cos\phi \end{bmatrix} \tag{8}$$

The full set of equations of motion, including the orientation equations, is presented in component form in Table V. Expressions for the applied forces and moments, X, Y, Z, L, M, N, Q, M_{C_1} , M_{S_1} , M_{C_2} , M_{S_2} , are developed in detail in Reference 9.

	TABLE V. EQUATIONS OF MOTION
	/:·
X	= m (U + qW - rV)
Y	$= m (\dot{V} + rU - pW)$
Z	= m (W + pV - qU)
L	$= I_{xp} - I_{xz} + qr (I_{z} - I_{y}) - I_{xz}pq$
М	$= I_{y}\dot{q} + rp(I_{x} - I_{z}) + I_{xz}(p^{2} - r^{2})$
N	$= I_{z}r - I_{xz}p + pq (I_{y} - I_{x}) + I_{xz} qr$
Q _S	= $I_{TORS} \dot{\Omega} + Q_R$
M _G 1	$= -I_{b_1} \left(\dot{q}_1 + 2\Omega_1 p_1 \right)$
M _{S1}	$= -I_{b_1} \left(\dot{p}_1 - 2\Omega_1 q_1 \right)$
M _{C2}	$= -I_{b_2} \left(\dot{q}_2 + 2\Omega_2 p_2 \right)$
MS ₂	$= -I_{b_2} \left(\dot{p}_2 - 2\Omega_2 q_2 \right)$
$\dot{ heta}$	= $q \cos \phi - r \sin \phi$
$\dot{\phi}$	= p + q $\sin \phi$ $\tan \theta$ + r $\cos \phi$ $\tan \theta$
$\dot{m{\psi}}$	= $(q \sin \phi + r \cos \phi)/\cos \theta$
$\dot{\theta}_1$	= $q_1/\cos \theta_1$
$\dot{\phi}_1$	= p ₁
$\dot{ heta}_2$	= $q_2/\cos \theta_2$
$\boldsymbol{\dot{\phi}}_2$	= p ₂
[x, y,	z] = [U, V, W] [T]

Aerodynamic Forces and Moments

Rotors, Propellers, Auxiliary Propulsion

The rotor aerodynamic performance and airloads analysis is similar to that described by Blankenship and Harvey (15), but a number of minor improvements such as planform taper have been added (9). Both rotors are treated in the same manner and in the same subroutine. The aeroelastic-feedback mechanism appears as velocity terms added to both inflow and tangential velocities, and an added term for blade-pitch variation in the local angle-of-attack expression. These added quantities are computed in the rotor blade bending-moment section. The dynamic pitch change, $\Delta\theta_D$, dynamic out-of-plane velocity, ΔVP , and in-plane velocity, ΔVT , are used in the rotor equations thus:

$$\theta = \theta_{0} + \frac{\mathbf{r}}{R}\theta_{TW} - \tan \delta_{3}(\beta - \beta_{0}) + \Delta\theta_{D}$$

$$U_{p} = \left(\lambda \cos \beta - r \frac{\dot{\beta}}{\Omega R} - \mu \sin \beta \cos \psi\right) \Omega R - W_{Gust} + \Delta V_{p}$$

$$U_{T} = \left(\frac{r}{R} + \mu \sin \psi\right) \Omega R - U_{Gust} \sin \psi - V_{Gust} \cos \psi + \Delta V_{T}$$

$$\phi = \tan^{-1}\left(U_{p}/U_{T}\right)$$

$$\alpha = \theta + \phi$$

The velocity at the swashplate for the main rotor of a pure single-rotor helicopter is given by

$$\vec{v}_S = \vec{v}_C + \vec{\omega} \times \vec{\rho}_S$$

The expression for local inflow ratio is

$$\lambda = \overline{\lambda} + \frac{V_{x}}{\Omega R} \left[1 - (1 + k \cos \psi) \frac{4}{3} \frac{r}{R} \right]$$

where

$$\overline{\lambda} = (|V_S| \sin \alpha_C - v_i) / \Omega R$$

$$v_x = (1 + kk') v_i$$

$$\mu = |V_S| \cos \alpha_C / \Omega R$$

The angle of attack of the swashplate, α_{C} , is obtained from the components of $\overline{V_{\text{S}}}$.

k is a function of advance ratio discussed in Reference 19. k' is a function of ψ and r derived empirically to reproduce local induced-flow variations due to tip-vortex effects and is discussed in Reference 16. The following approximations are used:

$$\mathbf{k} = \begin{cases} 11.25\mu, & \mu \le .1067 \\ 1.36 - 1.5\mu, & .1067 < \mu \le .5733 \\ .5 & , & .5733 < \mu \end{cases}$$

$$k' = 10 \sin[6(\psi - 45^{\circ})] \sqrt{-\frac{1}{2} |\vec{v}_{S}|^{2} + \frac{1}{2} \sqrt{|\vec{v}_{S}|^{4} + 4v_{i}^{2}}}$$

for $\frac{\mathbf{r}}{\mathbf{R}} \ge .8$ and $45^{\circ} \le \psi < 165^{\circ}$ or $225^{\circ} \le \psi < 315^{\circ}$

Outside these limits k' = 0.

Preparation for analyzing Rotor 2 is essentially the same as for Rotor 1. If Rotor 2 is a tail rotor, the side-wash effect is brought in as a modifier on the V-component (body reference) of the hub velocity.

$$\vec{v}_{S_2} \cdot \vec{j}_B = \vec{v}_c \cdot \vec{j}_B (1 - TRSWC) + [\vec{j}_B \vec{\omega} \hat{\rho}_{S_2}]$$

where TRSWC is input data to account for the sidewash effect on the tail rotor. Also, the swashplate plane is rotated 90° about the $x_{\rm B}$ -axis.

If Rotor 2 is the rear rotor in a tandem configuration, the air may be disturbed. The equations used are

$$x = \tan^{-1} \left[\left(| \overline{v_{S_2}} | \sin \alpha_{c_1} - v_{i_1} \right) / | \overline{v_{S_2}} | \cos \alpha_{c_1} \right] 57.3$$

$$\Delta v_{i_2} = v_{i_1} (1.04 - .005 \text{ X} + .000298 \text{ X}^2)$$

If Rotor 2 is the left rotor in a side-by-side configuration, no unusual treatment is used. In all cases Rotor 2 is assumed to rotate counter to Rotor 1, so that various sign shifts must be made.

The program can be used for performance studies, but it should be noted that the airfoil data are approximated by suitable nonlinear functions of angle of attack and Mach

number, as shown in Figure 12. The rotor analysis is quasi-steady-state based on the tip-path plane, rather

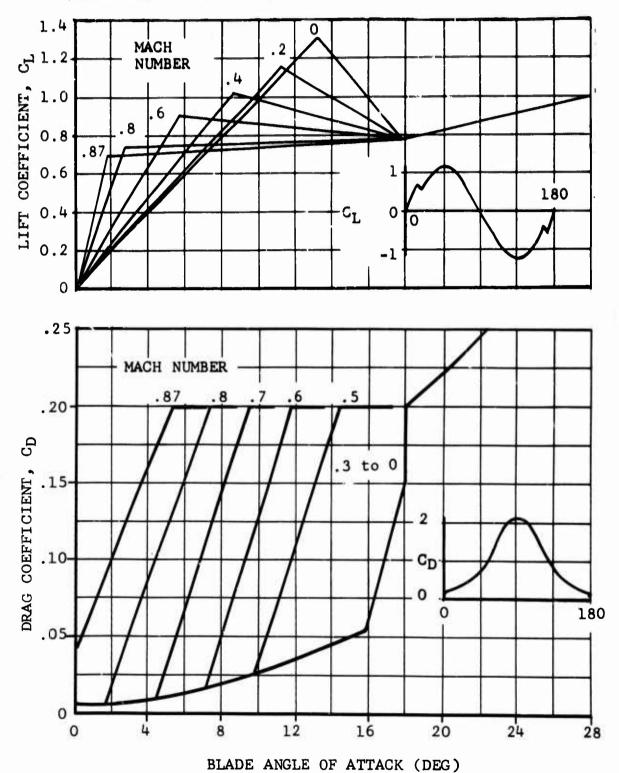


Figure 12. Example of Airfoil Characteristics as Described by Aerodynamic Functions.

than a time-variant step-by-step process for each blade. Harmonic components of aerodynamic-shear distributions through four per rev are computed and supplied to the rotor dynamics analysis section. The rotor aerodynamic analysis sections of the program consume a large portion of the total time required to run a case. When aeroelastic feedback is included, the time used for each pass through the rotor analysis is more than doubled.

A simplified analysis of a propeller for auxiliary propulsion was developed for a special design concept and remains in the program. One propeller can be selected and located at the center of the rotorcraft, or two propellers can be placed a specified distance on either side of the center. Either thrust or collective pitch can be required. Provision is made for nonlinear twist and for tapered planform. This feature is separate from the converted rotor option. Auxiliary jet-thrust simulation is included as specified forces acting through certain points and directed forward at a given angle to the centerline of the aircraft.

Rotor Blade Bending-Moment Analysis

The rotor blade bending-moment program is a tabular method similar to the Myklestad procedure (20). The analysis is based on the assumption that the displacement, slope, shear, and moment at any point on a beam are linear functions of the corresponding four root or base values of these state variables. It is further assumed that the forcing functions and state variables can be treated as consisting of uncoupled harmonic components based on rotor rpm. This assumption allows the single-blade representation, because the conditions at the hub depend on the harmonic component as well as the hub type and number of blades. A set of eight linear equations can then be written for a particular harmonic. These relate the state variables at a point on the beam with index j to the state variables at the root. Formally, for the ith variable at the jth point on the beam,

$$x_{i,j} = B_{i,jo} + \sum_{R=1}^{8} B_{i,jR} x_{o_R}, i = 1, 8$$
 (9)

Recursive expressions for determining the coefficients appearing in the above equations are applied to a segmented representation of the rotor blade. These coefficients are functions of the dynamic parameters of the beam and of the harmonic components.

At least four of the eight root boundary values are known for the given harmonic, hub type, and number of blades.

Since the tip shears and moments are zero, the equations for these four quantities are solved for the remaining four unknown root conditions. For example, consider a two-bladed, semirigid rotor, first harmonic component. The known root conditions are:

- out-of-plane deflection and moment equal to zero
- in-plane deflection and slope equal to zero.

Then the four equations to solve are

$$S_{B_{Tip}} = B_{3_{Tip,0}} + B_{3_{Tip,2}} + \Phi_{0} + B_{3_{Tip,3}} + B_{0} + B_{3_{Tip,4}} + \Phi_{0} + B_{3_{Tip,4}} + \Phi_{0} + B_{3_{Tip,4}} + \Phi_{0} + B_{4_{Tip,3}} + B_{0} + B_{4_{Tip,4}} + \Phi_{0} + B_{4_{Tip,3}} + B_{0} + B_{4_{Tip,4}} + \Phi_{0} + \Phi_{0} + B_{4_{Tip,4}} + \Phi_{0} + \Phi_{0}$$

These equations are solved for the out-of-plane root slope, ϕ_0 , and shear, S_{B_0} , and in-plane root shear, S_{C_0} , and moment, M_{C_0} . Since all quantities in the state equations are now determined, the displacement, etc., along the beam can be computed from the equations (9) for each harmonic. Net values over the rotor disc are obtained by superposition.

Equations showing the effects of the centrifugal force field and the blade-pitch angle, including linear twist, are detailed in Reference 15. The pitch-change values are based on torsional moments arising from aerodynamic pitching moments on the blade segment, and the cross product, F x d, where F is the aerodynamic force vector and d is the deflection of a segment. These moments are assumed to act against a control linkage represented by a spring, while the blade is assumed to be rigid in torsion. The velocities arising

from blade response are computed from the deflection harmonics and are superposed.

The pitch changes and velocities at each of 20 blade segments, and at up to 12 azimuth locations, are used in the subsequent rotor aerodynamic analysis. Since this dynamic consideration is not used in the trim section, a modified trim attitude may be expected. Rather than introduce still another loop in the steady-flight solution program, the dynamic contributions are fed back gradually within the time-variant section.

Certain limitations are inherent in the representations. The number of blades, type of hub, and harmonic component under consideration combine to determine the root conditions. Hence, each contingency must be accounted for in the program. At present, the program can handle steady through fourth-harmonic components for the following rotor types:

- articulated
- semirigid
- semirigid with hub restraint
- rigid

Each of these rotor types can have two, three, or four blades. In practical applications, the two-bladed rotor is not combined with a rigid hub.

The feedback feature of the program can be suppressed if it is not needed for a particular job. The rotor's dynamic response can be computed at specified times without feedback if desired. If either of the provisions for computing rotor oscillatory loads is to be used, the rotor must be designed dynamically to avoid resonances, since the dynamic response is calculated on an undamped basis.

Wings, Control Surfaces, and Fuselage

Wing forces are derived from wing-geometry parameters, and flight-path and ship-motion vectors. A left wing and a right wing are represented because the angle of attack is not necessarily the same on both sides. Finite aspect ratio is taken into account (21), and realistic lift-and-drag-coefficient functions include stall and Mach number effects (22). Ailerons are simulated by allowing variation of wing incidence with stick motions.

The horizontal stabilizer-elevator and fin-rudder are simulated similarly to the wing-aileron. The fuselage has angle-of-attack-dependent lift, drag, and pitching-moment characteristics, and yaw-dependent side-force, drag, and yawing-moment characteristics.

Special Aerodynamic Considerations

Allowances in the program for unusual airflow are made in several ways. As has already been indicated, induced velocity on the rotors, including first-order effects of nonuniform inflow due to the wake-vortex system, is taken into account. Furthermore, some part of the main-rotor induced velocity is felt by the wing in the case of composite craft. The elevator is affected by rotor downwash and wing wake, and the fin is affected by the tail-rotor induced velocity. The airstream may be bent by the fuselage so that the fin's angle of attack is influenced (sidewash effect). In tandem-rotor configurations, the aft rotor may be flying into a flow that has been disturbed by the forward rotor. These variations have been simulated in the aerodynamic equations.

Nonsteady aerodynamic considerations have also been included in the program (23). They are discussed on page 41.

The aerodynamic representation includes the capability for gradual penetration of a gust. The change in rotor thrust, resulting from local angle-of-attack changes due to the presence of gust velocities over a segment of the rotor disc, is constrained to a gradual variation. The whole rotorcraft gradually enters the gust. Hence at a given time, a gust velocity dependent on the gust shape and the component location applies at all points on the aircraft in a plane normal to the flight path; wing and elevator also penetrate the gust gradually. The lift-buildup functions appear to give good results. When more concise theoretical developments are available, new functions can replace the present ones without difficulty.

Engine-Governor-Torsional System

The drive system includes the engine, two rotors, propellers if any, and two types of governors. An engine-governor simulation matches the total torque required to the engine output in normal operation. Power recovery after a full or partial throttle chop is simulated by a parabolic function that includes engine lag time. Power available is increased to its maximum, held until required rpm is attained, then set as for normal operation. A change in rpm results if torque required exceeds the range from zero to maximum available. In addition, a prop-rotor collective-pitch governor (PCG) controls rpm by changing rotor collective pitch during changes in throttle setting (effectively, horsepower supplied). This servomechanism is represented as having a dead band to reduce hunting, and an acceleration capability to a maximum pitch-change rate. This allows a throttle variation (represented by horsepower-supplied change rate) while maintaining, within limits, a specified rpm. Variations in main-rotor rpm and torque required produce reactions in body-motion degrees of freedom as well as in the rotor's performance.

Control System

The control system, as represented, consists of pilot-control capabilities and servomechanisms. The pilot controls are collective and cyclic sticks, pedals, throttle, mast-tilt actuator, rpm selector, and engine-governor selector. These controls are linked to the swashplate, control surfaces, and other affected mechanisms, and the displacement ratios are specified (where appropriate) by input data. In the trim section, the stick and pedal positions are the primary values to be found. In the maneuver section, each of these controls can be moved at specified rates (or switched on) during selected time intervals.

Several automatic mechanisms that affect the controls are represented. Pitch stabilizing is induced by a transfer function sensitive to pitch displacement from trim, pitch velocity and acceleration. This function produces changes in cyclic and collective pitch, subject to a lag factor. Yaw stability is handled similarly.

RPM is maintained either by a standard governor which varies the power supplied, or by the PCG which varies rotor collective pitch. These mechanisms are more fully described above in the Engine-Governor-Torsional System. If one or two propellers are used for auxiliary propulsion, an automatic control that varies the propeller's collective pitch with forward speed is available. Provision is made for a pilot-input override.

A flat-tracker mechanism may be activated to hold the trim values of either rotor-to-mast flap angles or specified flap angles within a stated tolerance by varying cyclic pitch. Collective-pitch-bobweight coupling can be switched on or off at data-specified times. Pitch-flap and pitch-cone coupling are controlled by configuration parameters. They are not subject to change during maneuvers.

Solution Procedures for Trim and Maneuvers

For a given description of the rotorcraft and its steady-state flight conditions, the trim parameters listed earlier must be found from the set of algebraic equations obtained by equating the first ll equations in Table V, page 30, to zero. By assuming that the required horsepower is available, the drive-system rotation equation can be omitted, since rpm is input. With 10 equations and ll unknowns, a value may be assigned to one of the unknowns. In the current version of the program, the fuselage yaw angle is assigned. There remains a set of 10 nonlinear algebraic equations in 10 unknowns.

It is impractical to attempt to write these equations in explicit form since, among other complications, the entire rotor analysis is involved. However, an iterative procedure which depends on the evaluation of functions can be employed

for solution. The procedure begins with the substitution of an initial-approximation vector, Zo, in the force and moment sum functions and computation of their values. If $\mathbf{Z}_{\mathbf{O}}$ is the exact solution, all the functions will be zero and the equations are satisfied. Otherwise, the function values are a vector, E, and $\mathbf{Z}_{\mathbf{O}}$ must be changed so that the magnitudes of the components of E are reduced. The total differential of a function is the sum of the products of the partial derivative of the function with respect to each independent variable, and the differential of that variable. The set of net changes desired in the functions is -E, the negative of the error vector. Let Δ be the vector representing the set of independent-variable differentials, and M the matrix of function partial derivatives. It now appears that M \cdot Δ = -E represents a set of linear equations, that values of Δ can be computed, and that Z_{0} + Δ will be the correct-answer vector. This is not altogether true, however, because the partial derivatives are not constant, but are evaluated numerically about the point specified by $\mathbf{Z}_{\mathbf{O}}$. It may be possible, though, to converge to good results by replacing Z_0 with a new approximation, Z_0 + Δ , and substituting again in the functions. Let \overline{E} be the vector whose components have the magnitudes of the elements of E, and A, an allowable-error If $\overline{\mathbb{E}}$ -A has no positive components, the solution is satisfactory. If not, the elements of M are reevaluated and the process is repeated. After satisfactory results are obtained, stick and pedal positions are checked against stop and range data, and required horsepower is checked against available horsepower. If all of the conditions are met, the program proceeds to the maneuver section. The numerical solution method described above is suggested in many texts. If we consider a function of many variables expanded in a Taylor's series in the neighborhood of a point, the equations in the first-order partial derivatives, as used in the program, result when all higher-order terms of the series are ignored. However, since many of the equations are strongly nonlinear (especially in the case of high advance ratios), considerable difficulty may be experienced in applying this technique. This is a problem that is often encountered in the numerical analysis of large nonlinear systems (24).

Considerable effort has been expended in the course of this study in searching for improvements to the method used for calculating trim solutions. Inclusion of second-order partial derivatives has been tried, but without marked improvement in capability. Work is continuing in two directions to expedite solutions: (1) limited analyses (i.e., linear theory) using empirical data to provide better initial approximations; and (2) more precise mathematical analysis.

Stability derivatives about the trim point are computed numerically using the same program technique as for the other partial derivatives. The calculation of these velocity-based rates can be selected if required by the user of the program.

Maneuvers are activated by input data which result in timedependent changes in control positions or aerodynamic environment. Certain automatic-control devices can also be turned on or off at specific times. Response to these changes is derived from stepwise solution of the differential equations, with the trim values being used as initial conditions. Thus the stability and control characteristics of the configuration can be ascertained. Almost any maneuver that a given type of rotorcraft is capable of executing may be simulated.

A Runge-Kutta procedure (25) is used to solve the differential equations. The process is characterized as four-pass, non-iterative, and noncorrective. It is noncorrective because the initial values for the second time step are the final values computed in the first time step, and no further influence due to previous values is included. Computer time becomes a problem in this section because each cycle involves complete analysis of two rotors. Predictor-corrector methods of solution (26,27) are being considered as a means for improving this part of the program.

The process is somewhat complicated by the transformations of the reference axes that are involved. The first group of equations, in fuselage-reference accelerations, is integrated to yield fuselage-reference velocities. The instantaneous angular velocities are transformed to Euler-angle velocities, which are used to compute new Euler angles. The instantaneous linear velocities are transformed to fixed-reference, and these quantities are used to compute linear displacement. The rotor equations are handled similarly. Two objectives are realized:

Equations are retained in straightforward, simple form, including constant mass moments of inertia; and

Fuselage-reference velocities, which are needed for stability and control studies, are computed as a necessary part of the procedure.

Input and Output

The input data required for this computer program are fully discussed by Blankenship and Bird (9). An effort was made to keep the number of inputs to a minimum, and to express them in conventional units. The parameters are organized into logical categories in the input format. In addition to quantifying data, identification and program control data are included.

The computer data output is fully annotated and, except for conditional output, is self-explanatory. When undesirable or unusual numerical situations occur in the computing process, output messages stating the nature of the problem are provided. In addition to digital information, plots of most of the

variables can be obtained automatically, controlled by the data specifying the variable and the range.

A program capability for retaining maneuver data on tape for retrieval and plotting when required is also available. Subsidiary programs may be used to set up a permanent library of case results. The principal input and output features are illustrated in Figure 9.

WING NONSTEADY AERODYNAMICS

Nonsteady aerodynamics for a fixed wing are treated by the methods developed by Küssner and Wagner (28,29). The Wagner function represents the lift buildup due to a sudden change in angle of attack, and is given by the equation

$$\Phi(s) = C_0 + C_1 e^{r_1 s} + C_2 e^{r_2 s}$$
 (11)

where s is the distance traveled in semichords, and C_0 , C_1 , C_2 , r_1 , and r_2 are constants which must be selected to reflect the wing aspect ratio. Following a sudden change in angle of attack, a "starting" vortex is generated that partially suppresses the sudden increase in wing lift. The "starting" vortex remains stationary in space, thereby losing its influence on the moving wing. Depending upon wing aspect ratio, the initial lift increment for the Wagner function is approximately one-half of the final lift increment, as shown in Figure 13.

The Küssner function represents the lift buildup for a wing gradually penetrating a gust, where the lift builds up from zero (no initial increment). For the general case of a shaped gust profile, the wing simultaneously experiences a change in gust velocity and a change in angle of attack due to aircraft pitch response. It is necessary, therefore, to combine the Wagner and Küssner functions into a single analytical expression. An approximation of the Küssner function is obtained by multiplying the Wagner function by the average gust velocity at four points along the wing chord (leading edge, 0.25c, 0.50c, and 0.75c). For a sharp-edged gust, the approximation results in a series of steps as the control points successively enter the gust. Figure 13 also shows the Küssner function and the approximation used for this study.

ROTOR NONSTEADY AERODYNAMICS

For a rotor, Drees and Lucassen (8,13) report that a noticeable reduction of the lift increase due to a sudden gust is to be expected if nonsteady aerodynamics are considered. Since Drees and Lucassen assumed the rotor to act as a fixed circular wing,

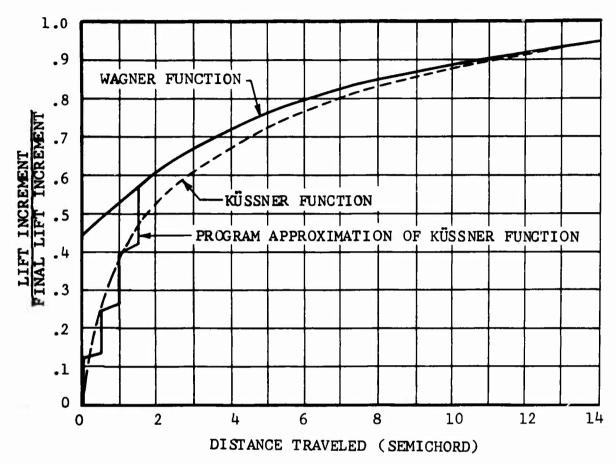


Figure 13. Wagner Function, Küssner Function, and Approximation of Küssner Function.

their results show only the qualitative influence of nonsteady aerodynamics on the gust response of a rotor.

Recent analytical methods (14,30,31), which use detailed representations of the free vortices shed from the rotor blades, produce the lift functions needed for this study. Limitations on storage and computing time, however, precluded the use of such methods in the present analysis. Following the concepts used by Wagner and Küssner in the fixed wing analyses, a more suitable solution was developed during the course of this study by Buettiker and Weber (32,23). The two major components of the rotor wake are considered separately:

1. The far wake consists of the helical pattern of vortices that is shed from the rotor tips after a change in rotor lift.

2. The near wake consists of vortices that are shed along the trailing edge of a blade due to changes in the local blade angle of attack.

Consider, briefly, a rotor with an infinite number of blades but with the usual values of solidity and rotational speed. Each local airfoil section travels a distance of many chord lengths in a negligible amount of time because the chord length is nominally zero. Therefore, there is no delay in the lift buildup on the local airfoil due to local changes in gust velocity or angle of attack. Furthermore, the local effects of vortices shed from the trailing edge of preceding adjacent blades are cancelled by the effects of vortices shed from the trailing edges of following adjacent blades. The tip vortices (far wake) remain as the only contributor to non-steady aerodynamic effects for a rotor with an infinite number of blades.

For a finite number of blades, the far wake effects are unchanged. An additional consideration is that a finite time is required for the lift to change at a local airfoil section. The delay in lift buildup is comparable to the fixed-wind non-steady aerodynamic effect, except that the distances traveled must be expressed in terms of rotor diameters instead of wing semichords. The near-wake effect (reflecting a finite number of blades with finite chord length) is superposed with the far-wake effect to represent nonsteady aerodynamics for a rotor.

Far Wake Effect

Buettiker's analysis assumes that, due to appropriate control inputs, a sudden change in rotor lift is distributed uniformly over the rotor disc and that the rotor does not flap. induced flow is calculated versus time at four sampling points on the disc (0.75R, 4 azimuth positions). Typical results are shown in Figure 14. Note that the maximum local induced velocity is reached first at the forward part of the rotor (180° azimuth position) and somewhat later for the aft part of the rotor (0° azimuth position). These calculations include only the net circulation of the wake increment as it develops. The average induced velocity gradually increases and reaches its final value shortly after the new tip-vortex sheet from the forward part of the rotor passes beneath the aft part of the rotor. A flow pattern then is established with the highest induced velocity near the aft section of the rotor. Since the change in the induced velocity is zero at the time of the sudden lift change, the subsequent wake development results in a decay of the initial lift increment to a smaller steady-state value. The solid line of Figure 15 presents an example of the far-wake lift function as calculated for a rotor with a solidity of 0.07 at an advance ratio of 0.5. Note that the initial lift is about 8 percent higher than the final lift.

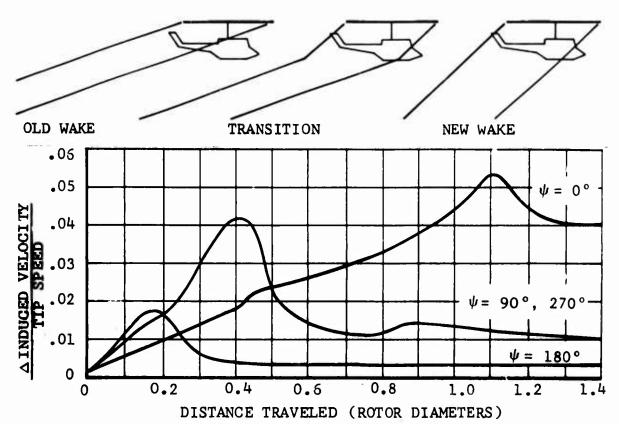


Figure 14. Induced Velocity at 0.75R after a Sudden Lift Change.

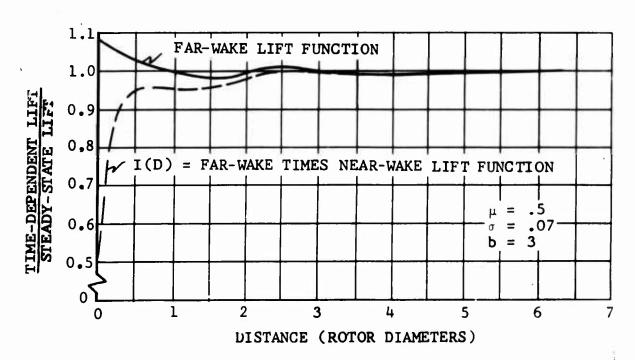


Figure 15. Lift Buildup Due to Wake.

Near-Wake Effect

The lift on a rotor with a small number of blades cannot build up instantaneously. By analogy with fixed-wing theory, vortices are shed along the trailing edge of the rotor blade as the lift changes, causing a time-variant induced flow that reduces the lift increment on the local airfoil section. This phenomenon is identical to the fixed-wing effect that is represented by the Wagner function. In the analysis, the far-wake effect and the near-wake effect are superposed by multiplying the far-wake lift function by the Wagner function.

Far-wake lift functions were calculated for 25 combinations of solidity and advance ratio for both a 3-bladed rotor and a 36-bladed rotor (to approximate an infinite number of blades). Solidity was varied from 0.05 to 0.09 in steps of 0.01; advance ratio was varied from 0.1 to 0.5 in steps of 0.1. A large change in either solidity or advance ratio shows no appreciable effect on the total nonsteady-aerodynamic lift function for a rotor (23). For each set of 25 parameter combinations, an average lift function was established that should be valid for the entire range of solidities and advance ratios that were used in the computer case studies. The lift function for a 36-bladed rotor exceeds 0.9 after the rotor travels about 0.15 diameter; the lift function for a 3-bladed rotor exceeds 0.9 after the rotor travels 0.32 diameter. The lift function for the combined far-wake and near-wake effects is synthesized by a sixth-order polynominal:

$$I(D) = +0.5 + C_1D + C_2D^2 + C_3D^3 + C_4D^4 + C_5D^5 + C_6D^6$$

where D is the distance, in rotor diameters, traveled after the disturbance. The resulting lift function (shown by the dotted line of Figure 15) has an initial lift change that is equal to one-half of the final lift change, and reaches 90 percent of the final value within a distance traveled of about 0.25 diameter. Note that this analysis is not valid for hovering or low forward speeds.

In relation to the lift function for a 3-bladed rotor, the synthesized function yields conservative results for thrust increase and slightly understates the relative importance of rotor nonsteady aerodynamics, but the evaluation of the computer case results showed that this effect was among the least significant of those studied. Although considerations of stall, compressibility, and reverse flow were excluded by the selection of sampling points (at 0.75R and 4 equally-spaced azimuth positions) for the above development, valid first-order quantitative effects should be obtained for rotors with any finite number of blades:

Immediately after an angle-of-attack change, there is a greater induced velocity than during the steady state, and the vortices move very slowly away from the rotor plane. A lift overshoot should be expected. References 33 and 34 tend to confirm this expectation. Measurements reported in Reference 14, however, show little overshoot of the average lift. Figure 16 shows a comparison of the lift function used in this study with results from Reference 14. (Note that Reference 14 includes a gradual pitch increase which tends to reduce the initial slope of the lift curve.)

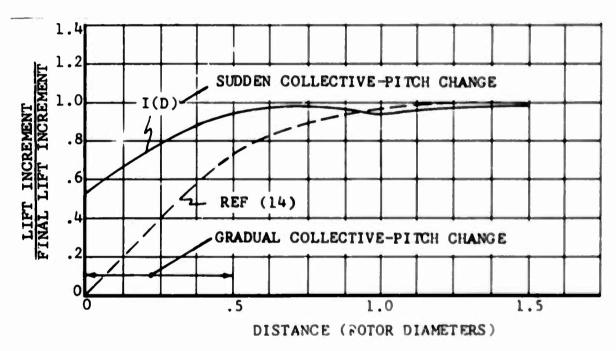


Figure 16. Correlation of Lift Buildup.

The method for evaluating the time-dependent lift buildup uses the Duhamel Integral (35), in which the lift functions $\phi(s)$ for the wing and I(D) for the rotor assume the roles of the indicial admittances of the systems. Since the maneuver program computes the steady-state wing lift and rotor thrust due to a gust or angle-of-attack change, the lift and thrust are used as inputs for the time-dependent lift computation. This procedure has the advantage that the nonsteady lift functions for both the rotor and the wing are treated in the same manner by a simple mathematical procedure. The storage requirements in the computer are minimized, and the time required is acceptable: a maximum of 50 seconds is required for 100 time steps, using the lift function I(D). The computation of this information from the wake itself would take more than 15 minutes.

In retrospect, it is believed that a more desirable approach might be to keep the far-wake and near-wake effects separate (see Figure 15), to relate the near-wake effects to the lift functions of each local blade element, and to relate the far-wake effect to the rotor thrust. The advantage would result from effectively including the nonsteady lift functions in the calculation of steady-state flight conditions. The computational involvements would be far less than with a full-wake representation. This approach is suggested as a future modification of the program.

GUST MODEL

The mathematical representation of gust velocities, horizontal or vertical, is accomplished with time-variant air-velocity functions. These gust-shape functions are represented in the maneuver section as follows:

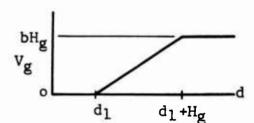
Sharp-edged

$$v_{g} = \begin{cases} 0, & d < d_{1} \\ c, & d \ge d_{1} \end{cases}$$

v_g o d₁

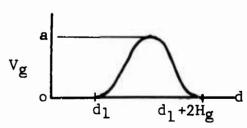
Ramp

$$v_{g} = \begin{cases} 0, & d < d_{1} \\ b(d-d_{1}), & d_{1} \le d < d_{1} + H_{g} \\ bH_{g}, & d \ge d_{1} + H_{g} \end{cases}$$



Sine-squared

$$V_{g} = \begin{cases} 0, & d < d_{1} \\ a & \sin^{2} \pi \left(\frac{d-d_{1}}{2H_{g}}\right), & d_{1} \leq d < d_{1} + 2H_{g} \\ 0, & d \geq d_{1} + 2H_{g} \end{cases}$$



where d = distance from the origin to the point considered

 d_1 = distance from the origin to the gust

Hg = ramp length or distance over which the gust velocity increases

a,b,c = constants controlling the gust amplitudes

The duration and maximum velocity reached, as well as the shape, are determined by input data.

The introduction of the gradual penetration into the program involves careful "bookkeeping" to establish the exact gust velocity on each part of the aircraft at any given time. The locations of rotor hubs, wing, elevator, and fin are already inputs to the program for calculating force and moment balance. The output format includes a presentation of the instantaneousgust velocities over the rotor disc. Figure 17 shows examples of such an output for a sine-squared gust with a ramp length of 90 feet on a helicopter traveling at a speed of 200 knots.

The important question - which gust model to use - is discussed at some length in Reference 8. In that study, the sine-squared gust shape is introduced in parallel with the techniques developed for fixed-wing aircraft (11, 36). The problem is that the ramp length of the gust for fixed-wing aircraft is expressed in terms of the chord length (ramp length = 12.5 chords). Obviously, this measure cannot be used for a rotor. It is therefore concluded in Reference 8 that the gust function must be related to the circumstances actually found in the atmosphere (which are, of course, independent of the chord length of a particular aircraft).

References 10 and 37 present information on gust envelopes, determined indirectly by flying fixed-wing airplanes through gusts. Using the analyses developed for fixed-wing airplanes, a region determined by the maximum gust velocity and ramp length was found to contain almost all the test data. Figure 18 shows that the gust velocity (Vg) in this envelope reaches a maximum of about 50 feet per second at a ramp length (Hg) of 90 feet. Although a roof-top gust model was used, very little change is expected when a sine-squared gust shape is substituted, as is shown later (page 57).

Figure 18 indicates that very high gust velocities will not be present in the atmosphere without a considerable ramp length. Understandably, then, high-velocity gusts will build up more gradually than sharp-edged gusts, and the gust loads will be relatively lower.

The sine-squared gust shape was chosen as the most realistic model for this study. A later section of this report shows the establishment of critical values for the gust velocity (V_g) and ramp length (H_g) to produce the maximum load factor. The sine-squared gust is invariably used in conjunction with the gradual penetration and the nonsteady aerodynamic lift functions. The result is compared with the sudden gust case, in which the entire aircraft is instantaneously submerged in the gust with a velocity (V_g) , without the benefits of gradual penetration and nonsteady aerodynamic effects.

For horizontal gusts, which are assumed to hit the aircraft from the front or the side, similar assumptions are made.

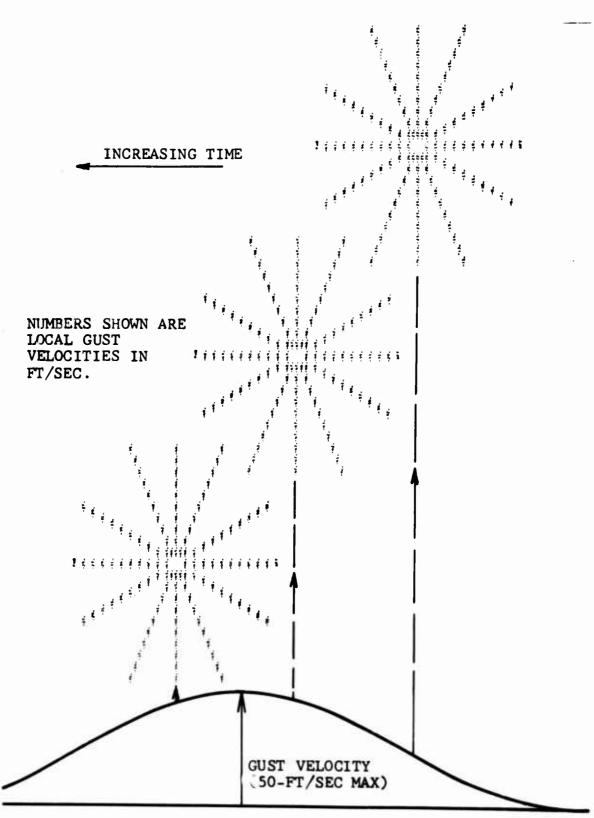


Figure 17. Gradual Gust Penetration (Automatic Computer Output).

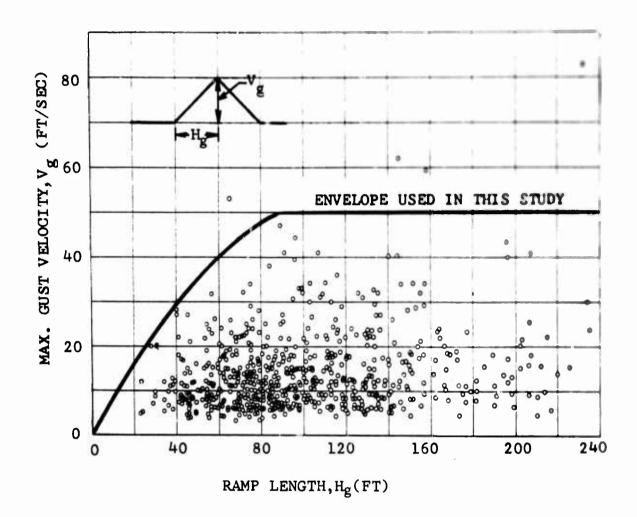


Figure 18. Envelope of Gust Based on Flight Tests With Fixed-Wing Aircraft.

STOPPED- AND TRAILED-ROTOR ANALYSIS

The response analysis for the stopped rotor and for the trailed rotor encountering a gust is presented in detail by Weber (17). Two gusts were used: a sine-squared gust with a 90-foot ramp length and a sudden gust, both with 50 feet per second maximum velocity.

Schematics of the stopped rotor and the trailed rotor are shown in Figures 19 and 20, respectively. The stopped rotor has two flexible blades cantilevered on a flexible mast. The mast is cantilevered at its base. The trailed rotor is shown in cruise condition with its three blades folded aft from the ring tip.

A computer program with provision for thirty-six degrees of freedom was written specifically for this analysis. The

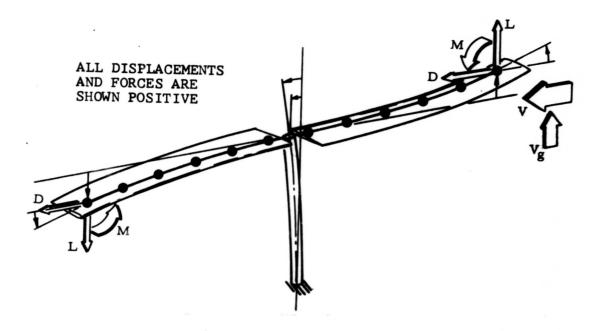


Figure 19. Schematic of Stopped Rotor.

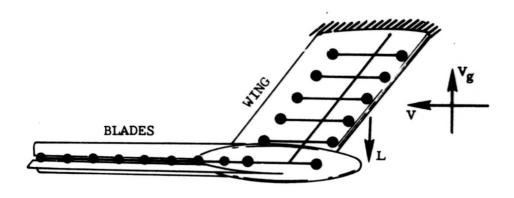


Figure 20. Trailed-Rotor Dynamic Representation and Sign Convention, Perspective View.

program forms the dynamic and aerodynamic matrices from the input data (17). The time-dependent solution to the equations is found by use of the Runge-Kutta technique. The basic equation for both cases is

$$[m]{\ddot{x}} + [c]{\dot{x}} + [k]{x} = [F_1]{\ddot{x}} + [F_2]{\dot{x}} + [F_3]{x}$$
(12)

The damping matrix [c] is considered to be diagonal, and the aerodynamic mass matrix [F1] is considered to be a second-order effect and consequently is neglected. The general equation can now be written:

$$[m]{\ddot{x}} + [c]{\dot{x}} + [k] {x} = [F_2]{\dot{x}} + [F_3]{x}$$
 (13)

Because of the problem of generated input data, two methods of problem setup are used. The dynamics of the stopped rotor are set up so that the two blades and the mast are treated as three cantilevered systems. This allows easy generation of the stiffness matrices for each section. The boundary conditions are then applied, and the structure is assembled as a rigid rotor with a flexible mast; thus the coordinate system is such that all coupling terms between segments are included in the mass and aerodynamic matrices and are excluded from the stiffness matrix. For this problem, six mast segments and twelve blade segments (six per blade) are used with two degrees of freedom (displacement and slope) per segment. See Figure 19.

The dynamics portion of the trailed-rotor analysis uses a generalized coordinate system with the coupling between degrees of freedom being represented in the full stiffness matrix. The wing is represented by a series of masses arranged as "dumbbells" along the wing's elastic axis and parallel to the airflow (see Figure 20), with two control points per segment. The control points for the rotor blade are on the elastic axis. Only displacements of the control points are considered, with wing torsion represented as differential displacement of the control points. This method necessitates a mass matrix with coupling between bending and torsion for each segment but with no coupling between segments.

The aerodynamics are expressed as functions of displacements and displacement velocities. For the stopped rotor, the lift generated by blade flapping is the exciting force for the blades. The $dC_L/d\alpha$ for the first forward-blade segment is assumed to be 2π , while all other segments have a $dC_L/d\alpha$ of $2\pi/10$. This distribution approximates the lift distribution on a very low-aspect-ratio wing. The hub moment and the drag produced by this lift are used to excite the mast. Drag of the mast is neglected. The trailed-rotor analysis uses steady-state aerodynamics with a constant lift-curve slope. A lift-

curve slope of 2π is used for the wing, and $2\pi/10$ is used for the trailing-blade portion of the system.

FLAPPING STABILITY AT HIGH ADVANCE RATIO

Although this study pertains primarily to gust effects on loads and load factors, it is known that rotor-flapping stability may also be affected by gust inputs. Drees and McGuigan (8) discuss the flapping instability for an unloaded rotor. Jenkins (22) points out that the azimuth of the blade at which the disturbance is applied is of importance. While a detailed investigation of this matter falls outside the scope of this study, a general discussion of the problem is in order.

A 3/4R analysis and rigid-body free flapping are assumed. In the resulting equation of motion,

$$F_{o}(\psi) = \beta'' + h_{o}(\psi)\beta' + g_{o}(\psi)\beta$$
 (14)

where

$$\begin{split} &h_{o}(\psi) = \frac{9}{32} \gamma \left| \frac{3}{4} + \mu \sin \psi \right| \\ &g_{o}(\psi) = 1 + \frac{3}{8} \gamma \left| \frac{3}{4} + \mu \sin \psi \right| \left[\mu \cos \psi + \tan \delta_{3} \left(\frac{3}{4} + \mu \sin \psi \right) \right] \\ &F_{o}(\psi) = \frac{3}{8} \gamma (\theta + \phi) \left| \frac{3}{4} + \mu \sin \psi \right| \left(\frac{3}{4} + \mu \sin \psi \right) \end{split}$$

 $\boldsymbol{F}_{0}(\boldsymbol{\psi}),\;\boldsymbol{h}_{0}(\boldsymbol{\psi}),\;\text{and}\;\boldsymbol{g}_{0}(\boldsymbol{\psi})$ include all the aerodynamic effects.

The absolute value of the relative velocity at the 3/4-radius blade element is used in order to correctly account for the reversed-flow area. The damping coefficient, $h_0(\psi)$, is zero or positive for all values of ψ , but the spring rate, $g_0(\psi)$, can become negative.

Figure 21 shows variation of the damping coefficient with blade azimuth position for a Lock number (γ) of 2 and for values of μ from 0 to 3. The figure also shows variation of the spring rate with μ for $\gamma=2$, $\mu=2$, and two values of δ_3 , 0 and 30 degrees. The damping coefficient goes to zero at azimuth values in the neighborhood of $\psi=200$ degrees and $\psi=340$ degrees. A negative spring rate appears first in the region between $\psi=100$ degrees and $\psi=180$ degrees. A second region of negative spring rate may appear at very high advance ratios (for $\mu\gg1$) near $\psi=240$ degrees. The mechanism causing this negative spring rate can be understood by considering the blade in a forward-swept condition ($\psi=135$ degrees). In a flapped-up condition, an aerodynamic up-force will appear,

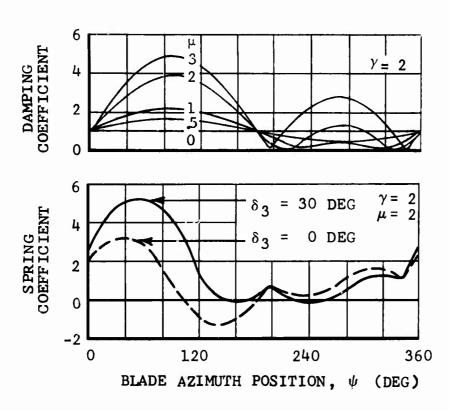


Figure 21. Blade-Flapping Stability Coefficients.

causing static divergence when it overcomes the restoring effect that centrifugal force imposes on flapping.

In Reference 22 it is shown that an initial disturbance at ψ = 90 degrees is more severe than one at ψ = 0 degrees. This is an understandable effect, as the disturbance initiated at zero degrees will be partially damped while the blade traverses the azimuth from zero to 90 degrees, before it enters the instability region between 100 and 180 degrees.

The simplified study has been expanded during the course of the contract to include investigation of the effects of gust velocity and rotor loading. The objective is to determine under what condition a 10-degree angle of attack will be reached by the blade element at 3/4 radius because of the combined effects of gust, rotor lift, and blade-flapping divergence in the region from ψ = 100 to 180 degrees. Simplifications are made by using average values for the functions $h_0(\psi)$ and $g_0(\psi)$. It is assumed that a sharp-edged gust is imposed on the blade just before it enters the region of unstable flapping spring rate $g_0(\psi)$. Figure 22 shows the result. Assuming that at 3/4 radius an angle of attack greater than 10 degrees would give rise to blade stall and high loads, high gust velocities (and the consequent increased blade loads) can be seen to decrease the

safe operating speed of the aircraft. Hence, high blade inertia (low Lock number, γ) is an advantageous feature.

This treatment of flapping stability is not sufficiently complete to predict the behavior of a specific rotor configuration. It should be expanded to include rigid and semirigid rotors, blade-bending flexibility, torsional degrees of freedom, hub restraint, etc. Nevertheless, it is believed that the general trends and first-order effects are valid. For the high-speed compound helicopter and stopped-rotor configurations in particular, flapping stability must be taken into account.

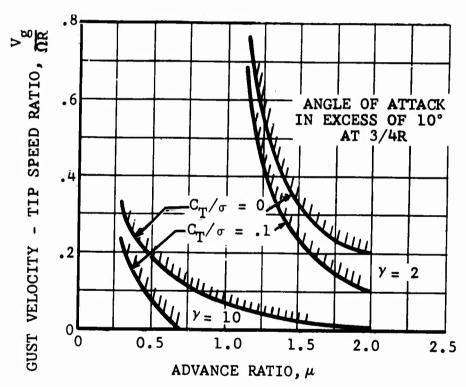


Figure 22. Gust Effect on Blade Flapping.

DISCUSSION OF RESULTS

GENERAL DISCUSSION

The cases investigated for this study are listed by categories in Table I (page 16) and summarized in more detail in Appendix II. Each individual sine-squared gust case resulted in a 385-page output of information concerning performance, stability and control characteristics, time history of the maneuver, and steady and oscillatory rotor loads. The output for sudden-gust cases is 56 pages per case. It was considered one of the objectives of this report to put order to the multitude of information in such a way that trends can be distinguished and conclusions can be drawn. Appendix III gives the principal results for 295 cases. The physical parameters of the rotors used for these cases are presented in Appendix IV. The stability derivatives for 9 cases are presented in Appendix V.

In this section of the report, the effects of the many combinations and variations are discussed after showing a sample output case and details of the parameter selection of aircraft and rotors used in this study.

Sample Case

A sample case is given in Appendix I. Only a selection of the 385 pages of computer output are given. Pages 137 and 138 (in Appendix I) show the input data as arranged in logical groups. Some principal quantities are indicated. The case is for a 8500-lb compound helicopter with a single, 2-bladed, semirigid rotor at 150-knot trim velocity. Aeroelastic feedback and nonsteady wing and rotor aerodynamics are included. Pitch-flap coupling (83) is also included.

One cycle of the trim iteration-loop output is shown next (page 139). Forces and moments are listed and partial derivatives are presented for use in stability and control studies. The number of iterations to trim depends on many factors and can become excessive if the initial control position and values are not close to the final values, especially at high speed. (If no trim is achieved, messages will indicate the source of the problem.)

Next (page 140) are the output details for the trim condition. The forces on fuselage, rotors, wings, elevator, fin, and auxiliary propulsion are listed, as well as control positions, fuselage attitude, and performance information. The stability derivatives are shown on page 141.

At this point, the maneuver section becomes effective. Inputs defining details of the required disturbances or control motions

are listed on page 142. Computation of the maneuver then proceeds step by step.

Information is furnished concerning details of the fuselage and the rotor plane position in space, and the forces and moments applied to the rotorcraft. Output for one time point appears on page 143. Velocities due to blade vibrations, which are used as aeroelastic-feedback information, are listed on page 144. Blade control deflections are on the same page. The gust velocity versus azimuth is charted on page 145. A summary of the steady and oscillatory in-plane and out-of-plane rotor moments for 20 blade stations is given on page 146. All of the information is supplied for each time point. Automatically printed time histories conclude the data presentation (page 147).

Parameter Selection

The selected input parameters for the pure and compound single-rotor, tandem and side-by-side helicopters are listed in Table VI. The stopped-rotor parameters are given in Table XIX, and the trailed-rotor parameters are given in Table XX. The combinations cover the entire range of parameters specified in Table I (page 16) and Appendix II. Figure 23 summarizes the cases in terms of disc loading, blade loading, and configuration.

Mass and stiffness distributions of the rotor had to be selected such that no resonance condition would be encountered. Natural frequencies were computed for all rotors used in the study. Examples of the resulting automatically plotted frequency diagrams are given in Figure 24a, b, and c.

EFFECT OF GUST SHAPE

The effect of a sharp-edged gust versus a sine-squared gust was discussed in connection with Figure 6 (page 11). Other gust shapes are also possible. In Figure 25 a summary is given of response of a typical helicopter to

-	sharp-edged gust	(case 253	3)			
	ramp gust	(case 256	for Ho	=	90	ft)
	rooftop gust	(case 258	i) ⁵			,
-	sine-squared gust	(case 254	1)			

In each of the four cases referred to above, aeroelastic feed-back and gradual penetration were used. (Note that gradual penetration causes the aircraft to respond before the gust reaches the cg, where Δn is the load factor at the aircraft cg). It is seen that the ramp gust creates gust loads comparable to the rooftop and sine-squared gusts. The ramp gust, however, was not selected for use in the detailed analysis

calculations because of the wealth of data available for the rooftop and sine-squared gust shapes. Cases 33, 34, 255, and 256 are ramp-gust cases that have been run to compare with other gust-shape variations. The rooftop and sine-squared gusts give only slightly different maximum gust loads (.81 g for the rooftop gust versus .89 g for the sine-squared gust). For this reason the gust envelope presented in Figure 18, page 50, which pertains to a rooftop shape, is applied to the sine-squared gust shape. Ramp-length and maximum gust-velocity combinations selected from Figure 18 have been applied to the sample case cited on page 56 and presented in Appendix 1. Time histories of gust-load factor are presented in Figure 26.

X PURE SINGLE-ROTOR
O COMPOUND SINGLE-ROTOR
□ TANDEM
△ SIDE BY SIDE

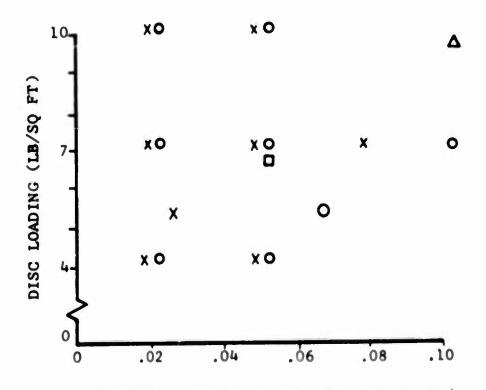


Figure 23. Summary of Case Parameters.

THRUST COEFFICIENT-SOLIDITY RATIO, CT/o

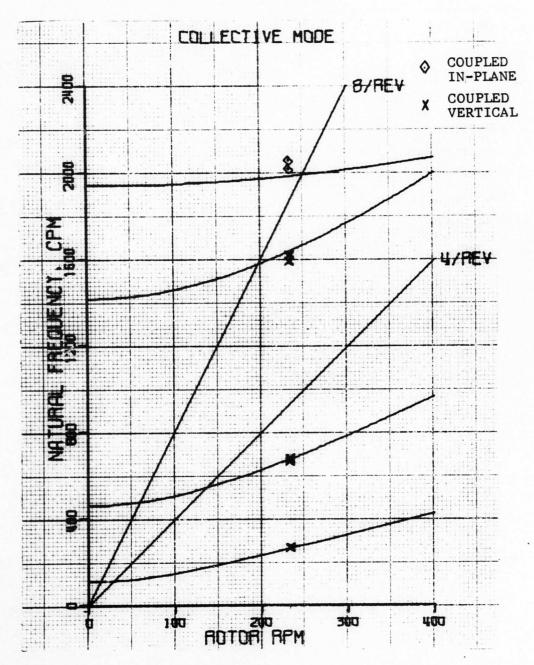
TAB	LE VI.	INPUT I	DATA SELEC	TION	
,	Pure Single Rotor	Com- pound No. 1	Com- pound No. 2	Tandem	Side by Side
FUSELAGE	<u> </u>				
Gross Weight (lb)	15000	15000	8500	15000	23000
Location of Center of Gravity					
Station (in.)	250	250	193.85	320	320
Waterline (in.)	111	111	61.61	111	126
Butt Line (in.)	0	0	0	0	0
Roll Inertia (slug-ft2)	7200	7200	2350	7200	119300
Pitch Inerita (slug-ft ²)	39000	39000	11716	39000	48200
Yaw Inertia (slug-ft ²)	36000	36000	10164	36000	140000
Product of Inertia I _{XZ} (slug-ft2)	3600	3600	-871	3600	o
Effective Drag Area at Zero Pitch (ft ²)	8.5	8.5	4.0	8.5	5.5
PYLON					
Weight (lb)	_	_	-	•••	5000
Location of Center of Gravity at Zero Mast Tilt					31
Station (in.)	-	-	-	-	320
Waterline (in.)	-	-	-	-	200
Drag Coefficient at Zero Tilt (ft2)	_	_	-	_	18.8
WING					
Area (ft ²)	=	225	27.8	-	330.5
Aspect Ratio	-	5	1000	-	7.44
Incidence (deg)	-	7.52	14.0	-	8.0
Collective-Stick Coupling (deg/in)	-	0	0	-	o
Lateral Cyclic-Stick Coupling (deg/in.)	-	.5	0	_	.438

AT	BLE VI.	- Contin	ued		
	Pure Single Rotor	Com- pound No. 1	•	Tandem	Side by Side
WING (Cont'd)					-
Location of Center of Pressure					
Station (in.)	-	250	192	-	310.5
Waterline (in.)	-	111	62		135.0
Butt Line (in.)	-	±100	±39	-	±144.0
Slope of Lift Curve (/deg)	-	.07	.0606	-	.07
Drag Coefficient at Zero Attack	-	.01	.01	-	.01
ROTOR 1					
Function	Main	Main	Main	Forward	Right
Number of Blades	4	4,	2	4	3
Radius, Chord, RPM, etc.	(5	See Appe	ndix II)		
Weight and Stiffness Distributions	(:	See Appe	ndix IV)		
Twist (deg)	-10	-10	-10	-10	-29.06
Precone (deg)	2.5	2.5	2.75	2.5	1.75
Mast Length (ft)	7	7	0	7	6.17
Pitch-Cone Coupling Ratio	0	0	0	0	0
Pitch-Flap Coupling, 83 (deg)	20	20	0	20	20
Location of Shaft Pivot Point					
Station (in.)	250	250	200	40	320
Waterline (in.)	116	116	152.62	135	141
Butt Line (in.)	0	0	0	0	280.5
<pre>Slope of Lift Curve (/deg)</pre>	.100	.100	.107	.100	.100
Drag-Divergence Mach Number	.87	.82	.80	.87	.87

7	TABLE VI	- Contin	nued		
		pound	Com- pound No. 2	Tandem	Side by Side
ROTOR 1 (Cont'd)			- . •		
Coefficients for Nondivergent Drag Equation					
δ ₀	.010	.010	.008	.010	.010
δ ₁ (/deg)	00005	00005	0	00005	00005
δ_2 (/deg ²)	.00018	.00018	.00003	.00018	.00018
Gear Ratio	.01758	.01758	.0491	.01758	.02475
ROTOR 2					
Function	Tail	Tail	Tail	Aft	Left
Number of Blades	4	4	2	4	3
Radius, Chord, RPM, etc.	(See Appe	endix II)		
Weight and Stiffness Distributions		See Appe	endix IV)		
Twist (deg)	0	0	0	-10	-29.06
Precone (deg)	0	0	1.5	2.5	1.75
Mast Length (ft)	2	2	0.0	9	6.17
Pitch-Cone Coupling Ratio	0	0	0	0	o
Pitch-Flap Coupling, 83 (deg)	35	35	45	20	30
Location of Shaft Pivot Point					
Station (in.)	700	602	520.7	510	320
Waterline (in.)	154	154	118.27	135	141
Butt Line (in.)	0	0	-14.85	0	280.5
Slope of Lift Curve (/deg)	.100	.100	.107	.100	.100
Drag-Divergence Mach Number	.87	.82	•80	.87	.87

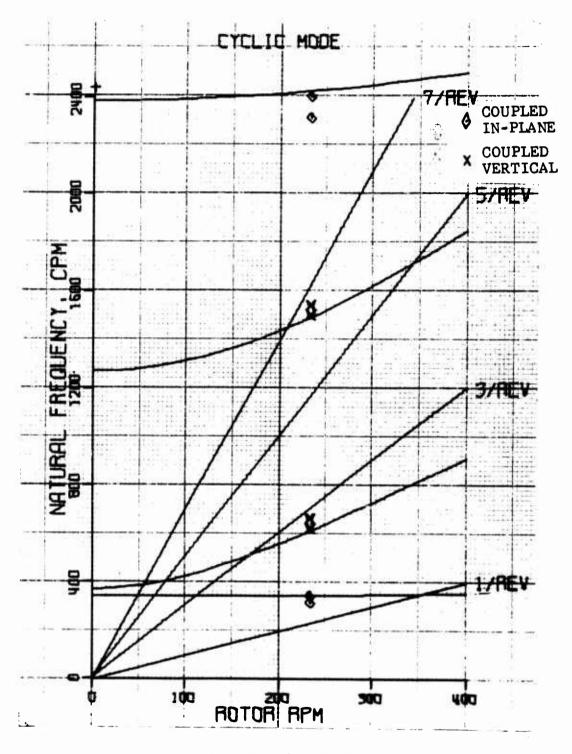
	TABLE	VI – Cont	inued		
	Pure Single Roto		Com- pound No. 2	Tandem	Side by Side
ROTOR 2 (Cont'd)					
Coefficients for Nondivergent Drag Equation					
50	.010	.010	.010	.010	.010
δ ₁ (/deg)	00005	00005	0	00005	00005
δ ₂ (/deg)	.00018	.00018	.00003	.00018	.00018
Gear Ratio	.108	.120	.251	.01758	.02475
ELEVATOR					
Area (ft ²)	34	34	15.0	_	90
Aspect Ratio	2.5	2.5	1000	_	4.5
Incidence (deg)	-2.5	2	6.21	mes.	-2
Collective-Pitch Coupling (deg/in.)	0	0	0	-	0
F and A Cyclic-Stick Coupling (deg/in.)	0.5	1	.827	_	1.67
Mast-Tilt Coupling Factor	0	0	0	-	0
Location of Center of Pressure					
Station (in.)	502	602	398.5		635.3
Waterline (in.)	120	200	56		195
Slope of Lift Curve	.055	.058	.0524	-	•07
Drag Coefficient at Zero Attack	.010	.015	.008	-	.010
FIN					
Rudder Connection	No	Yes	No	No	Yes
Area (ft ²)	45	45	25	45	100
Aspect Ratio	2.5	2.5	1000	2.5	1.6
Incidence (deg)	10	1	4.5	0	0
Tail-Rotor Coupling Factor	0	2	0	-	o

	TABLE VI	- Contin	ued		
,	Pure Single Rotor	Com- pound No. 1	Com- pound No. 2	Tandem	Side by Side
FIN (Cont'd)					
Location of Center of Pressure					
Station (in.)	700	602	501	520	609.6
Waterline (in.)	144	111	84	111	180.0
Butt Line (in.)	0	0	0	0	0
Slope of Lift Curve	.055	.055	.040	.055	.039
Drag Coefficient at Zero Attack	.01	.01	.008	•01	.01



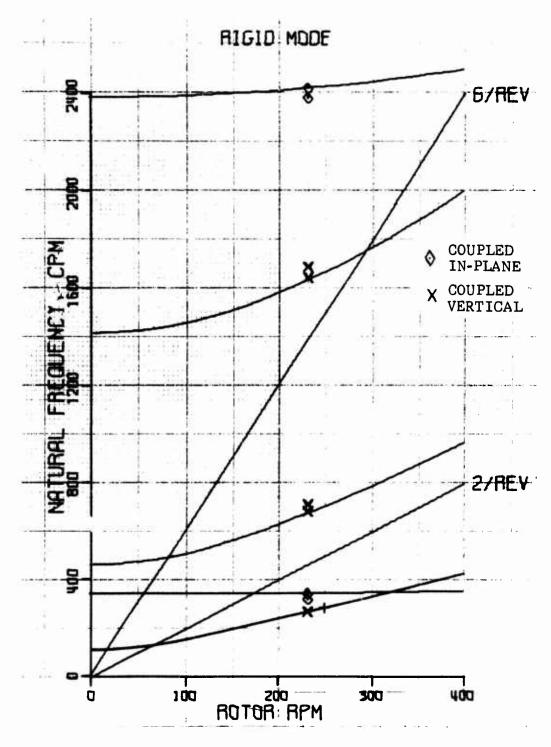
a. Collective Modes

Figure 24. Coupled Rotor Natural Frequencies (4-Bladed Rigid Rotor).



b. Cyclic Modes

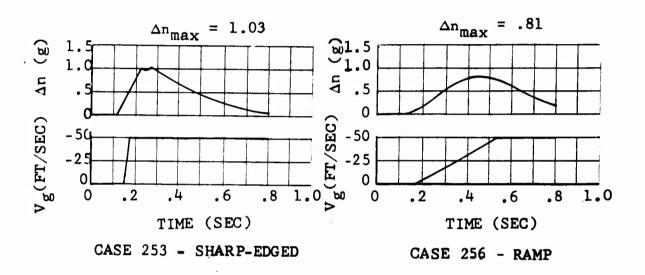
Figure 24 - Continued.

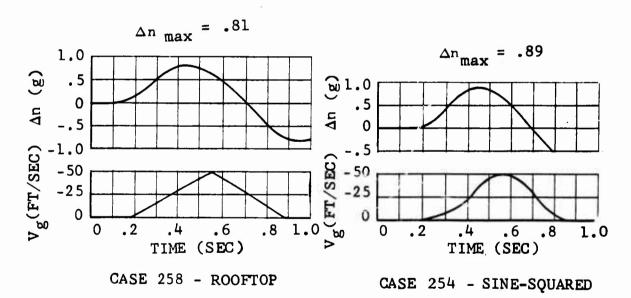


c. Rigid Modes

Figure 24 - Continued

COMPOUND SINGLE-ROTOR HELICOPTER VELOCITY = 150 KT GROSS WEIGHT = 8500 LB DISC LOADING = 5.6 LB/SQ FT C_T/σ = .064





All cases include gradual penetration and nonsteady aerodynamics. $V_{\rm g}$ is taken at the cg of the aircraft.

Figure 25. Effect of Gust Shape on the Gust-Load Factor.

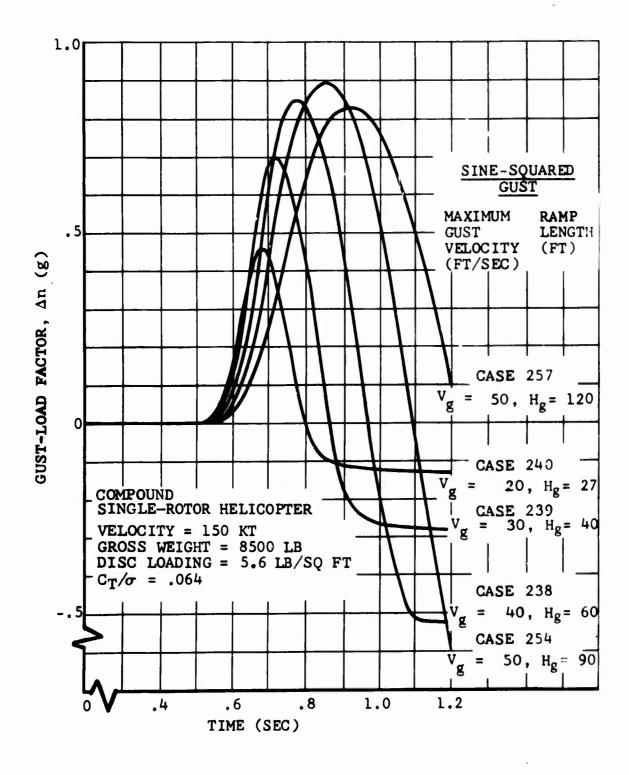


Figure 26. Effect of Ramp-Length and Gust-Velocity Combinations on the Gust-Load Factor.

In Figure 27 the effect of the Hg and V_g combinations (from Figure 18) on maximum gust load, blade flapping, fuselage pitching, and blade loads is shown. The maximum value of Δn occurs for the combination of $H_g=90$ feet and $V_g=50$ ft/sec. This combination is used throughout the remainder of this study although flapping and hub bending moments are more critical at longer ramp lengths.

EFFECT OF CONFIGURATION

Rotorcraft configurations represented in the gust-response case study are:

- pure single-rotor helicopter

- compound single-rotor helicopter

- pure tandem helicopter

- trailing rotor

- stopped rotor

- tilt rotor

About 85 percent of the cases were run on pure single-rotor helicopter and compound single-rotor helicopter configurations. The tilt-rotor cases include speed variations with mast tilt of 90 degrees, thus simulating aircraft flight conditions. Trailed-rotor and stopped-rotor cases were computed using methods as described previously.

The compound single-rotor helicopter cases generally produced The compound single-rotor nellcopter cases generally produced higher values for the gust-alleviation factor, K_g , than did the pure single-rotor helicopter cases. Since the wing plays a principal role in the compound single-rotor helicopter configuration, factors were computed for the wing (K_{gw}) and for the rotor (K_{gr}) separately, thus: $K_{gw} = \frac{\Delta L}{\Delta L} \frac{\Delta$

$$K_{g_w} = \frac{\Delta L_{sine-squared}}{\Delta L_{sudden}}; \quad K_{g_r} = \frac{\Delta T_{sine-squared}}{\Delta T_{sudden}}$$
 (15,16)

The net value, Kg, for the compound single-rotor helicopter configuration, considering only wing and rotor effects, can be expressed as

$$K_{g} = \frac{\Delta L_{sudden} K_{g_{w}} + \Delta T_{sudden} K_{g_{r}}}{\Delta L_{sudden} + \Delta T_{sudden}}$$
(17)

This value will differ slightly from the ratio Ansine-squared/ Ansudden since the fuselage, with control surfaces and tail rotor, has some effect. The advantage of separating rotor and wing gust-response ratios is to allow comparison with the other configurations. COMPOUND SINGLE-ROTOR HELICOPTER
DISC LOADING = 5.6 LB/SQ FT

 $C_T/\sigma = .064$ V = 150 KT

CASES 238, 239, 240, 254 and 257

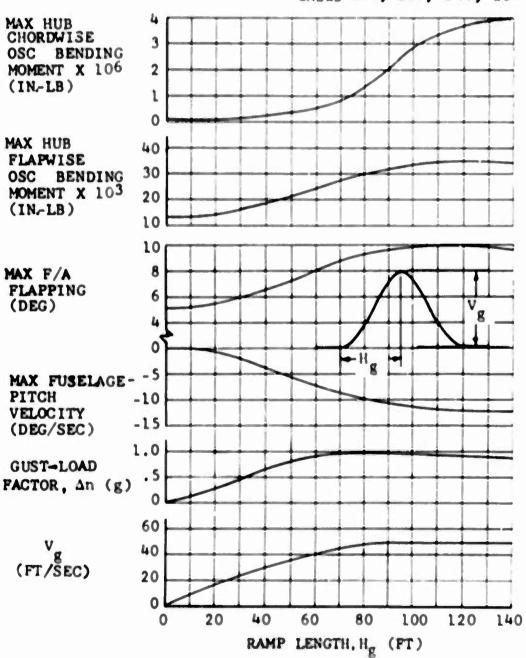


Figure 27. Effect of Combinations of Hg and Vg on a Compound High-Speed Helicopter for a Sine-Squared Gust

The compound single-rotor helicopter cases are characterized by the proportion of lift carried by the main rotor in steady flight. Although a broad range of auxiliary-thrust values was required to trim these cases, the gust-response characteristics were not materially affected. The average value of $K_{\rm g}$ for cases with thrust more than 1/3 the gross weight is .47, which compares closely with a mean $K_{\rm g}$ of .50 for pure single-rotor helicopter cases. Average $K_{\rm g}$ for compound single-rotor helicopters with unloaded rotor is .65. The histograms in Figures 28, 29, and 30 show the distribution of alleviation factors computed for these two configurations.

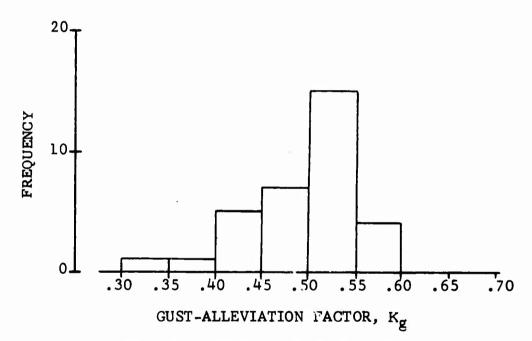


Figure 28. Histogram of Gust-Alleviation Factors for Pure Single-Rotor Configuration.

The compound single-rotor configuration cases may also be compared with the airplane configurations by considering $K_{\rm g}$ (Figure 30). For the compounds, $K_{\rm g}$ averaged .79, with about 50% of the cases having a value in the .80 to .85 interval. The average value of $K_{\rm g}$ for airplane cases is .83, thus establishing a strong relationship for all the wing-response evaluations.

Results of eight cases for the tandem configuration are summarized in Table VII. The sine-squared gust responses were adversely affected by choice of fuselage parameters determining pitch stability. Parameters selected for the tandem cases include low fuselage-pitching inertia, aft cg location, zero rotor overlap, and no elevator, all of which are conservative in regard to the sine-squared gust response. The results

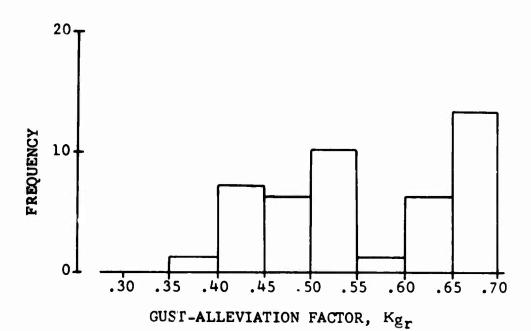


Figure 29. Histogram of Rotor Gust-Alleviation Factors for Compound Single-Rotor Configuration.

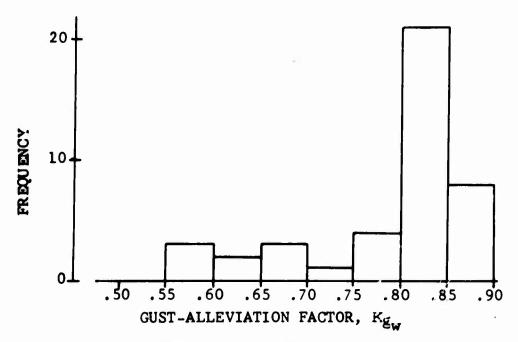


Figure 30. Histogram of Wing Gust-Alleviation Factor for Compound Configuration.

of this limited study suggest a need for further investigation to delineate the individual importance of these parameters.

Figure 31 is a time history of three variations of cg location. Pitch attitude, and aircraft normal acceleration are shown in relation to the gust disturbance. For the aft and neutral cg cases, the continued increase in g level after both rotors emerge from the gust is clearly a function of the severe pitch displacement and the high forward speed. A dashed line is also shown in Figure 31 as an approximation of the acceleration level attributable solely to pitch attitude. By removing this effect from the computed responses, adjusted gust-alleviation factors are obtained that agree with those for a single-rotor helicopter. The adjusted alleviation factors are included in Table VII below.

							V
Case	Speed	DL	$\frac{c_{T}/\sigma}{}$	Gust	Δn	Kg	^{ng} adj.
183	200	7	.02	sudden	4.37	1.14	
184	200	7	.02	sine-squared	4.97	1.14	. 57
185	200	7	.05	sudden	1.35	77	50
186	200	7	.05	sine-squared	1.04	.77	. 52
187	225	7	.02	sudden	4.09		5.0
188	225	7	.02	sine-squared	4.56	1.12	. 56
189	225	7	.05	sudden	1.22	~ 1.	50
190	225	7	.05	sine-squared	0.91	.74	. 58

A good measurement of the effects of a gust on a stopped rotor or a trailed rotor is the shear load at the root of the blade, shown as time histories in Figures 32 and 33 for airspeeds of 100, 200, 300, and 400 knots. The requirements of this study (Table I) specify only sine-squared gust encounters for these two configurations. To provide a common basis for evaluation of results, sudden-gust responses also have been computed and are presented herein without the assignment of additional case numbers. For identification purposes, the suffix "A" denotes sudden-gust response and "B" denotes sine-squared gust response.

In each case, the aircraft is considered to be flying faster than the transition speed and operating in the fixed-wing aircraft mode with the rotor(s) stopped and unloaded. For the trailed-rotor configuration, the three blades of each rotor are assumed to be folded aft as depicted in Figure 20 (page 51). For the stopped-rotor configuration (Figure 19), the analysis is restricted to a two-bladed rotor with the blades assumed to be completely stopped and locked at the forward and aft azimuth positions.

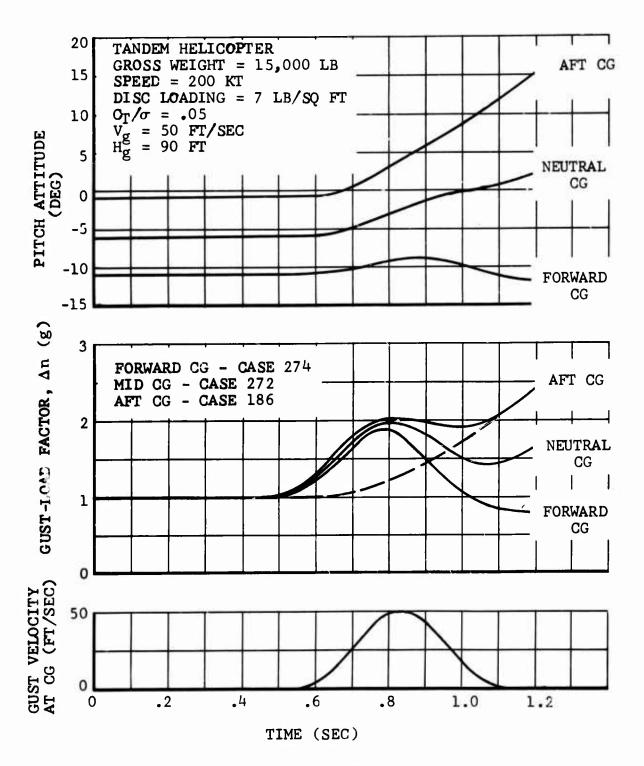
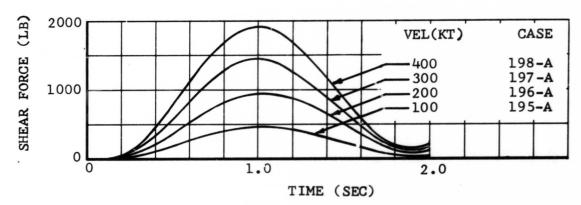
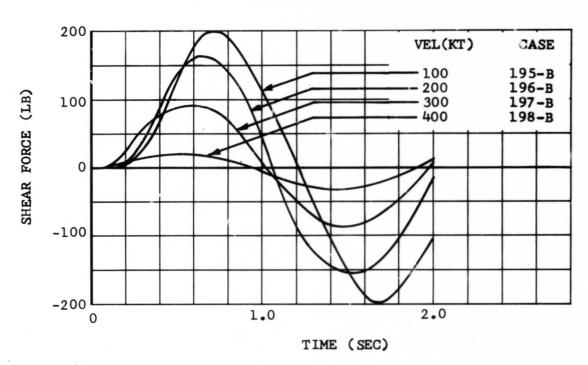


Figure 31. Time History of Tandem-Helicopter Response to 50-Ft/Sec Sine-Squared Gust.

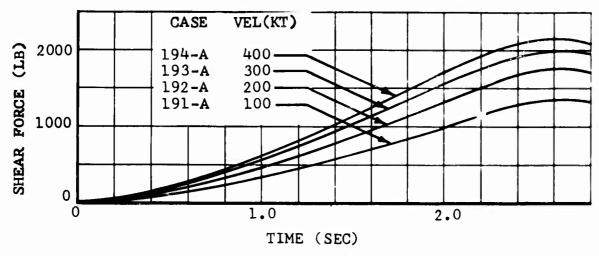


a. Sudden Vertical Gust

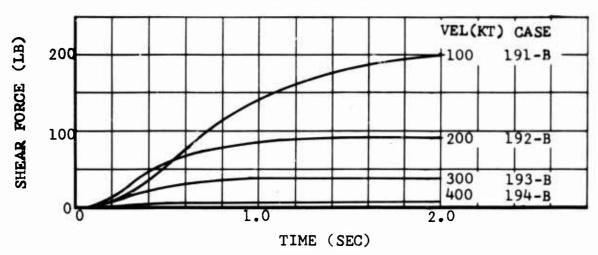


b. Sine-Squared Vertical Gust
 Figure 32. Stopped-Rotor Shear at Forward Blade Root.

For a sudden gust, the root-shear loads of both configurations increase with increasing airspeed (Figures 32a and 33a). The response is essentially proportional to the product of the angle-of-attack change and the square of the forward speed. The angle-of-attack change, however, is inversely proportional to the forward speed. Except for pitching and heaving motions of the aircraft, then, the sudden-gust response of both configurations is directly proportional to the forward speed.



a. Sudden Vertical Gust



b. Sine-Squared Vertical Gust

Figure 33. Trailed-Rotor Shear at Wing Tip.

The period of the sudden-gust response is a function of the natural frequencies of the structural system and is independent of forward speed. In changing suddenly from one steady environment to another, the transient response builds up rapidily and oscillates while tending to decay to a steady value equal in magnitude to one-half of the first peak. This effect is illustrated in Figure 32a.

For a sine-squared gust, the root-shear loads of both configurations decrease with increasing airspeed (Figures 32b and 33b), because of the decreasing time that is required for the aircraft to pass through the gust field. At the lowest speed for which a response was computed (100 knots), the entire length of the sine-squared gust (180 feet) is traversed in only 1.07 seconds. The effective length of the gust and the equivalent traversal time are reduced by the shape of the gust; the first peak of

the stopped-rotor response for 100 knots occurs after about 0.7 second. Elapsed time to the first peak decreases with increasing forward speed. After the first response peak has been reached, the response period is controlled by the natural frequencies and pitching characteristics of the aircraft, as indicated in Figure 32b.

The difference in character of the gust-response time histories for the stopped- and trailed-rctor configurations is attributable to the wing-torsion effect for the latter. In a typical transient for this type of structure, wing bending and wing torsion respond at unequal periods. In comparison with Figure 32b (stopped-rotor), Figure 33b shows a relatively flatter first-peak response due to wing-torsion lagging wing-bending.

By dividing the shear load due to a sine-squared gust by the shear due to a sudden gust, a shear ratio can be obtained for each case. This shear ratio bears some similarity to K_g as calculated for the conventional helicopter cases. Figure 34 shows a comparison of the shear ratios based on maximum response for both a stopped rotor and a trailed rotor. The figure shows a marked decrease in the shear ratio as velocity increases.

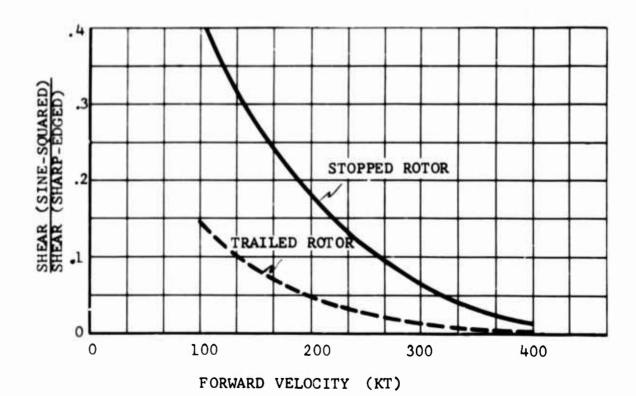


Figure 34. Gust Response for Stopped and Trailed Rotors, Cases 191-198.

The gust response of a <u>tilt-rotor</u> composite-type aircraft has been investigated in considerable detail. In the airplane mode, the gust response of this configuration is generally similar to that of a fixed-wing airplane, with the wing-lift increase proportional to the forward speed. An additional consideration is the vertical-force increment from the rotor.

Figure 35 shows gust-load factors versus velocity for both sudden and sine-squared gusts. Over the range from 200 to 300 knots, the gust-load factors vary linearly with speed and the gust-alleviation factor is almost constant at 0.83. For the parameters used in this study, a flapping instability was computed for the sine-squared gust case at 400 knots. Since the basic problem of prop-rotor stability is affected by many design considerations (wing stiffness, pylon mounting, control system, stabilizing devices, etc.) that are not represented in the analysis, this subject was not pursued further in this study. It is appropriate to note that no implications are made by these results as to either forward speed limitations or attainable design ranges for the tilt-rotor configuration.

Figure 35 also indicates the effect of wing stall at speeds below 200 knots. Figure 36 shows an example of the aircraft's behavior due to a 50-ft/sec sine-squared gust at a speed of 150 knots. The effect of wing stall is quite obvious. The gust-

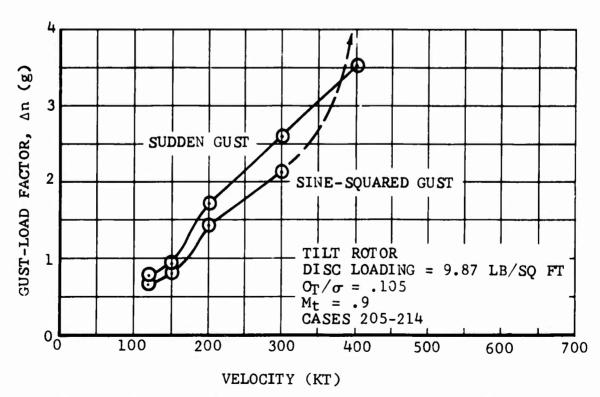


Figure 35. Acceleration Due to Gusts Versus Velocity, Tilt-Rotor Configuration in Airplane Mode.

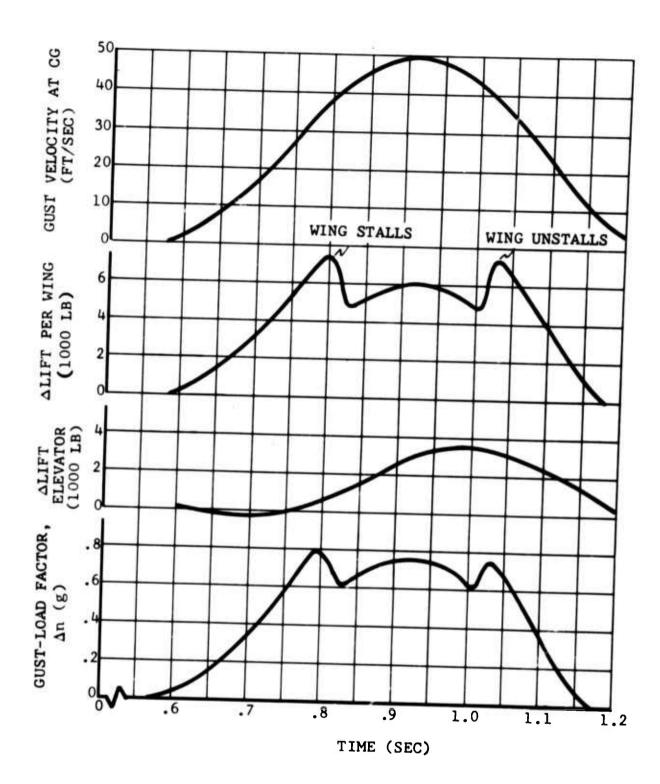


Figure 36. Vertical Sine-Squared Gust, Tilt-Rotor Airplane Configuration, 150 Knots, Case 208.

alleviation factor (0.81 at 120 knots) is not significantly affected by the occurrence of wing stall.

In the helicopter-mode, the tilt-rotor configuration responds to gust encounters in a manner typical of the compound configuration.

Figure 37 shows a time history of one of the cases where the aircraft is subjected to a 50-ft/sec sine-squared vertical gust during a pylon conversion process. The pylon moves from a partial conversion angle of 25 degrees toward the airplane position at a rate of 15 degrees per second. It can be seen that the gust produces both vertical and horizontal accelerations due to the increase in rotor thrust. The wing, of course, adds mainly to the vertical accelerations. Longitudinal blade flapping is increased by about 2 degrees. A number of similar cases were investigated; the vertical and the forward accelerations (body reference) due to a 50-ft/sec sine-squared gust during the conversion are given in Table VIII.

	TABLE VIII.	PRINCIPAL	RESULTS 0	F TILT-ROTOR	CASES
(Sine-	Squared Gust)		ñ		
		Convers: (de	ion Angle	Body-Refe Accelerat	
Case	Speed (kt)	At Start of Gust	At Peak of Gust	$\Delta a_{\mathbf{Z}}$ (Vertical)	∆a _x (Forward)
201	120	30	38	.89	•42
202	120	60	68	.55	.36
203	150	30	36	1.37	.50
204	150	60	67	1.02	•57

In addition to the study requirements (Table I), Figure 38 presents the effect of a 50-ft/sec horizontal sine-squared gust on a tilt-rotor aircraft (in airplane mode) at 350 knots. The variation in rotor thrust and horizontal acceleration is shown along with the gust-velocity curve. The slightly negative (aft) acceleration during steady-state flight is due to the pitch attitude of the fuselage in the gravity field. The maximum change in forward acceleration (body reference) is about -.38 g for this case.

EFFECT OF ROTOR TYPE

In this study, rotors are characterized by the hub arrangement as articulated, semirigid, or rigid. The analysis was first

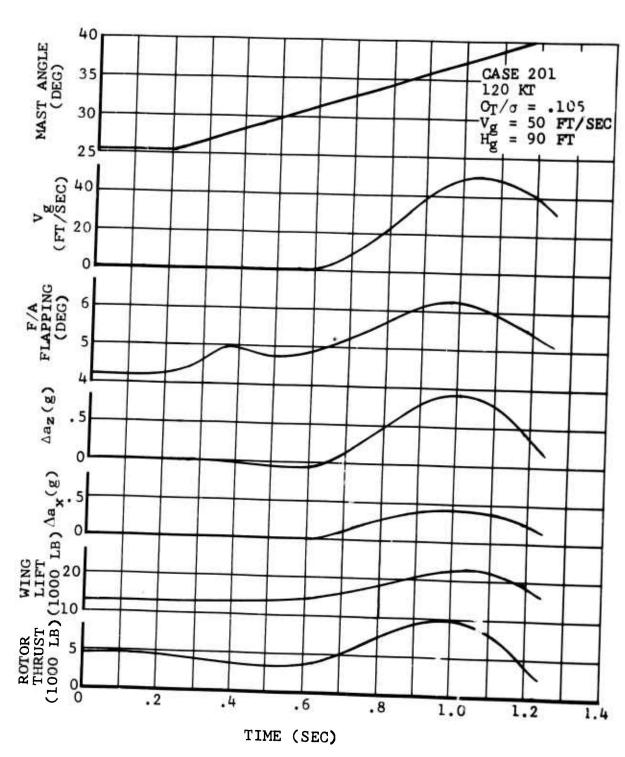


Figure 37. Sine-Squared Gust During Conversion of Side-by-Side Helicopter.

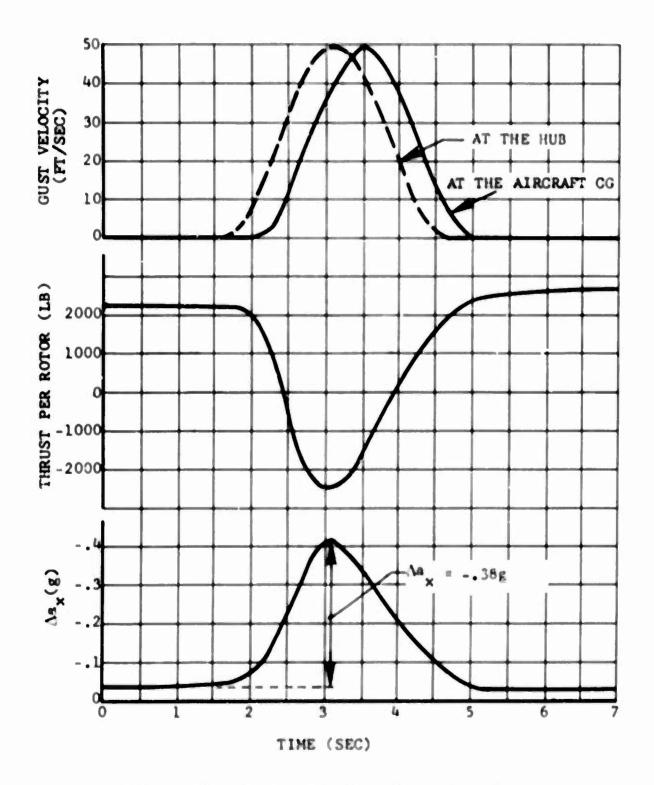


Figure 38. Horizontal Sine-Squared Gust, Tilt-Rotor Airplane Configuration, 350 Knots.

set up for a rotor with flapping hinge at the hub centerline and no chordwise articulation. This is called the semirigid rotor.

A rotor with no articulation still has some effective flapping as a result of elastic bending. This arrangement is referred to as a rigid rotor and is simulated by adding a spring restraint between the blade and the mast in the semirigid representation. A sketch of the resulting general configuration is shown in Figure 39a. The semirigid rotor is then a special case (spring constant, K, equal to zero).

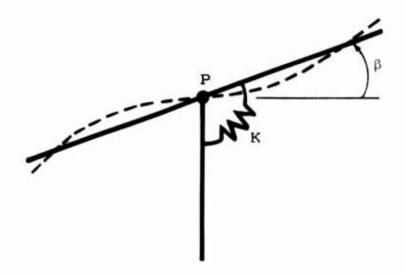
The rotor with offset flapping hinges is called an articulated rotor (Figure 39b). This rotor type was related to the no-offset type by considering the moment transmitted to the top of the mast in either case.

The rotor types simulated with flapping spring, K, have a moment, K β , about the hub. In the case of the articulated rotor, the moment about the hub is the product of the vertical component of shear at the hinge point, Q, and the hinge-offset distance, e. If CF is the centrifugal force at the hinge, the vertical component of shear is approximately equal to (CF)sin β cos β or, for small flapping angles, (CF) β . By choosing K so that K = e(CF) per unit angle, the rigid rotor and articulated rotor can be compared. The articulated-rotor and rigid-rotor flapping responses to the sudden gust are, therefore, nearly identical, as computed in the program. The dynamic treatment in the bending-moment analysis is different, and variations in flapping appear in the sine-squared cases run with aerodynamic feedback.

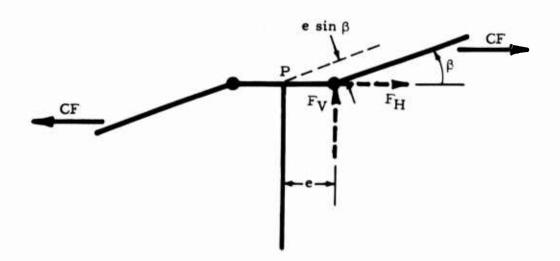
The most extensive set of cases available for comparison is the group of 200-knot, .9 advancing blade-tip Mach number cases that were computed for five or more combinations of disc loading and blade loading for each of the three rotor types. Both pure and compound single-rotor helicopter configurations were included. Results of these cases are listed in Table IX.

The 20 semirigid, 24 articulated, and 24 rigid-rotor cases at 200 knots have the same average value of $K_{\rm g}$, 0.50. The range for articulated and rigid rotors is .42-.56, while the compound single-rotor helicopter cases for semirigid rotors spread the range for that type to .40-.67. Corresponding cases (i.e., those having the same disc loading and $C_{\rm T}/_{\rm J}$) for articulated and rigid rotors generally have a $K_{\rm g}$ of near the same value.

Time histories for tip-path-plane-attitude variation during a sine-squared gust are shown in Figure 40a. The three rotor types shown are for a disc loading of 7.0 and $C_{\rm T}/\sigma$ of .05. Forward speed is 200 knots and advancing blade-tip Mach number is .90. As the rotor penetrates the gust, it produces positive



(a) Rigid Rotor $M_P = K\beta$



(b) Articulated Rotor $M_{\mathbf{P}} = \mathbf{e} \ \text{SIN } \beta \cdot \text{CF COS } \beta \approx (\mathbf{e} \cdot \text{CF})\beta$

Figure 39. Schematic of Rotor Types.

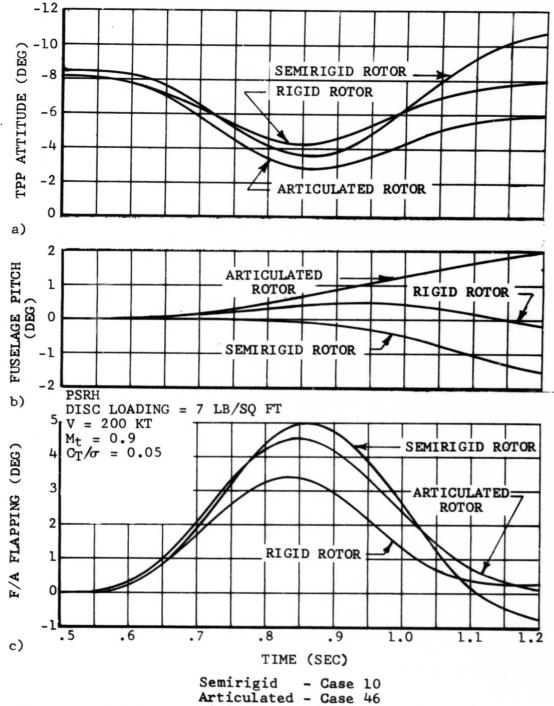
flapping velocities in each case. The resulting displacements reach maximum value at about .85 second, or .35 second after the rotor encounters the gust. The articulated rotor has flapped more than a degree farther than the rigid rotor by this time.

The change in fuselage-pitch attitude with time (Figure 40b) and the change in flapping with respect to the swashplate (Figure 40c) indicate the interconnections affecting rotor response. As would be expected, flapping excursion for the semirigid is greater than for the other two hub types. The rigid case shows marked damping of the flapping oscillation. The lower value of Kg for the rigid, .44, as compared with .52 for the articulated. is attributed to blade-dynamics effects. The semirigid case has a Kg of .53.

TABLE							HUB TYP	
Case	Conf	Hub Type	Disc Load- ing	$\mathtt{C}_{\mathrm{T}}/\sigma$	Δn_{r} SUDV	Δn _r SSQV	Kgr	Max. Flap Vel.*
39-40	PSRH	AR	4.	.02	5.22	2.65	.521	15.6
17-18	PSRH	SR	4.	.02	5.19	2.39	.471	12.3
51-52	PSRH	RR	4.	.02	5.22	2.81	.551	16.2
135-136	CSRH	AR	4.	.02	5.63	2.81	.499	13.9
111-112	CSRH	SR	4.	.02	5.62	2.57	.457	12.2
147-148	CSRH	RR	4.	.02	5.63	2.89	.513	14.2
41-42	PSRH	AR	4.	.05	1.90	1.07	.565	28.3
21-22	PSRH	SR	4.	.05	1.91	1.03	.547	25.4
53-54	PSRH	RR	4.	.05	1.90	1.02	.537	25.9
137-138	CSRH	AR	4.	.05	1.86	1.02	.548	24.4
117-118	CSRH	SR	4.	.05	1.95	1.03	.528	15.2
149-150	CSRH	RR	4.	.05	1.98	1.04	.525	19.9
43-44	PSRH	AR	7.	.02	5.30	2.56	.492	14.9
55-56	PSRH	RR	7.	.02	5.30	2.55	.491	14.3
139-140	CSRH	AR	7.	.02	5.95	2.58	.434	12.5
151-152	CSRH	RR	7.	.02	5.95	2.64	.444	12.5
*For the	sine_s	quered	(even-	numbara	d) cas	0.0		

*For the sine-squared (even-numbered) cases.

		TA	BLE IX	- Cont	inued			
Case	Conf	Hub Type	Disc Load- ing	$^{ extsf{C}}_{ extsf{T}}/\sigma$	Δ n $_{ m r}$ SUDV	Δ n $_{r}$ SSQV	Kgr	Max. Flap Vel.*
45-46	PSRH	AR	7.	.05	1.84	.96	.522	26.7
9-10	PSRH	SR	7.	.05	1.87	.97	.516	26.3
57-58	PSRH	RR	7.	.05	1.84	.81	.440	19.8
141-142	CSRH	AR	7.	.05	1.70	.90	.529	25.4
91-92	CSRH	SR	7.	.05	2.22	1.46	.660	16.8
153-154	CSRH	RR	7.	.05	1.70	.90	.529	25.4
25-26	PSRH	SR	10.	.02	5.32	2.33	.438	12.0
47-48	PSRH	AR	10.	.02	5.31	2.21	.425	12.6
59-60	PSRH	RR	10.	.02	5.31	2.32	.447	13.1
123-124	CSRH	SR	10.	.02	5.48	2.19	.399	10.7
143-144	CSRH	AR	10.	.02	5.42	2.29	.423	12.1
155-156	CSRH	RR	10.	.02	5.42	2.34	.432	12.1
29-30	PSRH	SR	10.	.05	1.79	.94	.525	27.1
49-50	PSRH	AR	10.	.05	1.77	.88	.497	25.9
61-62	PSRH	RR	10.	.05	1.77	.91	.514	26.8
129-130	CSRH	SR	10.	.05	1.89	1.03	.545	18.7
145-146	CSRH	AR	10.	.05	1.78	.93	.522	12.1
157-158	CSRH	RR	10.	.05	1.78	.95	.534	22.4



Rigid - Case 58

Gust Response for Three Hub Types. Figure 40.

To obtain insight in the effect of hub rigidity (or hub spring) four additional cases have been run on a four-bladed rigid rotor where the hub stiffness is varied as an independent variable. The results are shown in Table X. It is found that increasing the hub stiffness increases both the gust-load factor Δn and the gust factor $K_{\mbox{\scriptsize g}}$.

TABLE X. RESULTS FOR	R VARIED	HUB STIFFNESS	ON A RIGID	ROTOR
Hub-Spring Stiffness (Lb-In/Deg)	Vel (Kt)	Gust Type	Δn (g)	Кg
1260	120	Sine-squared Sudden	1.95	.756
3675	120	Sine-squared Sudden	2.21 3.58	.855

EFFECT OF DISC LOADING

Disc loadings of 4, 7, and 10 lb/sq ft were used for a variety of pure single-rotor helicopter and compound single-rotor helicopter cases. The tandem configuration has a disc loading of 7 lb/sq ft; the tilt-rotor configuration, near 10 lb/sq ft. The pure single-rotor helicopter cases are more suitable for showing effects of disc loading since the compound single-rotor helicopter cases are strongly influenced by rotor-to-wing-loading ratios. In addition to the 58 cases at 200 knots used in the discussion of effects of hub type (See Table IX), four cases at 175 knots and six cases at 225 knots are available for comparison.

Values of Kg for four-bladed, semirigid rotor helicopters at forward speeds of 175 to 225 knots and advancing blade-tip Mach numbers of .85 and .90 are shown in Figure 41. These cases were run with disc loadings of 4, 7, and 10 lb/sq ft. A slight downward trend of Kg is evident as the disc loading is increased. However, the low values of Kg for the combination of a rotor thrust coefficient-solidity ratio of .02 and a disc loading of 10 lb/sq ft are not considered to be significant because the rotor geometric parameters are not within reasonable limits. Variation of Kg with OT/o seems to be more pronounced than with either disc loading or forward velocity. Acceleration increments for the same cases are given in Figure 42. The slight variation with disc loading shown in this figure is overshadowed by the differences due to rotor thrust coefficient-solidity ratio.

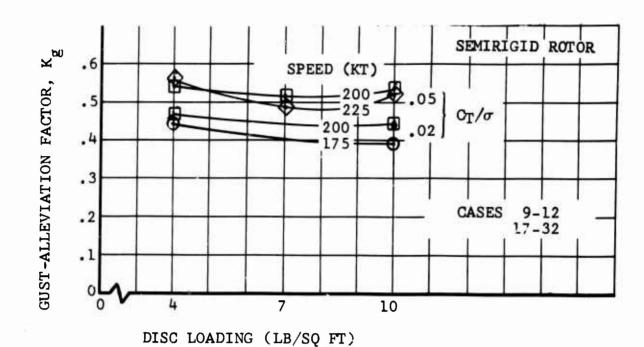
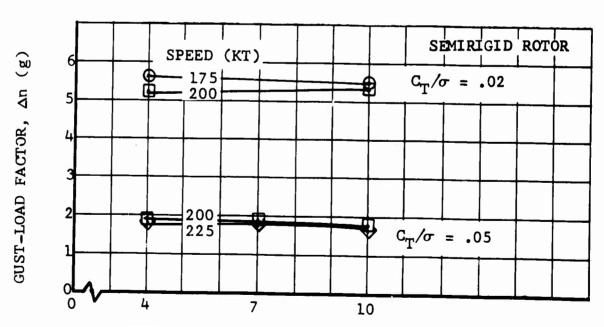


Figure 41. Effects of Disc Loading on Gust-Alleviation Factor.



DISC LOADING (LB/SQ FT)

Figure 42. Effects of Disc Loading on Sudden-Gust Response.

Results from compound single-rotor helicopter cases are somewhat more scattered than for the pure single-rotor helicopter. Considering only the 200-knot cases, average values of K_g for the different disc loadings range from .40 to .51 for $C_T/\sigma=.02$ and from .53 to .67 for $C_T/\sigma=.05$. The An values for suddengust cases vary from 6.5 to 7.0 for the lower rotor thrust coefficient-solidity ratio and from 2.9 to 3.3 for the higher. Changes in vertical acceleration due to change in rotor thrust only range from 5.4 to 5.9 for low rotor C_T/σ and from 1.8 to 2.2 for high C_T/σ . No particular trend with disc loading can be deduced from these data.

EFFECT OF ROTOR THRUST COEFFICIENT-SOLIDITY RATIO, ${\tt C_T/\sigma}$

The variation in the rotor thrust coefficient-solidity ratio, C_T/σ , which is a measure of the blade-lift coefficient, C_1 , produces the most pronounced change in Δn results, as seen in Table IX. Figure 42 also shows a consistently large shift in Δn for sudden gusts in going from low thrust coefficients ($C_T/\sigma = .02$) to high coefficients (.05).

A remarkable correspondence of Δn levels due to sine-squared gusts at the same values of C_T/σ is revealed in Table IX. Since the acceleration change values shown in the table are based on rotor-thrust change only, the compound single-rotor helicopter may be included with the pure helicopter. At the lower value of C_T/σ , the range for Δn is from 2.2 to 2.9; while for C_T/σ = .05, the range is from 0.8 to 1.1. Thus, there is in excess of 1.0g lower response to sine-squared gusts for the C_T/σ = .05 cases in comparison with the C_T/σ = .02 cases.

A limited number of cases were computed at C_T/σ = .08. Figure 43 shows Δn for sine-squared and for sudden gusts as functions of C_T/σ . The reduction in normal acceleration response with increasing blade-lift coefficient is evident. Average values of Δn (sine-squared gust) for the .02 and .05 cases at 200 knots are used in Figure 43.

Increasing rotor-blade flapping velocity with rotor thrust coefficient-solidity ratio is evidenced by the results. Average values from Table IX are plotted in Figure 44. The values of $C_{\rm T}/\sigma$ = .08 are also shown.

EFFECT OF ADVANCING BLADE-TIP MACH NUMBER

Advancing blade-tip Mach number variations from .80 to .95 are used in a series of cases with disc loading of 7.0 lb/sq ft and $C_{\rm T}/\sigma$ = .05. These cases cover a forward-speed range from 200 to 350 knots, encompassing both pure and compound single-rotor helicopter configurations with four-bladed semirigid rotors.

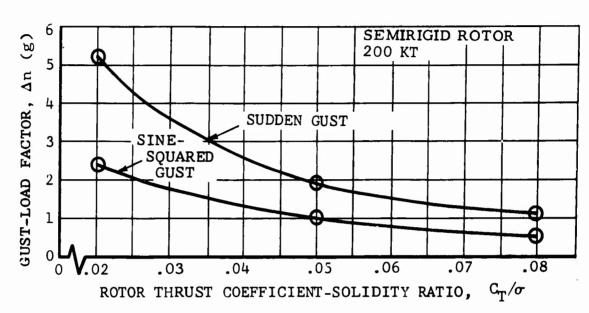


Figure 43. Effect of $C_{\rm T}/\sigma$ on Rotor Gust-Load Factor for Sudden and Sine-Squared Gusts.

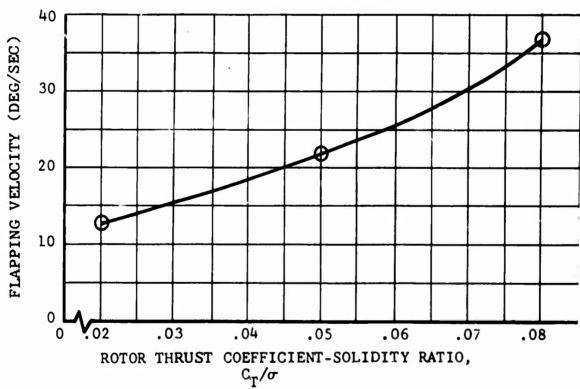


Figure 44. Effect of C_T/σ on Maximum Rotor-Flapping Velocity Due to Sine-Squared Gusts, Semirigid Rotor.

For the pure single-rotor helicopter, sine-squared gust runs, Δn holds almost constant at about .97 for 200 knots and .92 for 225 knots through advancing blade-tip Mach number of .90. At M_{t} = .95 there is a slight decrease in Δn values for both velocities. Corresponding to this situation, the K_{g} curves (Figure 45) turn sharply up at the high M_{t} end. This effect is associated with the input parameter for determination of drag divergence. In the calculations for this study, drag divergence begins at M_{t} = .87 for low angles of attack. A substantial portion of the outboard blade section is subject to significant compressibility effects at M_{t} = .95, resulting in an upturn in the gust-alleviation factor. This compressibility effect is further illustrated by plotting horsepower required vs M_{t} , as given in Figure 46 for a series of 200- and 225-knot cases.

Flapping velocities shown in Figure 47 for the pure single-rotor configuration sine-squared gust cases also indicate an increase in response with advancing blade-tip Mach number. The Lock number for all of these cases is $\gamma = 8.3$.

The situation for the compound-helicopter gust cases is again masked to some extent by other variables. Variations for Δn for sine-squared vertical gust cases are shown in Figure 48 for five velocities. Median values of .83 for K_g and .65 for K_{gr} resulted from calculations.

EFFECT OF FORWARD SPEED

As has been previously indicated, values of alleviation factors do not change radically with forward speed. However, the principal features of response, vertical acceleration and rotor flapping, show an upward trend with increasing forward The compound configuration offers an interesting example since the rotor- and wing-lift increases must both be considered. The An values for the entire aircraft, including fuselage, elevator, and tail-rotor response are also of interest. The most extensive velocity sweep was made for the compound cases with disc loading of 7.0 lb/sq ft and $C_{\rm T}/\sigma$ = .05. Δn for the entire helicopter and for the rotor and wing is plotted in Figure 49. Note that the rotor response falls off slightly above 300 knots. This is due to increasing stall since the advance ratio is becoming very large. The wing-lift increase due to encountering the gust is proportional to the forward speed. Rotor-flapping velocity versus forward velocity for 20 compound single-rotor helicopter cases is given in Figure 50, and fuselage-pitching velocity versus velocity, in Figure 51. Fuselage-pitching velocity reduces with forward speed since the dynamic pressure at the elevator tends to act against a change in pitch orientation.

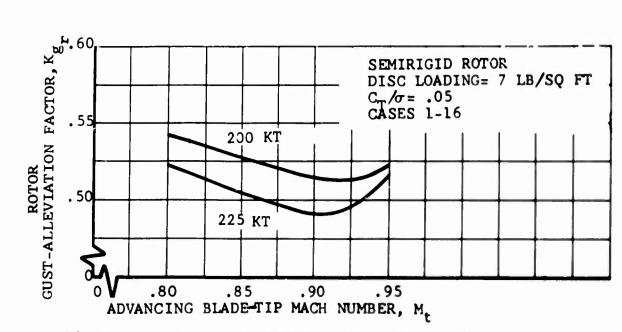


Figure 45. Rotor Gust-Alleviation Factor Versus Advancing Blade-Tip Mach Number for a Pure Single-Rotor Helicopter.

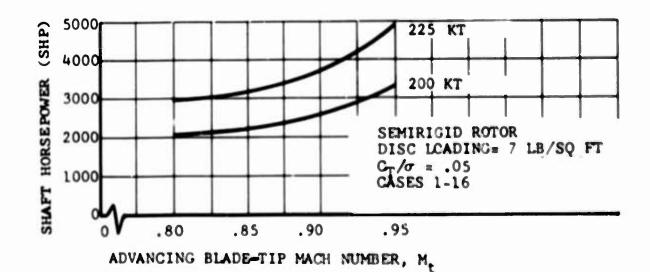


Figure 46. Required Shaft Horsepower Versus Advancing Blade-Tip Mach Number for a Pure Single-Rotor Helicopter.

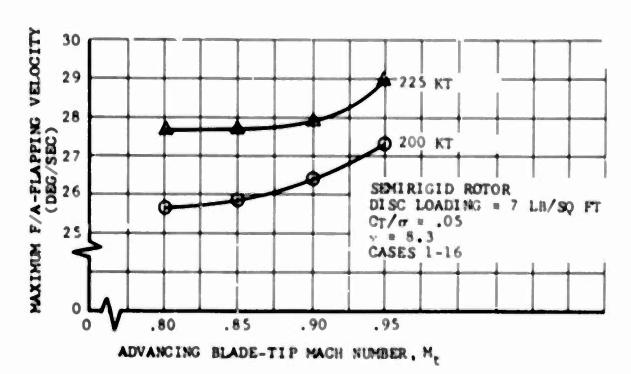
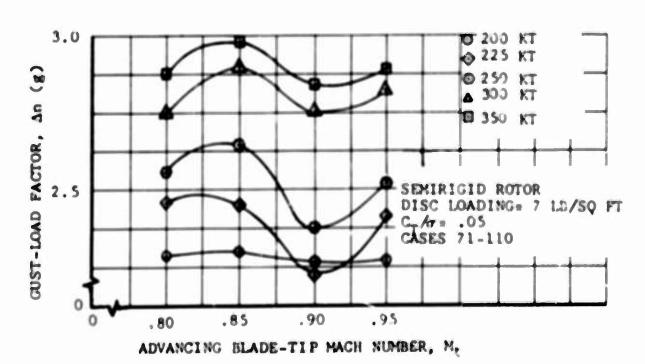


Figure 47. Flapping Velocity Versus Advancing Blade-Tip Mach Number for a Pure Single-Rotor Helicopter.



Pigure 48. Gust-Load Factor Versus Advancing Blade-Tip Mach Number for a Compound Helicopter.

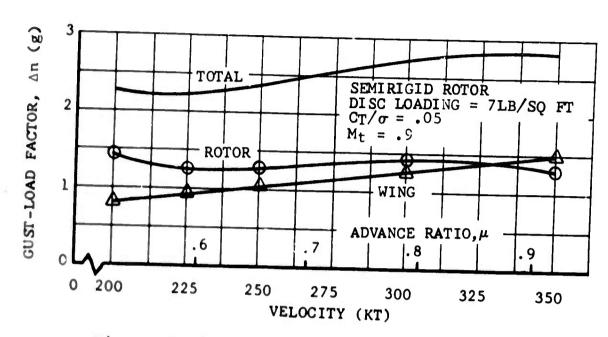


Figure 49. Acceleration Due to Sine-Squared Gust Versus Velocity for a Compound Single-Rotor Helicopter, Cases 91-110.

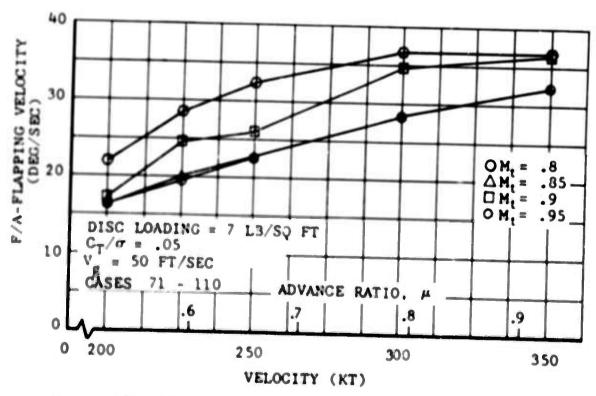


Figure 50. Flapping Velocity Versus Forward Speed for Sine-Squared Gust Cases, Compound Single-Rotor Helicopter.

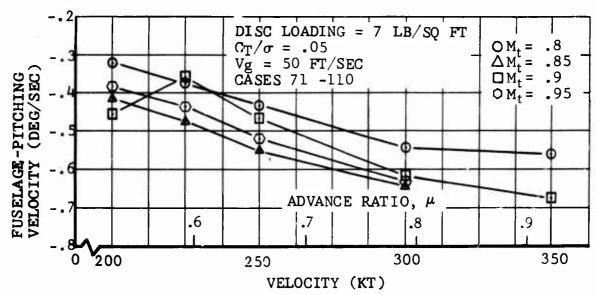


Figure 51. Fuselage-Pitching Velocity Versus Forward Speed for Sudden-Gust Cases, Compound Single-Rotor Helicopter.

EFFECT OF LOCK NUMBER, Y

The influence of Lock number on the gust response for three values of advance ratio has been evaluated for the articulated-, semirigid-, and rigid-rotor systems. A 50-ft/sec maximum-velocity gust was used in each of the 27 sine-squared gust cases. The simplified method, with a sudden gust, was used to compute responses for comparison with the detailed method calculations. Only one Lock-number value was used for the suddengust calculations because there is not time for this variation to affect the maximum an calculated. All of the cases in this group (cases 278 through 313) are four-bladed, pure single-rotor helicopter configurations with a disc loading of 7.0 lb/sq ft, OT/s of 0.05, and advancing blade-tip Mach number of .9. Advance ratios of .39, .45, and .50 were selected for the calculations. Lock-number values of 8.31, 5.56 and 4.43, used in these cases, were obtained by varying blade-tip weight.

The normal acceleration change due to gust loading, an, is listed in Table XI for each of the 36 cases. No significant variation with rotor configuration or with advance ratio was observed. There is, however, a definite indication of increasing an with increasing blade inertia.

For the articulated and semirigid rotors, the gust-alleviation factor varies with Lock number from .56 for = 8.31 to .66

for γ = 4.43 at μ = .45. The cases for μ = .39 and μ = .50 have only slightly different values of K_g at corresponding Lock numbers.

Time histories of the flapping, normal-acceleration increment, and flapping velocity are presented in Figures 52 through 57 for the different advance ratios for the articulated- and the semirigid-rotor types. The response curves for each of three Lock numbers of the sine-squared gust cases are shown on the same graph for a particular advance ratio and rotor type. The general character of the response is not changed over the range of Lock-number variation considered. The response curves for the rigid-rotor cases were practically the same as for the corresponding articulated-rotor cases. All of the configurations show the highest blade-flapping displacement and flapping velocity and the lowest Δn for the high Lock number (8.31). As Lock number is reduced, the maximum flapping velocity decreases and Δn increases.

The higher flapping velocities reduce the relative velocity normal to the tip-path plane as the gust passes across the forward section of the rotor disc. Lower rotor-thrust values are thus computed for the high Lock-number cases. These results emphasize that the effect of flapping velocity must be included in any analysis of gust response for helicopters.

	TABLE	TABLE XI. PRI	PRINCIPAL RESULTS	ULTS OF LO	OF LOCK-NUMBER VARIATION	VARIATIO	NC	
Advance Ratio	Forward Speed	Lock Number	Articulated	ed Rotor	Semirigid Rotor	d Rotor	Rigid F	Rotor
1 .	(kt)	>	Δn(g)	Kg	Δn(g)	Kg	$\Delta n(g)$	Kg
.39	150	*8.31	1.78	,	1.75	1	1.78	'
.39	150	8.31	1.03	.58	1.02	.58	1.03	.58
.39	150	5.56	1.11	.62	1.10	.63	1.11	.62
.39	150	4.43	1.17	99.	1.16	99*	1.17	99.
.45	175	*8.31	1.81	1	1.83	1	1.81	,
.45	175	8.31	1.02	• 56	1.02	.56	1.03	.57
.45	175	5.56	1.12	.62	1.11	.61	1.12	.62
54.	175	4.43	1.19	99.	1.19	.65	1.19	99.
.50	200	*8.31	1.83		1.85	,	1.83	1
.50	200	8.31	1.00	.55	0.99	.54	1.00	.55
.50	200	5.56	1.11	.61	1.11	09.	1.11	.61
.50	200	4.43	1.19	.65	1.18	79.	1.19	.65
*Indicates	es sudden-gust	gust cases.						

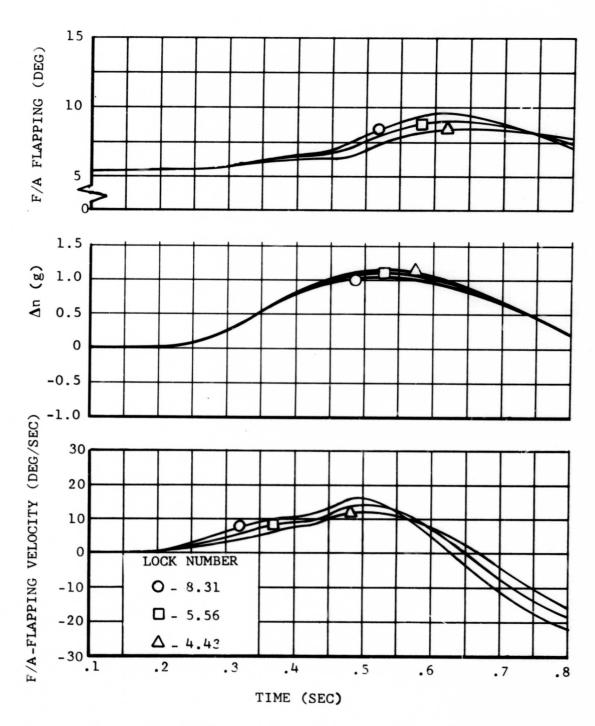


Figure 52. Effect of Lock Number on Response of Articulated Rotor to Sine-Squared Gust at 150 Knots.

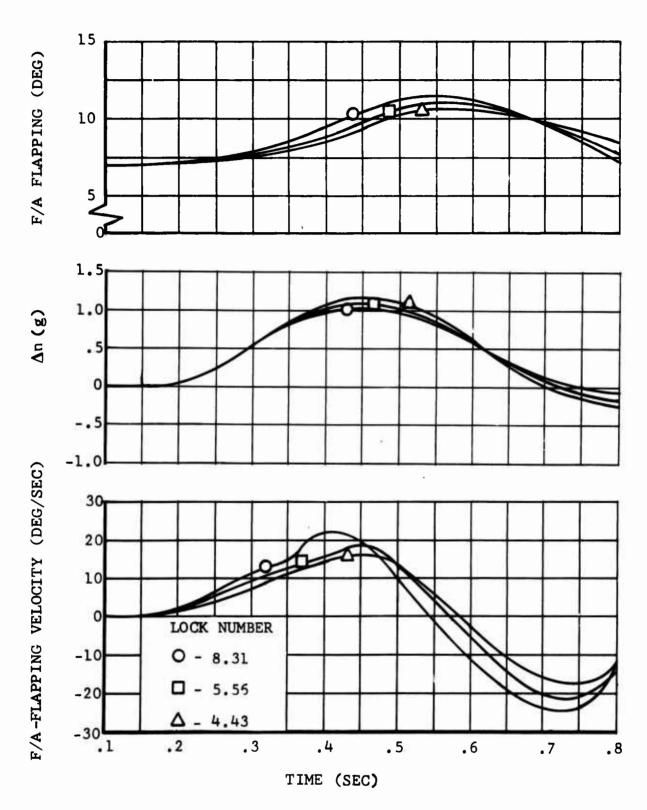


Figure 53. Effect of Lock Number on Response of Articulated Rotor to Sine-Squared Gust at 175 Knots.

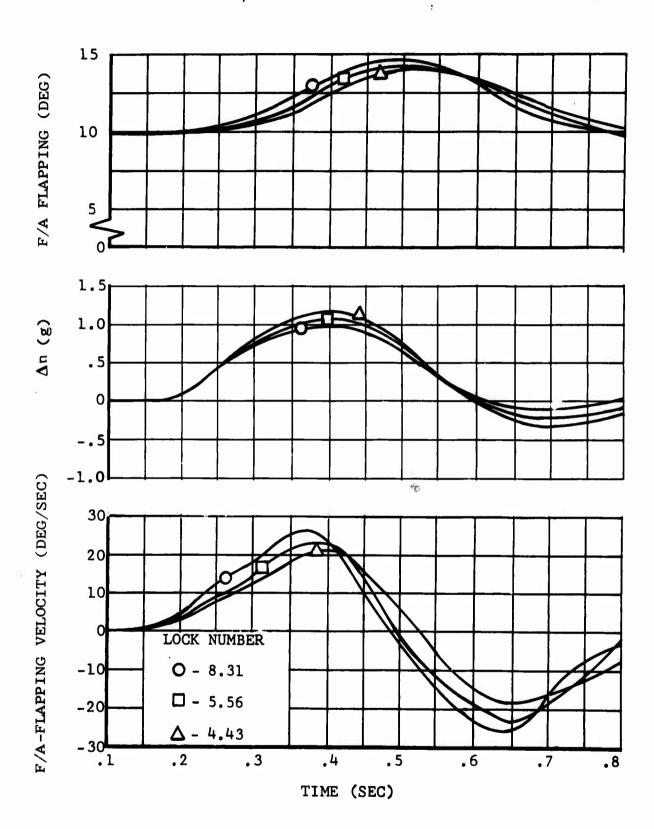


Figure 54. Effect of Lock Number on Response of Articulated Rotor to Sine-Squared Gust at 200 Knots.

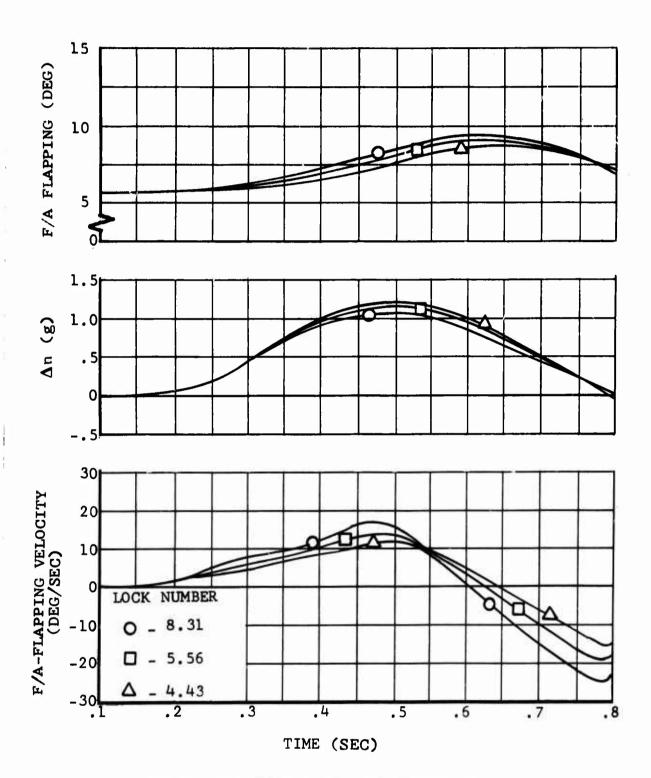


Figure 55. Effect of Lock Number on Response of Semirigid Rotor to Sine-Squared Gust at 150 Knots.

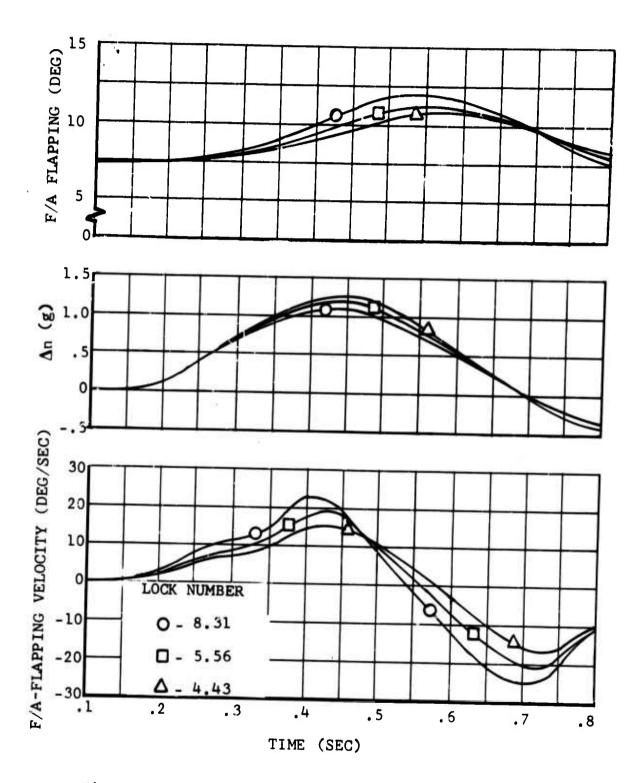


Figure 56. Effect of Lock Number on Response of Semirigid Rotor to Sine-Squared Gust at 175 Knots.

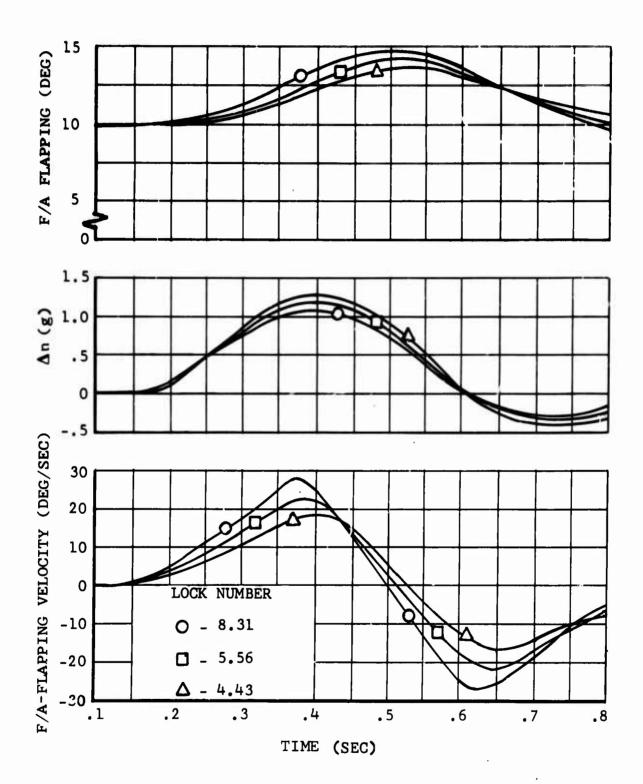


Figure 57. Effect of Lock Number on Response of Semirigid Rotor to Sine-Squared Gust at 200 Knots.

EFFECT OF ROTOR UNLOADING BY THE WING

The set of compound single-rotor helicopter cases (cases 71-134) was trimmed for a considerable range of rotor-thrust to wing-lift ratios. This variation, achieved while holding rotor rpm constant, had a significant effect on computed values of Kg, as was mentioned in the section on configuration effects. The lift-change ratios at maximum acceleration due to gusts as they vary with velocity are shown in Figure 58 for disc loading of 7 and $C_{\rm t}/\tau$ of .05. As would be expected, the rotor thrust predominates at the lower speeds and the wing lift at the higher speeds. Further, it is seen that the ratio is higher for sudden gusts than for sine-squared gusts. This points up the generality of the lower value of alleviation factors for rotors than for wings, since for

$$\frac{\left(\frac{\Delta T}{\Delta L}\right)_{\text{sine-squared}}}{\frac{\Delta T}{\Delta L}_{\text{sudden}}} < \frac{\left(\frac{\Delta T}{\Delta L}\right)_{\text{sudden}}}{\frac{\Delta L}{\Delta L}_{\text{sudden}}}$$

The rotor-thrust-change ratio is equal to Kg_r , the alleviation factor for the rotor; and the wing-lift-change ratio is equal to Kg_w , the alleviation factor for the wing. Therefore,

$$K_{g_r} < K_{g_w}$$
 (18)

The shaded bands in Figure 58 contain the load-share ratios at maximum loading for the majority of the compound-configuration cases considered. An analysis of the results calculated for 54 cases shows that the wing-lift change due to a gust versus velocity is very nearly linear for each of the gust shapes used. On the other hand, the rotor-lift increment is almost constant over the speed range. The rotor-thrust change due to a vertical sudden gust of 50 ft/sec averaged about 33,000 lb, while for the sine-squared gust of 50-ft/sec maximum amplitude, the average thrust change was 21,000 lb. The almost-constant rotor-thrust increment computed over the velocity range from 200 knots to 350 knots is consistent with the results shown in Figure 5, page 9. Thus the relative contribution of the rotor to gust response decreases as velocity increases.

EFFECT OF GUST-ALIEVIATING DEVICES

Three gust-alleviating devices were investigated:

- Pitch-cone couplingPitch-flap coupling
- Bobweight in collective-pitch system

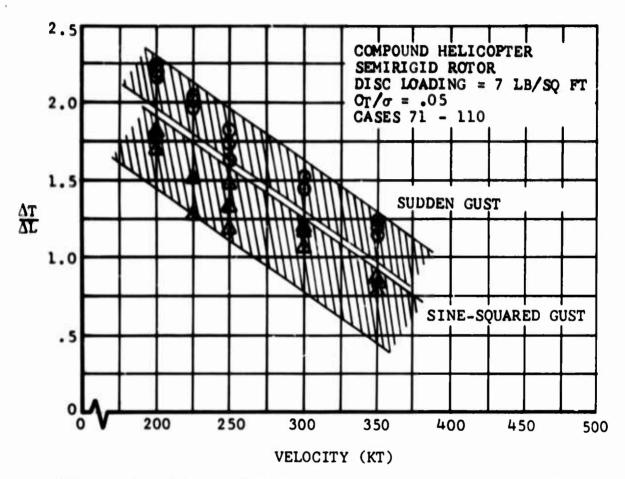


Figure 58. Ratio of Change in Rotor Thrust, ΔT , to Change in Wing Lift, ΔL , Due to Gusts Versus Forward Velocity.

Pitch-come coupling is present in the rotor system when the steady-state component of the rotor-blade flapping angle produces simultaneously a change in blade pitch. Pitch-flap coupling results in a change in blade pitch proportional to the one-per-rev component of the blade-flapping angle.

The effect of pitch-cone coupling on the sharp-edged gust response of a compound helicopter with a two-bladed semirigid rotor is illustrated in Figure 59. These gust-response time histories include the effects of penetration, nonsteady aerodynamics, and aeroelastic feedback. The difference indicated in Figure 59 is due to a pitch-cone coupling ratio of -1 (for case 269), whereby a one-degree increase in rotor coning causes a one-degree reduction in the collective pitch setting at the rotor. A sketch is included in the figure to indicate one possible geometric configuration of the rotor that will produce this coupling. Note that, because the pitch-horn points are on the flapping axis at the rotor centerline, rotor flapping does not introduce additional control coupling.

Figure 60 shows the effect of pitch-cone coupling on the sine-squared gust response of a pure helicopter with a four-bladed semirigid rotor. The range of coupling values for these cases is from -.5 to +.5, with the former value causing a 15% reduction in the gust-load factor.

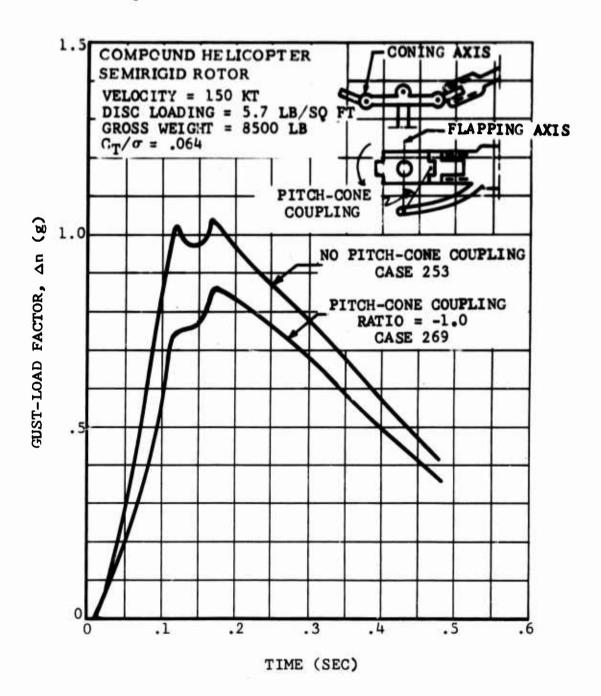


Figure 59. Effect of Pitch-Cone Coupling on Sharp-Edged Gust Response With Penetration, Nonsteady Airloads, and Aeroelastic Feedback.

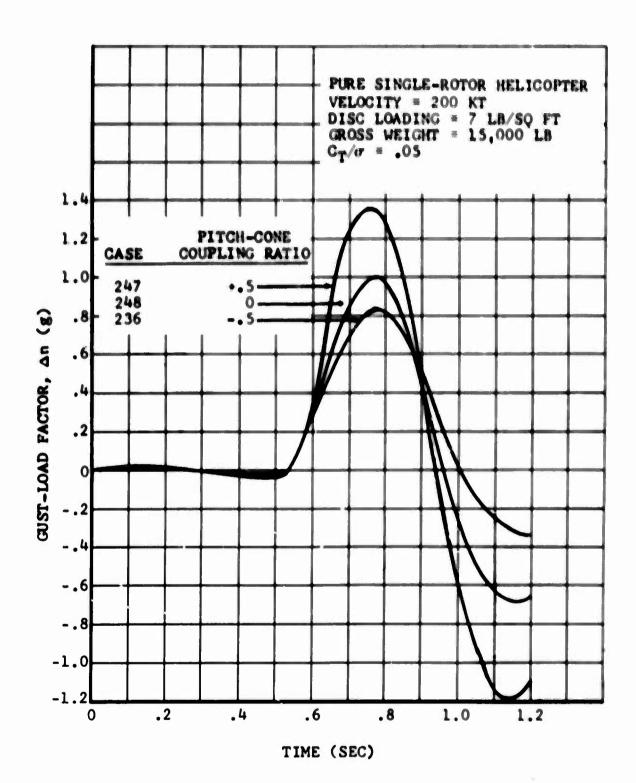


Figure 60. Effect of Pitch-Cone Coupling on Sine-Squared Gust Response.

The effect of pitch-flap coupling (δ 3) is shown in Figure 61 for a pure helicopter with a four-bladed semirigid rotor. The effect of 30 degrees of pitch-flap coupling on the maximum gust-load factor is very small. However, a considerable damping effect is indicated by the reduced overshoot. Figure 61 includes a sketch of one possible configuration with δ 3. In this arrangement, coning occurs about the offset hinges and causes no control coupling.

Combinations of pitch-cone coupling and pitch-flap coupling are possible in many ways. In articulated systems, the coupling ratios usually are equal because both coning and flapping occur about the offset axis of each blade. In rigid and semirigid rotors, the spanwise distribution of structural flexibility is an important consideration because bending of the structure has effects similar to those of a hinge.

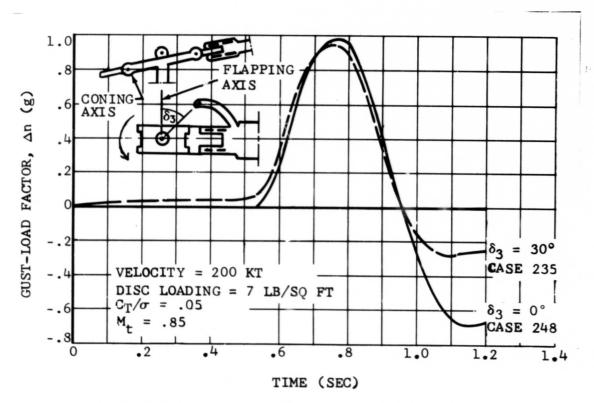
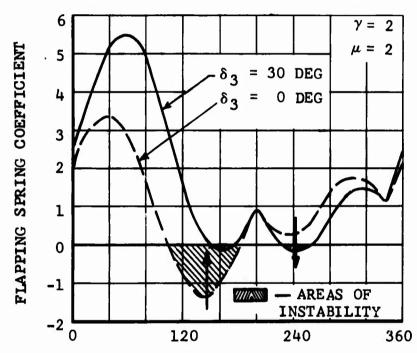


Figure 61. Gust Alleviation Due to Pitch-Flap Coupling (δ_3) for a Pure Single-Rotor Helicopter.

Pitch-flap coupling can have a pronounced influence on flapping stability, particularly at high advance ratios. Gust response at advance ratios greater than 1.0 depends primarily on flapping stability. Coupling between blade flapping and pitch can have a stabilizing effect. Figure 62 is a plot of the spring coefficient, $g_0(\psi)$ for δ_3 = 0 and for δ_3 = 30°, from equation (14), page 53. This illustrates the local spring-rate variation for a high- μ case. The large region of instability starting in the second quadrant is considerably reduced by pitch-cone coupling. However, a secondary destabilizing trend develops in the third quadrant with increasing δ_3 . Arrows in the negative spring-coefficient areas point in the direction of change in stability with increasing pitch-cone coupling. A closer investigation of this subject is in order for future studies.



BLADE AZIMUTH POSITION, ψ (DEG)

Figure 62. Effect of Pitch-Flap Coupling (δ3) on Flapping Stability for a Pure Single-Rotor Helicopter.

A third possibility for reducing gust sensitivity is the use of a bobweight in the collective control system. This concept was discussed by Drees and McGuigan (8). In Figure 63 the effect of a mechanism which reduces the collective pitch one degree per g is shown. This bobweight rate reduces the response to the sine-squared gust by about 15%. Of course, this rate can be increased, and damping can be added to prevent instability which might otherwise occur.

PURE SINGLE-ROTOR HELICOPTER SINE-SQUARED GUST DISC LOADING = 7 LB/SQ FT C_T/σ = .05 M_{+} = .85

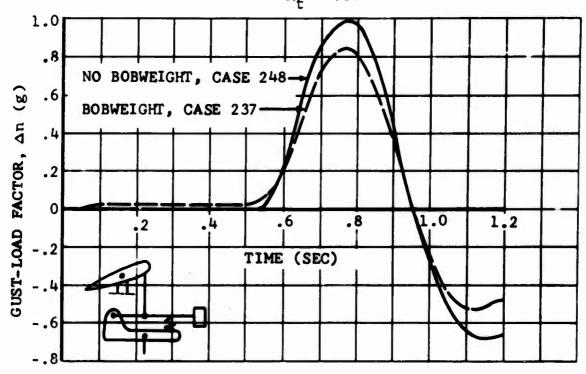


Figure 63. Gust Alleviation Due to a Bobweight $(\Delta\theta/\Delta n = -1 \text{ deg/g})$, Cases 237, 248.

EFFECT OF HORIZONTAL GUSTS

The effect of horizontal gusts has been investigated for a number of cases. The principal results are given in Figure 64 for the case of head-on horizontal gusts for forward speeds of 200 and 225 knots. Sudden-gust cases for the simplified analysis and sine-squared-gust cases for the detailed analysis are calculated for the horizontal gusts. The gradual penetration of the rotor disc into a horizontal sine-squared gust is represented in a manner similar to the vertical-gust case. The gust is assumed to consist of a sine-squared type of variation of the horizontal component of the wind velocity over a specified segment of the fixed x-axis. A ramp length, Hg, of 90 feet was used for these cases. The additional horizontal

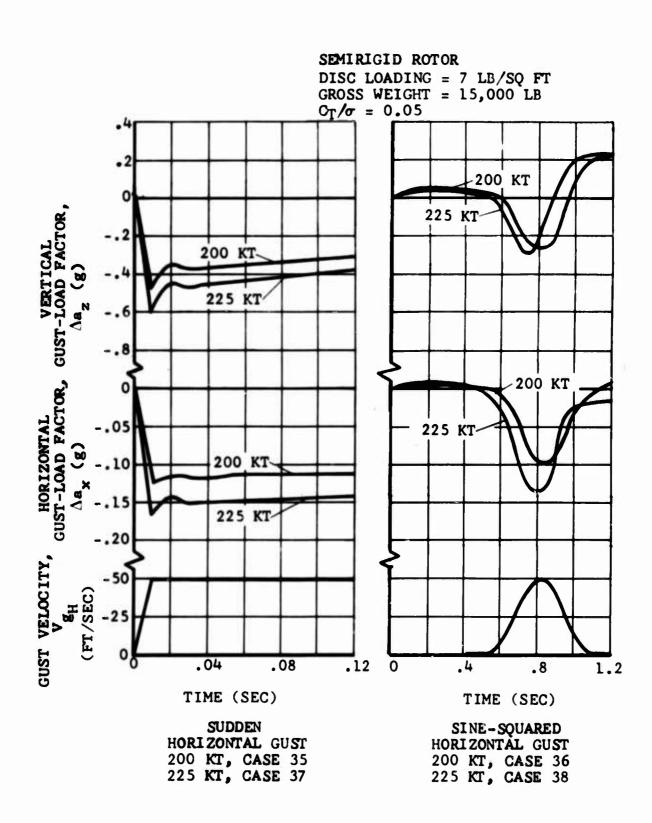


Figure 64. Effects of Horizontal Gusts, Pure Single-Rotor Helicopter.

velocity due to the gust is computed for each evaluated point on the rotor disc as a function of the x-coordinate (fixed reference) of that point.

The load factors involved are not of great consequence: less than .6g for the vertical load factor and less than .15g for the horizontal load factor. The effect on the rotor loads is equally small except for Case 38, where a blade-resonance condition results due to the gust. Table XII gives the computed values for the maximum oscillatory in-plane bending moments at the center of the rotor, normalized to the corresponding trim values.

	TABLE XII. PRI	NCIPAL RESULTS	OF HORIZONTAL GUST CASES
	Disc Loadi	ng = 7; C_T/σ =	.05; Madv tip = .9
Case No.	Forward Speed (Kt)	Horizontal Gust Type	Bending-Moment Factor Due to Gust
35	200	sudden	1.15
36	200	sine-squared	1.71
37	225	sudden	.78
38	225	sine-squared	2.02

A horizontal gust applied to a tilt-rotor aircraft in the airplane mode does not yield a large effect either. Figure 38 gives an example case, showing that a horizontal delta acceleration of -.38g is caused by a sine-squared horizontal gust of 50 ft/sec.

The effect of a lateral horizontal gust on a single-rotor helicopter is shown in Figure 65. It is seen that little effect results in the way of load factors on the airplane.

The use of a 50-ft/sec horizontal gust velocity with a ramp length of 90 feet is reasonably well established (Reference 36, Figures 20 and 21).

EFFECT OF ROTOR DYNAMICS

A major task of the gust-response study was the design of rotor dynamic characteristics for each combination of diameter, chord, number of blades, and rotor-hub type. If structural parameters for the rotor result in a natural frequency very near an excitation frequency of the forcing airloads, a numerical oscillation prevents proper operation of the program when aeroelastic feedback is included. The weight and stiffness distributions for the rotors used in this study are listed in

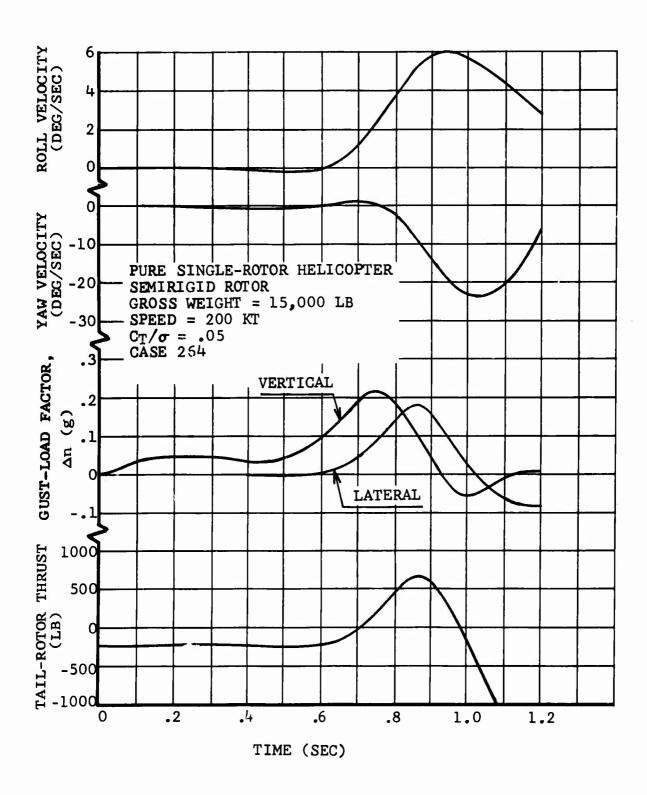


Figure 65. Time History of Response to a Lateral, Sine-Squared, 50-Ft/Sec Gust.

Appendix IV. Considerable effort was made to obtain realistic blade weight and stiffness distributions while controlling the dynamic characteristics to avoid resonances.

The rotor analysis considers three basic types of forced response, characterized by beam restraints at the hub centerline. Two of these are referred to as collective modes and cyclic modes. The collective modes describe the type of response to be expected from a sudden change in collective pitch. The cyclic modes describe the type of response to be expected from a sudden change in cyclic pitch. For simplicity, rigid mode refers to the response in the case of cantilevered boundary condition.

For a semirigid rotor, the collective mode is cantilevered beamwise (flatwise) and pinned chordwise (edgewise), the cyclic mode is pinned beamwise and cantilevered chordwise, and the rigid mode is cantilevered both beamwise and chordwise. The same centerline restraints apply to rigid and articulated rotors except that the cyclic mode is cantilevered beamwise. Hinges for the articulated rotor are simulated by extremely soft flexures located an appropriate distance from the axis of rotation. Lead-lag damper forces are applied based on the in-plane slope-change rate at 5% radius.

Collective pitch, built-in twist, and cyclic feathering are all included in the rotor dynamic analysis. Therefore, each of the three basic modes includes coupling effects among in-plane bending, out-of-plane bending, and blade-pitch displacements. In addition to the forced cyclic-feathering motions, the blade-pitching mode includes a torsionally rigid blade restrained by a single spring representing the control system.

The rotor dynamic response is calculated by harmonics of the rotor speed, with airloads components exciting modes as given in Table XIII.

TABLE XIII.	COUPLED MODES E	XCITED BY AIRLO	AD HARMONICS
Airload	N	umber of Blades	
Harmonic	2	3	4
Steady	Rigid	Rigid	Rigid
1/Rev	Cyclic	Cyclic	Cyclic
2/Rev	Collective	Cyclic	Rigid
3/Rev	Cyclic	Collective	Cyclic
4/Rev	Collective	Cyclic	Collective

A special path is available in the rotor dynamic analysis to study both coupled and uncoupled bending natural frequencies versus rotor speed and airload-excitation frequencies. Figure 24 shows the fan plots for a typical four-bladed rigid rotor used in the gust-response study. The lowest three uncoupled collective modes, Figure 24a, are cantilevered beamwise (flatwise), and the highest uncoupled collective mode is pinned chordwise (edgewise). In Figure 24b, the lowest and highest uncoupled cyclic modes are cantilevered chordwise, and the middle two uncoupled cyclic modes are pinned beamwise. Note that the uncoupled rigid modes, Figure 24c, match the uncoupled cantilevered modes of either the collective or the cyclic fan plot.

Coupled natural frequencies, including the effects of collective pitch and built-in blade twist, are also shown in the figure. The special path in the rotor-dynamics analysis will compute and plot the coupled frequencies for combinations of up to three values each of collective pitch and rotor rpm. For rotor designs used in this study, however, coupled frequencies were calculated only for the selected rpm and two collective-pitch values near the extremes of the anticipated range.

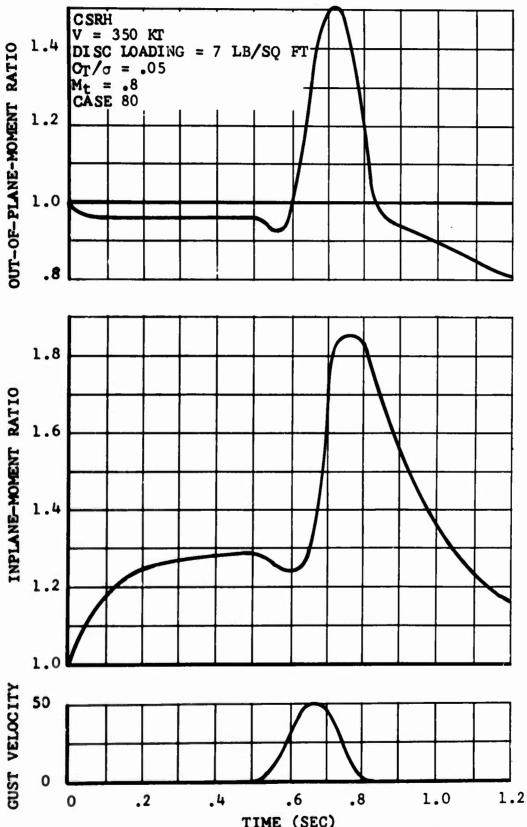
Figures 66 and 67 show oscillatory bending-moment ratios at the blade root for a series of pure single-rotor helicopter cases with a semirigid rotor. Figure 66 shows the ratios of maximum amplitude of oscillatory bending moment due to a sine-squared gust to that due to a sudden gust. The ratios in Figure 67 are maximum oscillatory bending moment due to a sine-squared gust to the oscillatory bending moment at the trim point. In both figures the ratios are shown as functions of advancing blade-tip Mach number for 200 krots and 225 knots. The oscillatory moments in a sine-squared gust are considerably higher than for a sudden gust (Figure 66), partly because of a smaller increase in rotor thrust. The sudden gust tends to stall a large amount of the rotor disc, leading to higher steady loads but lower oscillatory loads. The effect of rotor-thrust limit is also indicated in Figure 67, a comparison of maximum oscillatory loads in a sine-squared gust with those at the trim condition.

Part of the oscillatory-load level in a sine-squared gust is attributable to aeroelastic-feedback effects interacting between various harmonic airload components and the coupled rotor modes that are affected. Figure 68 is a typical time history of the maximum amplitude of oscillatory root bending moments, and illustrates the change in load level that occurs before the gust is reached. This change is due to the operation of the aeroelastic-feedback mechanism. The difference in the trim value and the steady-state value just before the gust excitation (at about .5 second, Figure 68) is a measure of the effect of including blade flexibility in the analysis.

Figure 66. Ratio of Oscillatory Root Bending Moments, Sine-Squared/Sudden, Cases 1-16.

PSRH, 4-BLADED SEMIRIGID ROTOR DISC LOADING = 7 LB/SQ FT, C_T/σ = .05 OUT OF PLANE IN-PLANE BENDING-MOMENT RATIO BENDING-MOMENT RATIO 200 KT 225 KT 200 KT 225 KT .75 .80 .85 .90 .95 .75 .80 .85 .90 .95 ADV-TIP MACH NO. ADV-TIP MACH NO.

Figure 67. Ratio of Oscillatory Root Bending Moments, Sine-Squared/Trim, Cases 1-16.



TIME (SEC)
Figure 68. Maximum Blade Root Oscillatory Moment Ratio
With Aeroelastic Feedback and Sine-Squared Gust

EFFECT OF BLADE TORSIONAL RESTRAINT

A limited consideration of blade torsion is included in the rotor dynamic analysis. Although the blade is considered to be torsionally rigid, blade-pitching moments act against a spring representing the blade-pitch control mechanism. The angular blade-pitch deflections are transmitted to the rotor aerodynamic analysis through the provisions for aeroelastic coupling.

The relative importance of blade torsional restraint on rotor loads was investigated by a series of three cases (275-277), in which only the torsional elasticity of the blade-pitch control system was varied. The cases are for a two-bladed single-rotor compound helicopter flying at a speed of 150 knots. As shown in Figure 69, the rotor loads increase only moderately as the oscillatory control displacement increases from zero to 1.5 degrees. It is to be noted that the rotor structural parameters used in this investigation have nearly optimum dynamic characteristics. For rotors with less well-behaved dynamics, blade-pitch control elasticity could be a primary variable in determining rotor loads.

MISCELLANEOUS EFFECTS

The computing program automatically accounts for the influence that elevator gust loads have on fuselage forces and moments. For this reason, the gust load on the entire aircraft, Δn , is found to differ slightly from the rotor thrust-weight ratio, $\Delta T/GW$.

Cases 1 and 2 (Table XXI) serve as examples. These are pure single-rotor helicopter cases with semirigid rotors. The forward speed is 200 knots in both cases. Case 1 is a sudden gust case, while Case 2 is a sine-squared gust case. The values of Δn and $\Delta T/GW$ for these two cases are as follows:

Case 1.
$$\Delta n = 1.81 \text{ g}; \frac{\Delta T}{GW} = 1.70 \text{ g}$$

Elevator Gust Load =
$$\Delta n - \frac{\Delta T}{GW} = 0.11 g$$

Case 2.
$$\Delta n = 0.98 \text{ g}; \frac{\Delta T}{GW} = 0.93 \text{ g}$$

Elevator Gust Load = 0.05 g

Rotors with 2, 3, and 4 blades were investigated (Appendix IV). Beyond the differing dynamic design requirements, however, the number of rotor blades has little effect.

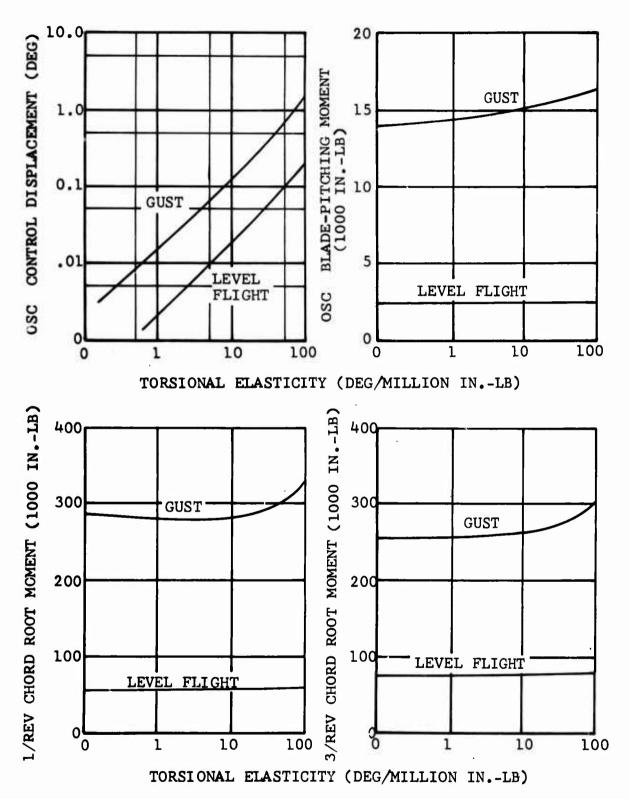


Figure 69. Effect of Control-System Flexibility on Oscillatory Rotor Loads for Level Flight and for 50-Ft/Sec Sine-Squared Vertical Gust.

A number of influences, such as the effect on tail-rotor behavior and the rolling and yawing that result from a gust, have not been investigated in detail. In general, however, these effects were found to play an insignificant role in the gust design-load problem. The effect of rpm changes was not investigated either, since it was assumed that a governor would hold the rpm within 2%. In governor open-loop mode, significant effects due to rpm variations may be expected.

SYNTHESIS OF RESULTS

In the previous section, Discussion of Results, the effects of various parameters on gust response were briefly evaluated. For a more complete presentation of the results, the reader is referred to Appendixes II and III, which give a listing of the most important parameters and findings of this study.

As previously discussed (see Introduction), the present military requirements for gust-load evaluation (MIL-S-8698) are inadequate. One of the principal objectives of this study was to derive new and relatively simple design rules which would enable the designer to determine gust loads for the aircraft without the benefit of an elaborate computing process. In order to accomplish this objective, it was originally planned to investigate the importance of certain parameters in the evaluation of the gust-alleviation factor Kg. This plan produced results from a large number (303) of cases. However, the attempt to determine Kg as a function of a particular parameter left many exceptions to be explained. Eventually, the idea of a gust factor was dropped in favor of a formula which would give directly the rotor-thrust increment due to a gust. The problems associated with attempting to determine gust-load functions are discussed below for each of the three rotorcraft configurations considered in this study. Finally, the development of the empirical formula is given.

GUST-ALLEVIATION FACTORS FOR THE PURE SINGLE-ROTOR HELICOPTER

The gust factor for the pure single-rotor helicopter seems to be affected very little by variation of rotor parameters. This is probably best illustrated by the histogram in Figure 28 (page 71). A Kg value of .6 would cover 95% of all pure single-rotor helicopter cases, while the majority of the cases have a Kg between .50 and .55. Figure 41 (page 89) shows that disc loading has only a small effect on Kg as determined by results of this study. Values of Kg are slightly lower for the higher disc loadings in some cases. The curve of Figure 2 (page 2) (from MIL-S-8698) shows an entirely different trend. The suggestion (8) to base Kg on a rotor-mass ratio in analogy with fixed-wing practice was also mentioned in the Introduction (see Figure 4, page 3). For the pure single-rotor helicopter cases, this approach resulted in Figure 70, in which the gust-factor function of Reference 8 is compared with the results of this study and the current criterion, MIL-S-8698. Obviously, no correlation is obtained; the gust-alleviation factor, Kg, of this study seems to be independent of the rotor-mass ratio. Variation of Kg with Lock number showed lowest Kg for highest Lock number for all rotor types and advance ratios calculated. However, the range of variation in Kg (about .15) is small compared with the change in Lock number (3.88). (See Table XI page 98).

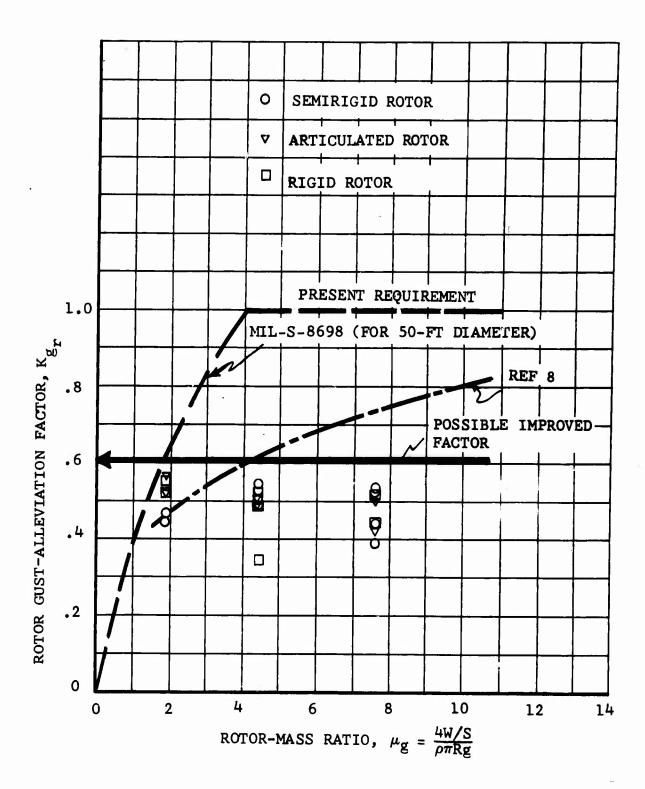


Figure 70. Rotor Gust-Alleviation Factor Versus Mass Ratio for Single-Rotor Helicopters - A Comparison With MIL-S-8698 and Reference 8.

Although several attempts were made to relate the gust factors to disc loading, Lock number, rotor—thrust coefficient, etc., no satisfactory solution was obtained. It is believed that effects such as in-plane rotor forces, elevator loads, control positions, and rotor—plane attitude at the initial trim position, as well as rotor—blade dynamic forces and deflections, are all influential factors.

The results for the pure single-rotor helicopter, regardless of the type of rotor, suggest a simple design rule which appears to be superior to the old requirements, yet conservative for all cases investigated. Such a rule could be formulated as follows:

Gust loads on pure single-rotor helicopters due to a 50-ft/sec sine-squared gust can be determined by applying a gust-alleviation factor of $K_g = .6$ to the gust load computed due to a 50-ft/sec sudden gust.

GUST-ALLEVIATION FACTORS FOR THE PURE TANDEM HELICOPTER

The tandem helicopter's inherent capacity of a large cg range is directly associated with the gust-response factors which can be expected. During the penetration of a sine-squared gust, the thrust buildup on the forward rotor precedes that of the aft rotor, thereby furnishing a nose-up pitching moment proportional to the distance aft to the cg. Thus for an aftcg condition, the pitch displacement from trim attitude adds a significant component of the forward speed to the maximum gust velocity. For the forward-cg cases, the pitch displacement is slight, and gust response fits the pattern established for the other configurations. An examination of the results showed that the maximum gust factor would be approximately .58 if the effect of pitch displacement is removed. This factor is compatible with the simple design rule for the pure singlerotor helicopter. A comparable design rule for the tandem helicopter, however, should include the effect of pitch dis-placement as related to distance between rotors, fuselage pitching inertia, and amount of rotor overlap. Variations of these parameters were not investigated by this study.

GUST-ALLEVIATION FACTORS FOR THE COMPOUND HELICOPTER

The compound helicopter presents a more complex situation than does the pure helicopter because of the load sharing between the rotor and the wing. It can be seen in Figures 29 and 30 that the gust factors, K_{gr} , on the rotor are smaller than 0.7. Most of the gust factors for the wing, K_{gw} , are found between 0.8 and 0.9, suggesting that the usual fixed-wing methods are a close approximation (a factor of 0.8 to 0.85 is found for the airplane mode of the tilt-rotor configurations, where the wing carries the major part of the load).

Although the results shown in Figures 35, 49, and 58 (pages 78, 95 and 106) indicate that forward speed does have some effect, the variation in Kg is small (about .10) over a speed range from 200 to 350 knots. Available data have been plotted in Figure 71 for both the rotor- and wing-gust factors. In Figure 71(a), Kg for pure helicopters, based on data from this study and from Figure 16 of Reference 8, is included for comparison with the compound helicopter cases. Some pure fixed-wing airplane cases are included in the wing-gust factor plot (Figure 71(b)). It can be seen that considerable spread of the results, which does not appear to be a simple function of major parameters such as disc loading or rotor thrust coefficient, is possible. The highest values of Kgr occur at a disc loading of 7 lb/sq ft, with $CT/\sigma = .05$. The lower values of rotor gust-load factor are from cases with both lower and higher disc loadings, and with C_T/σ values of both .02 and .05.

For design purposes, it appears that $K_{g_r}=0.7$ is a conservative factor for the compound configuration. This value is slightly higher than that suggested for the pure helicopter, because the rotor of a compound helicopter is usually unloaded, entirely or partly by the wing, in steady, level flight. The rotor's capability to assume a share of the gust load is, therefore, usually greater.

The wing-gust factor, K_{g_W} , shows a clearer trend than does the rotor-gust factor. Increased gust-load capability of the rotor (Δn) is primarily a function of C_T/σ (see Figure 43, page 91). If the rotor takes a major share of the total load (see Figure 58, page 106), the upward acceleration of the wing is larger for a compound than for a fixed-wing aircraft. One must therefore expect to see a considerable upward velocity of the aircraft at the time the maximum wing load develops. This upward motion reduces the wing's angle of attack and reduces its gust factor. The bar graph in Figure 72 illustrates this effect by sampling K_{g_W} for the two values of C_T/σ ; for comparison the case of a fixed-wing airplane is also shown.

It thus appears that a reduction of the fixed-wing-gust factor K_{g_W} is justified for rotors with low thrust coefficients. The exact determination of this reduction, however, remains a subject for further study.

EMPIRICAL FORMULA FOR ROTOR-GUST LOAD

In general, the use of an alleviation factor for the rotor is not altogether satisfactory. As an alternative to determining the actual gust load by applying a gust factor to the calculation for a sudden gust, gust loads on the rotor may be considered directly for the sine-squared gust cases. If in this way a reasonably simple rule can be found, the complex

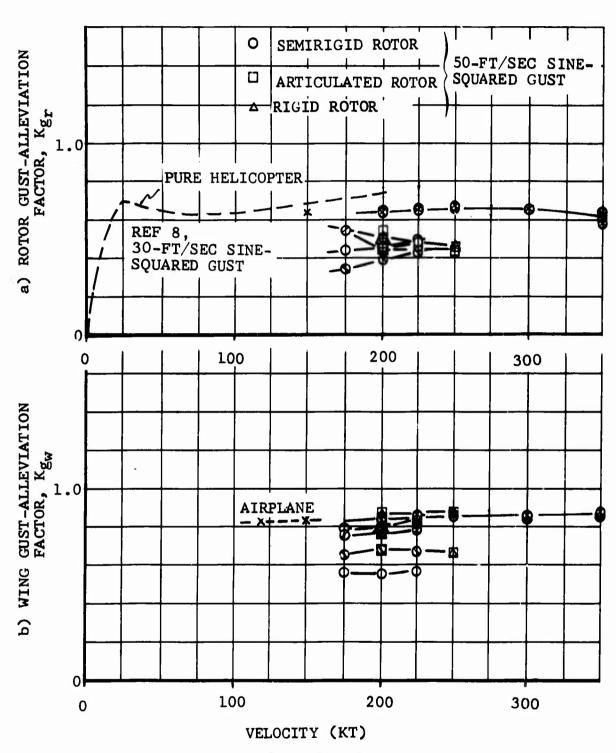
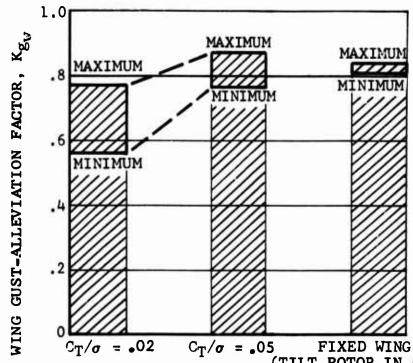


Figure 71. Rotor Gust- and Wing Gust-Alleviation Factors
Versus Forward Speed for Compound Helicopters
at High Speed and for Pure Helicopters and
Airplanes at Low Speed.



ROTOR THRUST COEFFICIENT-SOLIDITY RATIO (TILT ROTOR IN AIRPLANE MODE)

Figure 72. Effect of Rotor Thrust Coefficient-Solidity Ratio on Wing Gust-Alleviation Factor.

calculation of the sudden-gust case will be eliminated, as will the uncertainties in the actual values for the rotor-gust factor.

Inspection of the results for pure helicopters (Appendix III) shows that the disc loading has only a minor effect on the value of Δn , but that the rotor thrust coefficient-solidity ratio, CT/σ , has considerable influence. This trend is verified in Figure 73, where the rotor gust-load ratio, $\Delta T/T$ hover, is plotted versus CT/σ for all cases of this study. For the winged helicopter (tilt-rotor cases with the rotors lifting), only the thrust increase of the rotor is included.

Figure 73 presents some interesting facts:

At high values of $C_{\rm T}/\sigma$ the capability of the rotor to carry additional thrust disappears. The maximum value of $C_{\rm T}/\sigma$ for the pure helicopter seems to be close to .15, which is in agreement with data presented in References 6 and 8, where a limit value of about .16 is indicated.

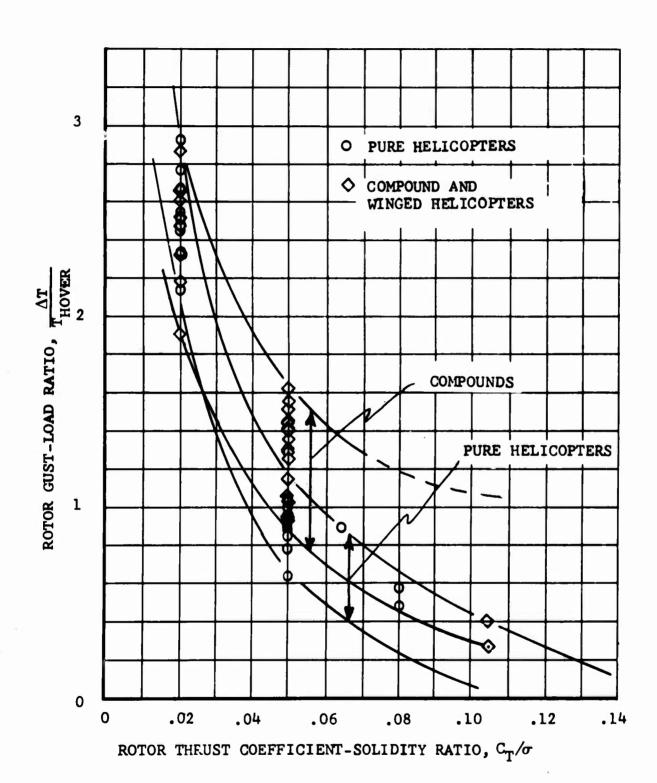


Figure 73. Rotor Gust-Load Ratio Versus Rotor Thrust Coefficient-Solidity Ratio.

- For compound-helicopter rotors, $\Delta T/T_{\rm hover}$ approaches unity for high values of C_T/σ . This condition is possible if the wing unloads the rotor completely in trimmed flight prior to the gust.

This discussion suggests that $\Delta T/T_{hover}$ probably can be approximated by a simple function of C_T/σ and L_w (wing lift prior to the gust). Figure 74 shows $\Delta T/T_{hover}$ versus $\Delta T/T_{hover}$. where

 $\Delta T/T_{\mbox{hover}_{\mbox{empirical}}}$, where

$$\frac{\Delta T}{T_{\text{hover}}} = \frac{0.057}{(C_{\text{T}}/\sigma)_{\text{hover}}} + 0.85 \frac{L_{\text{w}}}{T_{\text{hover}}} - 0.3 \quad (19)$$

The correlation is surprisingly good, considering the wide variation of disc loading, tip speed, forward speed, and configuration, and the fact that details such as gradual penetration, sine-squared gusts, and nonsteady aerodynamics are included. Only at the high values of $\Delta T/T_{\rm hover}$ do the data points show significant scatter. Attempts to explain and further reduce the scatter have not yet been successful. If the constant -0.3 were changed to -0.2 for semirigid rotors and to -0.1 for rigid and articulated rotors, all cases would be calculated conservatively.

The expression can be readily understood to be related to the mean-blade-lift coefficient and the maximum-lift coefficient. Approximately, $C_{\rm T}/\sigma$ = .1 $C_{\rm L}$ and $\Delta C_{\rm L}$ due to a gust equals

$$(dC_L/d\alpha)$$
 ' $(V_g/\frac{3}{4}\Omega R)$. Assume $dC_L/d\alpha$ = 6, V_g = 50 ft/sec, ΩR = 667 ft/sec, then ΔC_L ≈ 6 (50/500) = .6

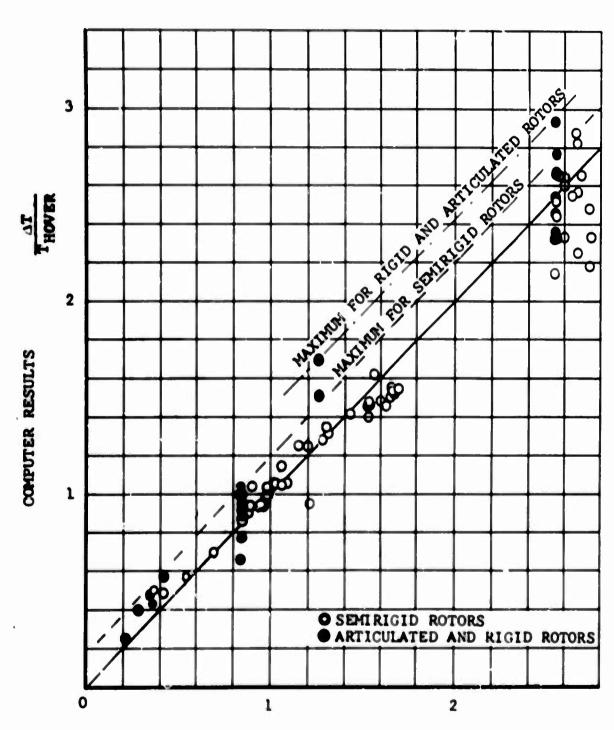
The first term can be approximated as follows:

$$\frac{\left(C_{T}/\sigma\right) \text{ due to gust}}{\left(C_{T}/\sigma\right)_{\text{hover}}} = \frac{.1\Delta C_{L}}{\left(C_{T}/\sigma\right)_{\text{hover}}} = \frac{.06}{\left(C_{T}/\sigma\right)_{\text{hover}}}$$
(20)

The second term includes the unloading of the rotor by wing lif , $L_{\rm W}$. The factor 0.85 is possibly an efficiency factor.

The constant determines the maximum $\mathbf{C}_{\mathrm{T}}/\sigma$ that is available for additional rotor lift.

The fact that the rigid and articulated rotors show a higher value for $\Delta T/T_{\mbox{hover}}$ is probably due to the hub moment causing some nose-up fuselage motion that causes additional lift increase. This is similar to the effect described in connection with tandem-rotor helicopters.



EMPIRICAL RESULTS $\frac{\Delta T}{T_{\text{HOVER}}}$

Figure 74. Correlation Between Computer Results and Empirical Equation for Rotor Gust-Load Ratio (Sine-Squared 50-Ft/Sec Gust).

From the standpoint of rotor design, the above expression can be most convenient to the designer. By simply determining the hovering $C_{\rm T}/\sigma$ and the minimum wing lift in steady flight, the rotor-gust load can readily be calculated. The wing- and elevator-gust loads can be found by conventional means and then reduced by a small amount (see Figure 72). The total gust load, then, is determined by summing the rotor-, wing-, and elevator-gust loads.

It is recommended that this approach, which is suitable for all the VTOL concepts and rotor types investigated in this study, be further developed and be given serious consideration for use in rotary-wing design requirements.

Several attempts were made to find a meaningful relationship for the computed rotor bending moments. Figure 75 shows the oscillatory beamwise moments at the blade root, in the form of a ratio of maximum values during the gust to the trim values, plotted against the ratio of thrust increase to hover thrust. No particular trend is discernible. During the selection of the rotor structural parameters, it was recognized that each rotor would have to be "designed" free of resonant conditions over an appreciable range of both rpm and collective pitch, as specified by the parameter variations in each group of cases. The possible variation in dynamic characteristics of a rotor, even for a specific aircraft configuration, cannot be represented by a simple rule that would relieve the designers of any of their present functions.

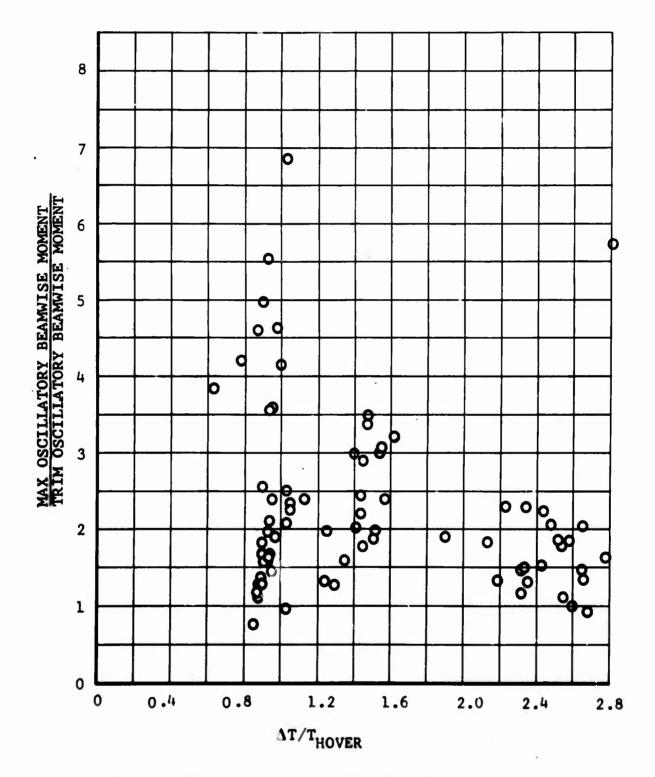


Figure 75. Beamwise Oscillatory Hub Bending Moment Ratio Versus Normalized Thrust Increment During Gust.

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APPENDIX I. SAMPLE OUTPUT FROM FLIGHT-SIMULATION PROGRAM

				" MASS MOMENTS	OF INERTIA			.000	0.0	99.000 C.P. LOCATION		0.0	0.0		2	CHORD		- 33, 000 DETTA 3	-	199-0	0.0		•	0.0	0.0			0.0		0.251	0.0	0.0	0.00	0.0	0.107	0.500 0.500
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M COL-11 MALYSIS		404-STEADY		0.0	0.0	0.00		0.0	001-1	1192.000	0.0	0.0	0.0		27.000		0.100	0.0	0.0	146.0	1.660		0.0	0.0	?•°°	•	0.0	000		014.0	0.0	000	•		0.149	0.098
BELL MELICOPTER 18M 3607 PROGRAM COL-1 MELICOPTER RIGIO BODY DYNAMICS ANALYSIS COMPILED 1-21-67	ASTIC FEEDSACK LOOP ACTIVE WITH FEEDSACK FACTOR .	SUARED GUST N		0.0				0.0	0 0	20.000	0.0	0.0	000		~	2.000	90.00	0.0			0.505		0.0	0.0	0,4		0.0	000	\$ 10	4.250	0.500	0.700		0	0.220	0.0
LICOPTER 18 ER RIGIO BOG COMPILEO	TIKER FUNC	SINE-SQUARED CH. # 8500. V	l,	0.0	17.500	0.00		14.000	1.200	20.000	2.420	0.0	000			1.250	1.300	0	0.0	0.000	0.505		0.0	0.0	0.0		0.0	000	7	12.000	1.062	1.300	2000	0	0.594	000
9ELL HEL ICOPT	ASTIC FEEDSAG	1160601	FLAGE GROUP		0.134	00	WING GROUP	0	000	0.0	0.0	0.0	00	M BOTOR CABUP	20	2.750	1.270	0.107	152.620	2.860	0.505	PROP GROUP	0.0	0.0	•	0	0.0	90	L ROTOR GROUP	20.000	1.500	1.270	[0.107	116.270	1.476	0.010
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0.927 0.0 0.008 23.000	0.0 0.0 0.0 0.0 0.0	LS GROUP 4.500 -13.200 -10.800	0.00 -7.000 0.0	[1157.000] 55.000 2.000 8103.000	163,000	1002 40.000 9.0
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AERGELASTIC FEEDBACK LOOP ACTIVE WITH FEEDBACK FACTOR = 0.100 WAGNER AND BUETTIKER FUNCTIONS ACTIVE ON TIME STEP 1

DELTA 3 = -30 SINE-SQUARED GUST NOW-STEADY GW. = 8500. V = 150. MODEL GUST STUDY 1090313

HELICOPTER IS IN STABLE CONDITION.

MAIN ROTOR COLLECTIVE PITCH	(DEGREES)	16.260	16.260 TAIL ROTOR COLLECTIVE PITCH	PITCH	(DEGREES)	2.289
F+A CYC PITCH	(DEGREES)	1.068	F+A CYC	F+A CYC PITCH	(DEGREES)	0.0
LAT CYCLIC PITCH	(DEGREES)	-1.336	LAT CYCLIC PITCH	PITCH	(DEGREES)	0.0
F+A FLAPPING	(DEGREES)	5.440	F+A FLAPPING	5NG	(DEGREES)	1.427
LAT FLAPPING	(DEGREES)	0.412	LAT FLAPPING	ING	(DEGREES)	0.585
THRUST	(188)	1139.107	THRUST		(587)	166*592
H-FORCE	(182)	638.573	H-FORCE		(182)	9.965
Y-FORCE	(182)	-103.235	Y-F JRCE		(188)	2.350
HORSEPOWER		931.625	HORSEPONER			18.045
z d x		324.360	M G M			1656.598
MAST TILT ANGLE	(DEGREES)	0.0	MAST TILT ANGLE	ANGL E	(DEGREES)	0.0
ELEVATUR ANGLE OF ATTACK	(DEGREES)	0.688	0.688 FIN ANGLE OF ATTACK	•	(OFGREES)	3.909
BOOY Z-FORCE (+DUWN)	(188)	-40.612	800Y Y-FORCE (+RIGHT)	2 3	(182)	300.254
BUDY X-FORCE (+FWD)	(1881)	-15.643	- HOOY X-FORCE (+FWO)	101	(188)	-22.031
FUSELAGE EULER ANGLE YAM	(DEGREES)	0.0	WING ANGLE OF ATTACK		(DEGREES)	4.385
PITCH	(DEGREES)	-7.097	800Y 2-FORCE (+0JWN)	(NACC	(587)	-827-160
ROLL	OEGREES	-1.972	BODY X-FORCE (+FWD)	(0)	(18)	-161.030
HELICOPTER GROSS WEIGHT	(597)	8500.000	8500.000 AUXILIARY PROPULSION.LEFT SIDE ILBS!	LEFT SIC)E (1.85)	0.0
FORWAND SPEED	(KNOTS)	150.000		RIGHT STOEILBS)	06(185)	0.0
RATE OF CLIMB	(FT/SEC)	0.0				
ENGINE RPM		6600.000				
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PITCH	-913.89 -146.68 2799.61 1:.66 -109.16 -68.16
MC#.	110
YAW	-659.62 -4667.80 257.21 38.03 -13.43
JACE	1
Z-FORCI	435.16 -28C.41 21669.92 -71.13 318.66
Y-FORCE	-1387.50 -438.67 -42.97 - -12.39 -13.05
X-FCRCE	-93.33 819.43 819.43 -61.60 -9.34
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רטני	THRUST	PATH PLAN	רטנע	THRUST	BODY REFERENCE	-2.491 -0.275	FIXED REFERENCE	176.9	FUSELAGE ATKY -0.313 ATKP -7.230	000	FORCES AND MOMENTS	L.PRCP	0.0	0.0			
OMEGA 0.3 44.359	A15 -1.367 815 -0.387	TAIL ROTOR FIP	0.0 0.0 39.550	1-419 THR	800V	0 -3.610 -0.497	FIXED A	DISTANCE ALTITUDE	RIGHT BING 7.343 FT 513.6 AG 87.8	THRUST(L/C) THRUST(R)	FORCES AN	R.PROP L.	0.0	9 6	0	0.0	0.0
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1210952	180	•	<u>:</u>	-:	2.	2.	2.		3.	3.	2	2.	5.	:	-0-	7 -	-3.	- 4.	-6	-1:-1	1-6-	-0.0007	
-27		•	-:	۶.	2.	÷	•	•	•	2	5	2	,	2.	٥.	2.	5	5	2	•		6	
		-:	-	۲.	3	3.	;	4.	5.	5.	5.	•	•	•	7.	7.	7.	'n	•		.21	GREES 0.0009	
Z	9	•	•	•	•	•	•	•	•	-:	:		-	-	:	2.	2.	2.	2.	3.	3	DEGREES 0.000	
1090313 = IPSN		-1-	.5.	÷	•	.5	.5.	•	•		٠.					.6.	•	. 9.	Ģ	•	.7.	INS,	
. 611		-1:																				CTIONS 3.0015	
040		· 0																				EFLE	
-	BEAM	1	1	•	•	•	•	1	•	•	1	1	ŀ	•	•	1						CONTROL DEFLECTIONS, 0.0015	
	STA		7	~	4	2	•	_	ю	0	2	= :	77	2	14	51	9	17	9	61	70	CONT	

						-22.	-21.	•				3131313.				7	-1-	.6.						
	-28.	-27.	-25.	-23.	-22.	••		-19.	-17.	-15.		-12121212131313131313.		-10.	-6-	•		-9-	-5.	ţ	-3.	-3.	-2.	
۰						-20.	-18.	-17.	-15.	:	-1414.	-1212	-11:-11:	-10-			-1.							YGUSTF 0.008
FWO	-31.	-29.	-27.	-25.	-23.	-21.	-1819.	-171717.	-151615.	71 71 7	-14141414.	212.	-11111111.	-10910-			-16.	-5-	Ť	-3.	-5.	-5.	7	AFT HGUSTF -0.032
TOR DISC		-27.	-25.	-23.	-22.	-50.	7		9	.15	1	-13131313131312121212.	7	-10.			•	-9-	-5-	÷	-3.	-3.		нGUSTE -0.283
GUST VELOCITIES ON ROTOR DISC	-28.	•						8	-17.			131313			.61	-7.							-2.	HGUST
JST VELOCI							-20-					1313					-7-							VGUSTE -2.232
ō						-22.						-						-6-						VGUSTW -11.922

			Ü
1090313	KWH = -27540121	16	0.675
_	-21		94
*			TIME
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Ş		20	
M C02,		PROD.540 ROTOR, 20 LB MID WT. 35 LB TIP	
JGRA		240	
PRC		8	
BHC SYS/360-50 PROGRAM COZ, MCMENT SYNTHESIS		PR	
BHC			

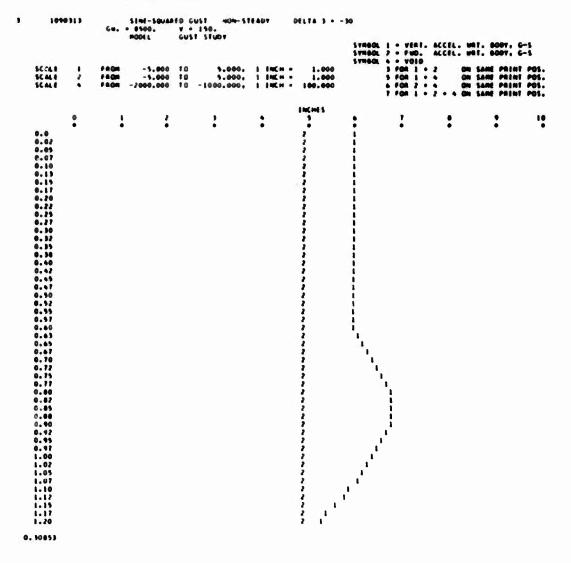
180 79219. 109642. 300 70 73026. 98408. 300
79219.
180
250
5956.
1421.

	LRS.	KNOTS	SQ.FT.	LBS.		DEG.	JEG.		LBS.	DEG.	FT.	FT.	
	8500.	150.	0.0	147.	379.	5.98	1.44	0160	642.	-8-3	10 0.17	SPAN166.73 FT.	
	GROSS MT.	FWD. SPEED	RAG AREA	DOWNLOAD	dH Y	AL FLAPPING 5.98 0	LAPPING	0- 40	+ FORCE	IPP ATTITUDE -8.3	CHOR	SPAN	
MARY	GROS	F.4D.	UR AG	OCH	ROTOR	ALF	91 F	INFL	F FO	100	LBS.	198	
NOS R											LIFT -1027. LBS.	-176.	
PARAMETER SUMMARY	ž	FT.	. N.			DEC.	DEG.	DEG.		FTRY	LIFT	DRAG	
	264. IN.	***	27.00	2.	324.	2.751	16.263	-10.002	. 2	TOB GEON	DATA	268	
	RADIUS	DIAMETER	CHORD	NO. BLADES	RUTON RP4	PRECUNE 2.751 D	RUOT COLL.	THIS! -10.002 DEG.	YU. HUB SEG.	TEETERING P	MING DATA	CL 3.4	
(COMPILEO)													

VERTICAL MUE SHEAR = 1656. LBS.(TOTAL)
BEAN CHURD
HUB VIBRATION
O.O VERT. 1/REV O. 84557.
(NON-ROTATING COORDINATES) O.O F/A 2/REV 14469.
(INCHES, SINGLE AMPLITUDE) O.O LAT. 3/REV O. 53002.

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HELICOPTER BIG 3607 PROGRAM (81-1) HELICOPTER BIGID BODY DYNAMICS ANALYSIS COMPILED 1-71-67



APPENDIX II. CASE DESCRIPTIVE INFORMATION AND TRIM DATA

TABLE XIV. CASE DESCRIPTIVE INFORMATION AND TRIM DATA, PURE SINGLE-ROTOR HELICOPTER												
Main Rotor Data												
Case No.	Vel (Kt)	Gust Type	Disc Ldg	C _T M _{ti}	Rad p (Ft)	Chord (In.)		Mass Ratio	Lock No.			
		S		gid Roto		ides)						
ı	200	SUDV	7.0	.05 .80	26.1	35.6	234.	4.47	8.31			
2	200	ssqv		1 1					•			
3	225	SUDV										
4	225	ssqv										
5	200	SUDV		.85								
6	200	ssqv			21		- 1					
7	225	SUDV						ŀ				
8	225	ssqv	1									
9	200	SUDV		.90								
10	200	ssqv										
11	225	SUDV					!					
12	225	ssqv							1			
13	200	SUDV		.95								
14	200	ssqv										
15	225	SUDV				İ						
16	225	ssqv		1 1	1	1	1					
17	200	SUDV	4.0	.02 .90	34.5	67.1	177.	1.93	8.42			
18	200	ssqv			1	1	1					
19	175	SUDV										
20	175	ssqv		1		1						
21	200	SUDV		.05		26.9			10.27			
22	200	ssqv										
23	225	SUDV				j						
24	225	ssqv		1	ļ	\	\	1	1			

Trim Data											
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	HPR (Hp)	Eff Drag Area (Ft2)	Fuse Pitch (Deg)				
1	19.7	12.8	- 7.8	15400.	2120.	10.4	- 4.4				
2	19.7	12.8	- 7.8	15400.	2120.	10.4	- 4.4				
3	24.1	16.8	-10.0	15500.	2990.	10.4	- 6.6				
4	24.1	16.8	-10.0	15500.	2990.	10.4	- 6.6				
5	19.9	13.0	- 8.1	15400.	2240.	10.5	- 4.5				
6	19.9	13.0	- 8.1	15400.	2240.	10.5	- 4.5				
7	24.5	17.2	-11.1	15500.	3180.	10.5	- 6.8				
8	24.5	17.2	-11.1	15500.	3180.	10.5	- 6.8				
9	20.5	13.7	- 8.8	15400.	2590.	10.6	- 4.8				
10	20.5	13.7	- 8.8	15400.	2590.	10.6	- 4.8				
11	25.4	18.2	-12.0	15500.	3730.	10.6	- 7.2				
12	25.4	18.2	-12.0	15500.	3730.	10.6	- 7.2				
13	21.6	15.1	-10.2	15300.	3310.	11.4	- 5.3				
14	21.6	15.1	-10.2	15300.	3310.	11.4	- 5.3				
15	27.6	20.5	-13.8	15400.	4940.	10.9	-8.1				
16	27.6	20.5	-13.8	15400.	4940.	10.9	- 8.1				
17	24.3	19.0	-18.2	14900.	5590.	12.0	- 7.3				
18	24.3	19.0	-18.2	14900.	5590.	12.0	- 7.3				
19	19.0	14.0	-13.1	15000.	3703.	12.1	- 4.5				
20	19.0	14.0	-13.1	15000.	3703.	12.1	- 4.5				
21	20.7	13.8	- 9.3	15300.	2600.	10.6	- 5.1				
22	20.7	13.8	- 9.3	15300.	2600.	10.6	- 5.1				
23	27.8	20.1	-12.9	15400.	4440.	10.6	- 8.0				
24	27.8	20.1	-12.9	15400.	4440.	10.6	- 8.0				

TABLE XIV - Continued (PURE SINGLE-ROTOR HELICOPTER) Main Rotor Data Case Vel Gust Disc C_T Chord Rad M Mass Lock tip (Ft) No. (Kt) (In.) RPM Type Ldg Ratio No. Semirigid Rotor (4 Blades) 25 200 SUDV 10.0 .02 .90 21.8 106.2 280 7.64 5.05 26 200 SSQV 27 175 **SUDV** 28 175 SSQV .05 29 200 SUDV 42.5 7.10 30 200 SSQV 31 225 **SUDV** 32 225 SSQV 33 200 **RMPV** ס.ל 26.1 35.6 234 4.47 8.31 34 225 **RMPV** 35 200 SUDH 36 200 SSQH 37 225 SUDH 38 225 SSQH Articulated Rotor (4 Blades) 39 200 SUDV 4.0 .02 .90 34.5 67.1 177 8.42 40 SSQV .02 67.1 8.42 41 **SUDV** .05 26.9 10.27 .05 42 SSQV 26.9 10.27 43 SUDV 7.0 .02 26.1 89.0 234 4.47 6.58 SSQV 44 .02 89.0 6.58 45 SUDV .05 35.6 8.31 46 SSQV .05 35.6 8.31

	Trim Data									
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	HPR (Hp)	Eff Drag Area (Ft ²)	Fuse Pitch (Deg)			
No.	(Deg)	(Deg)	(beg)	(LU)	(IID)	(11-)	(Deg)			
25	23.0	18.1	-16.2	15100.	4720.	11.1	- 6.3			
26	23.0	18.1	-16.2	15100.	4720.	11.1	- 6.3			
27	18.5	17.5	-12.0	.300دَ1	3570.	10.2	2			
28	18.5	17.5	-12.0	15300.	3570.	10.2	2			
29	20.5	13.9	- 8.4	15400.	2620.	10.6	- 4.5			
30	20.5	13.9	- 8.4	15400.	2620.	10.6	- 4.5			
31	24.9	17.8	-11.3	15500.	3580.	10.1	- 6.8			
32	24.9	17.8	-11.3	15500.	3580.	10.1	- 6.8			
33	20.5	13.7	- 8.8	15400.	2590.	10.6	- 4.8			
34	25.4	18.2	-12.0	15500	3730.	10.6	- 7.2			
35	20.5	13.7	- 8.8	15400.	2590.	10.0	- 4.8			
36	20.5	13.7	- 8.8	15400.	2590.	10.0	- 4.8			
37	25.4	18.2	-12.0	15500.	3730.	10.7	- 7.2			
38	25.4	18.2	-12.0	15500.	3730.	10.7	- 7.2			
39	24.1	13.6	-17.1	16500.	5640.	11.9	-13.6			
40	24.1	13.6	-17.1	16500.	5640.	11.9	-13.6			
41	20.6	12.5	- 9.1	15700.	2620.	10.8	- 6.6			
42	20.6	12.5	- 9.1	15700.	2620.	10.8	- 6.6			
43	23.1	13.2	-15.7	16600.	5200.	11.1	-12.2			
44	23.1	13.2	-15.7	16600.	5200.	11.1	-12.2			
45	20.4	12.4	-16.7	15800.	2620.	10.6	- 6.2			
46	20.4	12.4	-16.7	15800.	2620.	10.6	- 6.2			

TABLE XIV - Continued (FURE SINGLE-ROTOR HELICOPTER) Main Rotor Data Disc CT Vel Gust Case M Rad Chord Mass Lock tip No. (Kt) Type Ldg o (Ft) (In.) RPM Ratio No. Articulated Rotor (4 Blades) SUDV 10.0 .02 .90 21.8 106.2 280 7.64 11.4 47 200 SSQV .02 106.2 11.4 48 SUDV 42.5 10.6 49 .05 42.5 50 10.6 SSQV .05 Rigid Rotor (4 Blades) SUDV 4.0 .02 .90 34.5 67.1 177 1.93 8.4 200 51 .02 67.1 8.4 52 SSQV .05 26.9 10.3 53 **SUDV** 10.3 54 SSQV .05 26.9 7.0 .02 89.0 234 4.47 26.1 6.6 55 SUDV 89.0 6.6 .02 SSQV 56 35.6 8.3 .05 57 SUDV .05 35.6 8.3 58 SSQV 7.64 21.8 106.2 280 5.0 10.0 .02 59 SUDV 106.2 5.0 SSQV .02 60 42.5 7.1 61 SUDV .05 42.5 7.1 SSQV .05 62 Articulated Rotor (4 Blades) 89.0 234 7.0 .02 .90 26.1 4.47 6.6 225 63 **SUDV** 89.0 6.6 .02 64 SSQV 35.6 8.3 .05 65 SUDV 35.6 8.3 SSQV .05 66

		Trim Data									
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	HPR (Hp)	Eff Drag Area (Ft ²)	Fuse Pitch (Deg)				
47	22.6	12.7	-15.2	16700.	4960.	11.4	-11.9				
48	22.6	12.7	-15.2	16700.	4960.	11.4	-11.9				
49	20.5	12.5	- 8.2	15800.	2670.	10.6	- 5.8				
50	20.5	12.5	- 8.2	15800.	2670.	10.6	- 5.8				
51	24.1	13.6	-17.1	16500.	5640.	11.2	-13.6				
52	24.1	13.6	-17.1	16500.	5640.	11.2	-13.6				
53	20.6	12.5	- 8.1	15700.	2620.	10.7	- 6.6				
54	20.6	12.5	- 8.1	15700.	2620.	10.7	- 6.6				
55	23.1	13.2	-15.7	16600.	5200.	11.2	-12.2				
56	23.1	13.2	-15.7	16600.	5200.	11.2	-12.2				
57	20.4	12.4	- 8.6	15800.	2620.	10.6	- 6.2				
58	20.4	12.4	- 8.6	15800.	2620.	10.6	- 6.2				
59	22.6	12.7	-15.2	16600.	4960.	11.4	-11.9				
60	22.6	12.7	-15.2	16600.	4960.	11.4	-11.9				
61	20.5	12.5	- 8.2	15800.	2670.	10.6	- 5.8				
62	20.5	12.5	- 8.2	15800.	2670.	10.6	- 5.8				
63	30.3	19.0	-20.4	17100.	8420.	9.4	-15.5				
64	30.3	19.0	-20.4	17100.	8420.	9.4	-15.5				
65	25.3	16.9	-20.1	16000.	3780.	10.6	- 8.7				
66	25.3	16.9	-20.1	16000.	3780.	10.6	- 8.7				

TABLE XIV - Continued

(PURE SINGLE-ROTOR HELICOPTER)

			Main Rotor Data								
Case	Vel	Gust	Disc	C _T	М	Rad	Chord		Mass	Lock	
No.	(Kt)	Type	Ldg	<u> न</u>	tip	(Ft)	(In.)	RPM	Ratio	No.	
			Rig	id R	lotor (4 Blac	ies)				
67	225	SUDV	7.0	.02	.90	26.1	89.0	234	4.47	6.6	
68		ssqv		.02			89.0	ľ	ļ	6.6	
69		SUDV		.05			35.6			8.3	
70	†	ssqv	1	.05	+	+	35.6	↓	↓	8.3	
			Semir	igid	Rotor	(2 B1	ades)				
217	200	SUDV	7.0	.08	.9	26.1	43.8	234	4.47	10.3	
218	200	SSQV	7.0	.08	.9	26.1	43.8	234	4.47	10.3	
			Rig	id F	Rotor	(2 Bla	des)				
219	200	SUDV	7.0	.08	.9	26.1	43.8	234	4.47	10.3	
220	200	ssqv	7.0	.08	.9	26.1	43.8	234	4.47	10.3	
		A	rticul	Late	Roto	r (3 B	lades)				
221	200	SUDV	7.0	.08	.9	26.1	28.1	234	4.47	10.3	
222	200	ssqv	7.0	.08	.9	26.1	28.1	234	4.47	10.3	
				_		(4 Bl	-				
235	200	ssqv	7.0	.05	.85	26.1	35.6	234	4.47	8.3	
2 36								ŀ			
237	1	1								+	
243	150	SUDV			.1					8.3	
244	1.50	SSQV					÷				
245	100	SUDV									
246	100	SSQV	П								
247	200	ssqv	+	+	+	+	+	<u> </u>	<u> </u>	•	

		Trim Data										
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	HPR (Hp)	Eff Drag Area (Ft ²)	Fuse Pitch (Deg)					
67	30.3	19.0	-20.5	17100.	8440.	9.6	-15.5					
68	30.3	19.0	-20.5	17100.	8440.	9.6	-15.5					
69	25.3	17.0	-11.7	16000.	3820.	10.6	- 8.7					
70	25.3	17.0	-11.7	16000.	3820.	10.6	- 8.7					
217	22.4	16.0	- 6.4	15400.	2240.	10.0	- 3.5					
218	22.4	16.0	- 6.4	15400.	2240.	10.0	- 3.5					
219	23.9	16.9	- 6.1	15500.	2670.	10.0	- 4.4					
220	23.9	16.9	- 6.1	15500.	2670.	10.0	- 4.4					
221	24.4	17.2	- 6.1	15600.	2760.	10.0	- 4.7					
222	24.4	17.2	- 6.1	15600.	2760.	10.0	- 4.7					
235	19.9	13.0	- 8.0	15400.	2260.	10.6	- 4.8					
236	20.5	6.2	- 9.2	14700.	2700.	10.4	- 7.9					
237	19.9	13.0	- 8.0	15400.	2260.	10.5	- 4.5					
243	14.9	8.2	- 4.3	15200.	1300.	10.7	- 1.6					
244	14.9	8.2	- 4.3	15200.	1300	10.7	- 1.6					
245	12.9	5.6	- 2.1	15100.	970.	11.9	.2					
246	12.9	5.6	- 2.1	15100.	970.	11.9	.2					
247	19.9	13.1	- 8.1	15400.	2260.	10.5	- 4.5					

TABLE XIV - Continued

(PURE SINGLE-ROTOR HELICOPTER)

			<u>. </u>			Main	Rotor	Data		
Case No.	Vel (Kt)	Gust Typ e	Disc Ldg	$\frac{C_{\mathrm{T}}}{\sigma}$	M tip	Rad (Ft)	Chord (In.)		Mass Ratio	Lock No.
			Semiri	igid	Rotor	(4 Bla	ades)			
248	200			_				234	4.47	8.31
249		SUDV	ľ		.85					
263		SUDL			.90	i	- 1			
264	5	SSQL	+	\rightarrow	.90	+	ŧ	:∳	+	+
			Rig	id Ro	tor (+ Blad	es)			
265	120	SUDV	4.69	.037	.857	24.	21.	30 0	3.25	7.3
26 6		SSQV		Ì						
267		SUDV					- [ŀ	
268	†	SSQV	+	+	+	†	ŧ	ŧ	ŧ	+
						(4 Bla	des)			
270	120	SSQV	4.69	.037	.857	24	21.	300.	3.25	7.3
						(4 Bl				
278	150	SUDV	7.0	.05	•90	26.1	35.6	234	4.47	8.3
279	1	ssqv		1	1	1	ĺ		- 1	8.3
280		İ								5.6
281	†	+								4.4
282	175	SUDV						- 1		8.3
283	1 1	SSQV								8.3
284		1				i				5.6
285	+	+						ı		4.4
286	200	SUDV						- 2		8.3
287	1	ssov			1				٠	8.3
288							ı	11.7		5.6
289		•	+	•	+	1	1	3 6		4.4

		Trim Data										
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust	HPR (Hp)	Eff Drag Area (Ft ²)	Fuse Pitch (Deg)					
248	19.9	13.1	- 8.1	15400.	2260.	10.5	- 4.5					
249	20.4	6.1	-10.0	14700.	2370.	10.5	- 7.7					
263	20.3	14.6	- 8.6	15300.	2590.	10.5	- 4.7					
264	20.3	14.6	- 8.6	15300.	2590.	10.5	- 4.7					
265	11.0	2.6	- 6.9	9090.	940.	20.6	- 4.3					
266	1	2.6	1	9090.	1	20.6	- 4.3					
267	1	2.8		9070.		20.5	- 4.1					
268	ł	2.8	•	9070.	ŧ	20.5	- 4.1					
270	11.0	1.9	- 6.9	9040.	940.	20.6	- 4.9					
278	14.9	6.8	- 4.1	15400.	1310.	8.4	- 2.7					
279	ı	. 1	1	1	1	1	1					
280			. ↓									
281	+	į.	- 4.2	+	ŧ		+					
282	16.9	9.0	- 5.8	15600.	1740.		- 4.0					
283	- 1	9.0	- 5.8		1		- 4.0					
284		8.9	- 5.9				- 4.1					
285	+	8.9	- 5.9	+	ŧ	+	- 4.1					
286	20.3	12.3	- 8.4	15800.	2630.	8.3	- 6.0					
287	1	1	- 8.4		2630.		- 6.0					
288			- 8.5		2640.		- 6.1					
289	+	*	- 8.6	+	2640.	+	- 6.1					

TABLE XIV - Continued

(PURE SINGLE-ROTOR HELICOPTER)

					1111	Rotor	Data		
Case No.	Vel (Kt)	Gust Type	Disc Ldg	$\frac{C_{\mathrm{T}}}{\sigma}^{\mathrm{M}}$ tip	Rad (Ft)	Chord (In.)		Mass Ratio	Lock No.
		S	emiris	id Rotor	(4 Bla	ides)	•		
290	150	SUDV	7.0	.05 .90	26.1	35.6	234	4.47	8.3
291		ssqv	1	1 1	1	1	1	1	8.3
292		1							5.6
293	+	+							4.4
294	175	SUDV							8.3
295		SSQV	1						8.3
296									5.6
297	+	+						İ	4.4
298	200	SUDV							8.3
299		ssqv							8.3
300			1		1	1			5.6
301	†	+	Rigi	d Rotor (4 Blad	es)	*	*	4.4
3 02	150	SUDV	7.0	.05 .90	26.1	35.6	234	4.47	8.3
303		ssqv							8.3
304									5.6
305	+	*							4.4
306	175	SUDV	İ						8.3
3 07		SSQV						ŀ	8.3
308			ļ						5.6
309	†	*							4.4
310	200	SUDV							8.3
311		SSQV							8.3
312								1	5.6
313	1	*	*	7 7	1	7	•	•	4.4

				Trim I	Data		
Case	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)		HPR (Hp)	Eff Drag Area (Ft ²)	Fuse Pitch (Deg)
290	15.0	0 2	- 4.2	1.5200	1 200	0.5	1. 1.
291	13.0	0.3	- 4.2	15200.	1320. 1320.	8.5	- 1.4
292					1310.		
293	1	. ↓	1	↓.	1310.	1	
294	16.9	10.3	- 5.9	15300.	1720.	8.4	- 2.8
295	1	1	- 5.9	1	1	1	- 2.0
296			- 6.0				
297	1	. ↓	- 6.0		1		1
298	20.4	13.7	- 8.7		2610.	li l	- 4.7
299	1	1	- 8.7	ŀ	2610.		,
300			- 8.8		2620.	1	
301	1	↓	- 8.8	. ↓	2620.	8.3	1
302	14.9	6.8	- 4.1	15400.	1310.	8.4	- 2.7
303	1	1	ı	1	1	ı	1
304			. ↓				ı
305	•	+	- 4.2	↓	♦	j	+
306	16.9	9.0	- 5.8	15600.	1740.		- 4.0
307	П	9.0	- 5.8	1	1		- 4.0
308	↓	8.9	- 5.9				- 4.1
309	17.0	8.9	- 5.9	↓	\		- 4.1
310	20.3	12.3	- 8.4	15800.	2640.	8.3	- 6.0
311			- 8.4	1	Ī	j	- 6.0
312	+		- 8.5				- 6.1
313	20.4	+	- 8.6	†	+	↓	- 6.1

TABLE XV. CASE DESCRIPTIVE INFORMATION AND TRIM DATA, COMPOUND SINGLE-ROTOR HELICOPTER, No. 1 Wing: Area, 225 ft²; Chord, 80.5 in.; Mass Ratio, 67.2 Main Rotor Data Case Vel No. (Kt) Gust Disc Rad Chord Mass Lock $M_{\underline{\text{tip}}}$ (Ft) Type Ldg (In.) **RPM** Ratio No. Semirigid Rotor (4 Blades) 71 200 **SUDV** 7.0 .05 .80 26.1 35.6 234. 4.47 8.31 72 200 SSQV 73 **SUDV** 225 74 225 SSQV 75 250 **SUDV** 76 250 SSQV 77 300 **SUDV** 78 300 SSQV 79 350 **SUDV** 350 80 SSQV 81 200 **SUDV** .85 82 200 SSQV 83 225 **SUDV** 84 225 SSQV 85 250 **SUDV** 250 SSQV 86 87 300 **SUDV** 300 88 SSQV 89 350 SUDV 350 SSQV 90 91 200 .90 **SUDV** 200 92 SSQV 93 225 **SUDV**

				Trim Da	ta		
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)
71	9.44	-2.54	-1.83	3126.	12159.	649.	64
72	9.44	-2.54	-1.83	3126.	12159.	649.	64
73	8.56	-3.26	-1.12	2662.	12694.	669.	09
74	8.56	-3.26	-1.12	2662.	12694.	669.	09
75	7.95	-3.46	-1.71	111.	15367.	605.	0.01
76	7.95	-3.46	-1.71	111.	15367.	605.	0.01
77	13.4	1.60	-2.94	5540.	10270.	734.	-1.48
78	13.4	1.60	-2.94	5540.	10270.	734.	-1.48
79	17.3	3.44	-1.44	10749.	5825.	1115.	-3.16
80	17.3	3.44	-1.44	10749.	5825.	1115.	-3.16
81	9.67	9.67	-4.25	1311.	13833.	862.	0.03
82	9.67	9.67	-4.25	1311.	13833.	862.	0.03
83	6.88	-2.99	-0.07	1671.	13335.	1038.	2.38
84	6.88	-2.99	-0.07	1671.	13335.	1038.	2.38
85	7.15	-2.68	-1.10	168.	14961.	1006.	1.80
86	7.15	-2.68	-1.10	168.	14961.	1006.	1.80
87	10.0	96	-2.36	1750.	13814.	1031.	-0.15
88	10.0	96	-2.36	1750.	13814.	1031.	-0.15
89	14.3	1.29	-1.37	7997.	8068.	1464.	-2.08
90	14.3	1.29	-1.37	7997.	8068.	1464.	-2.08
91	6.26	-3.10	-2.10	1251.	12510.	1601.	-3.50
92	6.22	-3.10	-2.10	1251.	12510.	1601.	
93	15.9	3.08	-5.29	8845.	6431.	2190.	-4.18

		(CO			E XV NGLE-R		inued ELICOPT	ER, N	o. 1)	
Wing	: Are	a, 225	ft ² ;	Cho	rd, 80	.5 in.	; Mass	Ratio	, 67.2	
					1	Main R	lotor Da	ta		
Case	Vel	Gust	Disc	C _T		Rad	Chord		Mass	Lock
No.	(Kt)	Type	Ldg	$\overline{\sigma}$	Mtip	(Ft)	(In.)	RPM	Ratio	No.
			Semir	igid	Rotor		ades)			
94	225	SSQV	7.0	.05	•90	26.1	35.6	234.	4.47	8.31
95	250	SUDV	ı	T	1	1	1	1	1	1
96	250	SSQV								
97	300	SUDV								
98	300	SSQV								
99	350	SUDV		l						
100	350	ssqv			+					
101	200	SUDV			.95					
102	200	ssqv								
103	225	SUDV								
104	225	ssqv								
105	250	SUDV						1		
106	250	ssqv						1		
107	300	SUDV						1		
108	300	ssqv							-	
109	350	SUDV							-	
110	350	ssqv	+	↓	•	+	 	+	+	+
111	200	SUDV	4.0	.02	.90	34.5	67.1	177.	1.93	8.42
112	200	SSQV	1		1				1	1
113	225	SUDV		}						
114	225	ssqv								
115	175	SUDV								
116	175	ssqv	+	•	•		*	•	+	+

		Trim Data										
Case No.	Coll (Deg)	Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)					
94	15.9	3.08	-5.29	8845.	6431.	2190.	-4.18					
95	14.4	2.00	-3.23	8699.	6573.	2113.	-2.59					
96	14.4	2.00	-3,23	8699.	6573.	2113.	-2.59					
97	13.7	2.31	-3.89	3041.	12407.	1830.	-1.82					
98	13.7	2.31	-3.89	3041.	12407.	1830.	-1.82					
99	17.1	3.81	-1.95	8221.	7521.	2752.	-3.01					
100	17.1	3.81	-1.95	8221.	7521.	2752.	-3.01					
101	13.4	3.62	-6.32	2611.	12214.	2105.	-2.06					
102	13.4	3.62	-6.32	2611.	12214.	2105.	-2.06					
103	13.9	3.58	-5.87	2793.	12090.	2305.	-2.21					
104	13.9	3.58	-5.87	2793.	12090.	2305.	-2.21					
105	12.5	2.42	-5.21	-8.	14873.	2222.	-1.39					
106	12.5	2.42	-5.21	-8.	14873	2222.	-1.35					
107	12.5	1.69	-4.14	792.	14233.	2612.	-1.38					
108	12.5	1.69	-4.14	792.	14233.	2612.	-1.38					
109	17.5	4.00	-2.22	7156.	8266.	3925.	-3.74					
110	17.5	4.00	-2.22	7156.	8266.	3925.	-3.74					
111	19.9	15.3	-12.5	12662.	1841.	3655.	-2.98					
112	19.9	15.3	-12.5	12662.	1841.	3655.	-2.98					
113	23.6	19.1	-14.7	13489.	558.	4649.	-3.92					
114	23.6	19.1	-14.7	13489.	558.	4649.	-3.92					
115	16.6	12.3	-10.4	11776.	2943.	2781.	-1.83					
116	16.6	12.3	-10.4	11776.	2943.	2781.	-1.83					

TABLE XV - Continued (COMPOUND SINGLE-ROTOR HELICOPTER, No. 1) Wing: Area, 225 ft²; Chord, 80.5 in.; Mass Ratio, 67.2 Main Rotor Data Disc Gust Case Vel Rad Chord Mass Lock Mtip (Ft) (Kt) **RPM** Type Ldg (In.) Ratio No. Semirigid Rotor (4 Blades) 117 SUDV 4.0 .05 .90 34.5 26.9 177. 1.93 10.3 200 118 200 SSQV 119 225 **SUDV** 120 225 SSQV 121 175 SUDV 122 175 SSQV .02 200 123 SUDV 10.0 21.8 106.2 280. 7.64 5.04 124 200 SSQV 125 225 SUDV 126 225 SSQV 127 175 SUDV 128 175 SSQV 129 SUDV .05 42.5 200 7.10 130 200 SSQV 131 225 SUDV 132 225 SSQV 133 175 SUDV 134 SSQV 175 Articulated Rotor (4 Blades) 135 200 SUDV 4.0 .02 .90 34.5 67.1 177. 1.93 8.42 136 SSQV .02 67.1 8.42 137 26.9 SUDV .05 10.27 138 SSQV 26.9 .05 10.27

				Trim Da	ta		
Case No.	Coll (Deg)	Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)
117	17.1	10.9	-5.38	12334.	2709.	1754.	-2.60
118	17.1	10.9	-5.38	12334.	2709.	1754.	-2.60
119	20.3	13.6	-7.24	14561.	538.	2262.	-3.92
120	20.3	13.6	-7.24	14561.	538.	2262.	-3.92
121	14.2	8.39	-4.77	11062.	3926.	1290.	-1.19
122	14.2	8.39	-4.77	11062.	3926.	1290.	-1.19
123	20.4	17.4	-13.4	11406.	3255.	3450.	-2.43
124	20.4	17.4	-13.4	11406.	3255.	3450.	-2.43
125	22.5	19.4	-14.0	10670.	3599.	3475.	2.49
126	22.5	19.4	-14.0	10670.	3599.	3475.	2.49
127	19.3	21.0	-15.4	7628.	7037.	2744.	1.12
128	19.3	21.0	-15.4	7628.	7037.	2744.	1.12
129	17.1	11.9	-16.5	11047.	3949.	1728.	-1.87
130	17.1	11.9	-16.5	11047.	3949.	1728.	-1.87
131	20.7	15.0	-8.10	13216.	1723.	2888.	-3.38
132	20.7	15.0	-8.10	13216.	1723.	2888.	-3.38
133	14.7	9.27	-4.80	10656.	4333.	1358.	-0.87
134	14.7	9.27	-4.80	10656.	4333.	1358.	-0.87
135	13.9	6.72	-5.44	13797.	1921.	2688.	-2.94
136	13.9	6.72	-5.44	13797.	1921.	2688.	-2.94
137	16.9	9.52	-4.40	14271.	1135.	1798.	-3.50
138	16.9	9.52	-5.40	14271.	1135.	1798.	-3.50

TABLE XV - Continued (COMPOUND SINGLE-ROTOR HELICOPTER, No. 1)

Wing	: Are	a, 225	ft ² ;	Cho	rd, 80).5 in	.; Mass	Ratio	, 67.2	
						Main I	Rotor Da	ta		
Case No.	Vel (Kt)	Gust Type	Disc Ldg	$\frac{\mathrm{C_T}}{\sigma}$	M_{tip}	Rad (Ft)	Chord (In.)	RPM	Mass Ratio	Lock No.
		allee	Artic				Blades)			
139	200	SUDV	7.0	.02	.90	26.1	89.0	234.	4.47	6.58
140	1	ssqv	1	.02	1	1	89.0	1	1	6.58
141		SUDV		.05			35.6			8.31
142		ssqv	†	.05		+	35.6	•	♦	8.31
143		SUDV	10.0	.02		21.8	106.2	280.	7.64	5.04
144		ssqv	1	.02		i	106.2	1		5.04
145		SUDV		.05			42.5			7.10
146	•	ssqv	†	.05	+	•	42.5	•	•	7.10
			Rigid	Rote	or (4	Blade	s)			
147	200	SUDV	4.0	.02	.90	34.5	67.1	177.	1.93	8.42
148	1	ssqv	1	.02	1		67.1	- 1	1	8.42
149		SUDV		.05			26.9			10.27
150		ssqv	•	.05		•	26.9	+	+	10.27
151		SUDV	7.0	.02	9	26.1	89.0	234.	4.47	6.58
152	1	ssqv	1	.02		1	89.0	- 1	1	6.58
153		SUDV		.05			35.6			8.31
154		ssqv	•	.05		•	35.6		+	8.31
155		SUDV	10.0	.02		21.8	106.2	280.	7.64	5.04
156		ssqv	1	.02		1	106.2		1	5.04
157		SUDV	1	.05			42.5			7.10
158	•	ssqv	+	.05	+	+	42.5	+	+	7.10
		1	Artic	late	d Rot	or (4	Blades)			
159	250	SUDV	7.0	.02	.90	26.1	89.0	234.	4.47	6.54
160	1	ssqv	1	.02		1	89.0		1	6.54
161	•	SUDV	•	.05	<u> </u>	•	35.6	+	+	8.31

				Trim Dat			
		_	TPP		Wing		Fuse
Cas e No.	Coll (Deg)	Cyc (Deg)	Attack (Deg)	Thrust (Lb)	Lift (Lb)	HPR (Hp)	Pitch (Deg)
	(208)	(208)	(208)	1207	(LD)		(208)
139	16.4	10.1	-8.92	13353.	2477.	3864.	-4.25
140	16.4	10.1	-8.92	13353.	2477.	3864.	-4.25
141	16.9	8.57	-4.54	15299.	373.	2413.	-3.79
142	16.9	8.57	-4.54	15299.	373.	2413.	-3.79
143	16.8	8.88	-7.05	15963.	266.	3280.	-3.94
144	16.8	8.88	-7.05	15963.	266.	3280.	-3.94
145	16.9	9.86	-5.13	13198.	2267.	1812.	-2.80
146	16.9	9.86	-5.13	13198.	2267.	1812.	-2.80
147	13.8	6.72	-5.44	13980.	1921.	2688.	-2.94
148	13.8	6.72	-5.44 -5.44	13980.	1921.	2688.	-2.94
149	16.7	10.7	-6.17	11887.	3124.	1680.	-2.36
150	16.7	10.7	-6.17	11887.	3124.	1680.	-2.36
151	16.5	10.4	-9.13	13120.	2647.	3859.	-4.16
152	16.5	10.4	-9 . 13	13120.	2647.	3859.	-4.16
153	16.9	8.57	-4.54	15299.	373.	2413.	-3.79
154	16.9	8.57	-4.54	15299.	373.	2413.	-3.79
155	15.4	5.21	-6.21	15322.	840.	3060.	-3.61
156	15.4	5.21	-6,21	15322.	840.	3060.	-3.61
157	16.9	9.86	-5.12	13200.	2267.	1812.	-2.80
158	16.9	9.86	-5.12	13200.	2207.	1812.	-2.80
					,		2.00
159	22.4	16.9	-12.2	14300.	840.	5700.	-5.4
160	22.4	16.9	-12.2	14300.	840.	5700.	-5.4
161	16.7	8.9	-3.4	13100.	2600.	2600.	-3.1

TABLE XV - Continued (COMPOUND SINGLE-ROTOR HELICOPTER, No. 1) Wing: Area, 225 ft²; Chord, 80.5 in.; Mass Ratio, 67.2 Main Rotor Data Lock Mass Chord Rad Case Vel Gust Disc $M_{t\underline{ip}}$ RPM Ratio No. (Ft) (In.) (Kt) Type Ldg Articulated Rotor (4 Blades) 35.6 234. 4.47 8.31 .05 .90 26.1 7.0 250 SSQV 162 34.5 67.1 177. 1.93 8.42 4.0 .02 SUDV 163 240 8.42 67.1 240 SSQV .02 164 10.3 .05 26.9 SUDV 165 250 10.3 26.9 .05 SSQV 166 7.64 7.1 42.5 21.8 280. SUDV 10.0 .05 169 7.1 7.64 SSQV 10.0 .05 21.8 42.5 280. 170 Rigid Rotor (4 Blades) 234. 4.47 6.54 .90 26.1 89.0 SULV 7.0 .02 171 250 6.54 89.0 .02 172 SSQV 8.31 35.6 SUDV .05 173 8.31 35.6 174 SSQV .05 8.42 34.5 67.1 177. 1.93 .02 240 SUDV 4.0 175 8.42 67.1 .02 176 240 SSQV 10.3 26.9 .05 177 250 SUDV 10.3 26.9 .05 SSQV 178 42.5 280. 7.64 7.1 21.8 181 SUDV 10.0 .05 7.64 7.1 280. 21.8 42.5 SSQV 10.0 .05 182 Semirigid Rotor (4 Blades) 4.47 4.14 17.8 234. 26.1 SUDV 7.0 .10 .90 223 200 224 200 SSQV SUDV 225 250 SSQV 226 250

				Trim Data	a		
Case No.	Coll (Deg)	Cyc (Deg)	TPP Attack (Deg)	Thrust	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)
162	16.7	8.9	-3.4	13100.	2600.	2600.	-3.1
163	12.4	6.6	-4.3	7500.	8200.	2400.	-1.0
164	12.4	6.6	-4.3	7500.	8200.	2400.	-1.0
165	16.0	9.5	-4.3	9800.	5600.	1500.	-2.1
166	16.0	9.5	-4.3	9800.	5600.	1500.	-2.1
169	17.8	10.8	-4.7	11800.	3500.	1900.	-2.8
170	17.8	10.8	-4.7	11800.	3500.	1900.	-2.8
171	22.7	17.6	-12.6	14100.	870.	5800.	-5.4
172	22.7	17.6	-12.6	14100.	870.	5800.	-5.4
173	16.7	8.9	-3.4	13100.	2600.	2600.	
	16.7	8.9	-3.4			2600.	-3.1
174 175	12.4	6.6	-3.4 -4.3	13100. 7500.	2600. 8200.		-3.1
176	12.4	6.6	-4.3	7500.	8200. 8200.	2400. 2400.	-1.0 -1.0
177	16.0	9.5	-4.3 -4.3	9600.	5600.		
					-	1500.	-2.1
178	16.0	9.5	-4.3	9600.	5600.	1500.	-2.1
181	17.8	10.8	-4.7	11800.	3500.	1900.	-2.8
182	17.8	10.8	-4.7	11800.	3500.	1900.	-2.8
223	18.0	12.5	-4.3	10000.	5200.	1100.	-1.2
224	18.0	12.5	-4.3	10000.	5200.	1100.	-1.2
225	28.7	20.3	1.5	13500.	1500.	3900.	-3.6
226	28.7	20.3	1.5	13500.	1500.	3900.	-3.6

TABLE XV - Continued (COMPOUND SINGLE-ROTOR HELICOPTER, No. 1) Wing: Area, 225 ft²; Chord, 80.5 in.; Mass Ratio, 67.2 Main Rotor Data Disc CT Case Vel Gust Rad Chord Mass Lock ${\rm M}_{t\underline{\rm ip}}$ (Kt) (Ft) (In.) **RPM** Ratio No. Type Ldg Rigid Rotor (4 Blades) 227 200 SUDV 7.0 .10 .90 26.1 17.8 234. 4.47 228 200 SSQV SUDV 229 250 230 250 SSQV Articulated Rotor (3 Blades) SUDV 7.0 .10 234. 4.47 4.14 .90 26.1 23.7 231 200 232 200 SSQV 233 250 SUDV 234 250 SSQV

				Trim Data	a		
Case No.	Coll (Deg)	Cyc (Deg)	TPP Attack (Deg)	Thrust (Lb)	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)
227	20.2	12.2	-2.6	13600.	2100.	1500.	-2.9
228	20.2	12.2	-2.6	13600.	2100.	1500.	-2.9
229	27.6	20.3	4	12300.	2400.	3200.	-3.3
230	27.6	20.3	4	12300.	2400.	3200.	-3.3
231	20.6	12.6	-2.1	13600.	2000.	1500.	-2.9
232	20.6	12.6	-2.1	13600.	2000.	1500.	-2.9
233	26.7	19.3	3	12300.	2500.	3000.	-3.2
234	26.7	19.3	3	12300.	2500.	3000.	-3.2

T	ABLE X	rvi. c	ASE D OMPOU	ESCR ND S	IPTIVE INGLE-	INFOR ROTOR	MATION HELICOP	AND T	RIM DAT	Ά,
Wing	: Area	., 27.8	ft ² ;	Cho	rd, 45	.0 in.	; Mass	Ratio	, 8 1.5	
					N	Main R	otor Da	ta		
Case No.	Vel (Kt)		Disc Ldg	$\frac{C_{T}}{\sigma}$	M _{tip}	Rad (Ft)	Chord (In.)		Mass Ratio	Lock No.
			Semir		Rotor		ades)			
238	150	SSQV	5.6	.064	.86	22.	27.	324.	4.24	5.03
239	1		1	1	-	1	1	1	i	1
240		- 🕴								
250		SUDV			11					1
251		SEDV	l							
252		SUDV								
253		SEDV					<u> </u>			
254		SSQV								
255		RMPV								
256		RMPV	ŀ							
257		ssqv								
258		RFTP								
259		ssqv								
260		1							П	1 1
261		V								
262		SUDV								
269		SEDV								
275		SSQV							П	
276 277		1			1		1	1.	1	

Case No.	Coll (Deg)	F&A Cyc	TPP		111		
No.	(Deg)	(Deg)	Attack (Deg)	Thrust (Lb)	Wing Lift (Lb)	HPR (Hp)	Fuse Pitch (Deg)
238 239 240 250 251 252 253 254 255 256 257 258 259 260 261 262	16.3	6.7	-8.3	7700.	850.	950.	-6.9

TABLE XVII. CASE DESCRIPTIVE INFORMATION AND TRIM DATA, TANDEM-ROTOR HELICOPTER

							Main Re	otor Da	ta		
Case No.	Vel (Kt)	Gust Type	Disc Ldg		Mti	p	Rad (Ft)	Chord (In.)	RPM	Mass Katio	Lock No.
			Aft	CG			des)	16			
183	200.	SUDV	7.	.02	.9	0	18.35	57.6	348.	6.43	5.61
184	1	ssqv	1	.02		l	1	57.6		1	ì
185		SUDV		.05				23.0			
186	+	SSQV		.05				23.0			
187	225.	SUDV		.02				57.6			
183	1	ssqv		.02				57.6			
189		SUDV	1	.05				23.0			
190	+	SSQV	+	.05	4	•	+	23.0	Ť		↓
			Neut	ral	CG	(4	Blades)			
272	200.	ssqv	7.	.05	.9	00	18.35	23.0	348.	6.43	5.61
			Forw	vard	CG ((4	Blades)			
274	200.	ssqv	7.	.05	.9	0	18.35	23.0	348.	6.43	5.61

	Fo	rward Ro	tor	Trim				
Case No.	Coll (Deg)	Thrust (Lb)	TPP Attack (Deg)	Coll (Deg)	Thrust (Lb)	TPP Attack (Deg)	F&A Cyc (Deg)	Fuse Pitch (Deg)
183	22.4	7700.	-15.7	22.4	7300.	-14.2	18.0	- 8.2
184	22.4	7700.	-15.7	22.4	7300.	-14.2	18.0	- 8.2
185	20.7	7100.	- 9.8	20.7	7900.	- 7.0	19.7	- 0.7
186	20.7	7100.	- 9.8	20.7	7900.	- 7.0	19.7	- 0.7
187	27.0	7600.	-19.2	27.0	7600.	-17.8	20.6	-12.2
188	27.0	7600.	-19.2	27.0	7600.	-17.8	20.6	-12.2
189	25.3	7400.	-12.3	25.3	7700.	- 8.9	26.8	- 1.0
190	25.3	7400.	-12.3	25.3	7700.	- 8.9	26.8	- 1.0
272	20.3	7800.	- 8.57	20.3	7400.	- 7.6	1.2	- 6.1
274	20.1	8650.	- 7.6	20.1	6700.	- 8.4	6.6	-11.1

TABLE XVIII. CASE DESCRIPTIVE INFORMATION AND TRIM DATA, SIDE-BY-SIDE HELICOPTER

Wing: Area, 330.5 ft²; Chord, 80 in.; Mass Ratio, 67.6

						Main R	otor Da	ta		
Case No.	Vel (Kt)	Gust Type	Disc Ldg	C.L	Mtip	Rad (Ft)	Chord (In.)	RPM	Mass Ratio	Lock No.
			Heli			e (3 B	lades)			
199	120.	SSQV	9.87	.105	.9	19.25	20.	408.	67.6	5.39
200	150.	SSQV	9.87	.105	.9	19.25	20.	408.	67.6	5.39
			Tran	siti	on Mod	le (3 B	lades)			
201	120.	SSÇV	9.87	.105	.9	19.25	20.	408.	67.6	5.39
202	120.	SSQV	- 1	1	1	1	1	1	1	
203	150.	ssqv					İ		i	1
204	150.	SSQV		↓	+ :		•	+	1	•
			Airp	lane	Mode	(3 Blac	des)			
205	120.	SUDV	9.87	.105	.9	19.25	20.	408.	67.6	5.39
206	120.	SSQV		1	1	1	1	1	1	1
207	150.	SUDV								
208	150.	SSQV								
209	200.	SUDV				1				
210	200.	SSQV								
211	300.	SUDV								
212	300.	SSQV								
213	400.	SUDV								
214	400.	SSQV	+			+	+	+	+	+

				Trim Data			
Case No.	Coll (Deg)	F&A Cyc (Deg)	TPP Attack (Deg)	Thrust Per Rotor (Lb)	Lift (Lb)	HPR (Hp)	Pitch (Deg)
199	30.3	7.3	- 6.8	11600.	440.	3330.	-5.1
200	33.0	8.4	- 8.3	13900.	-316.	5000.	-7.8
201	32.2	3.6	-20.1	4600.	13000.	1760.	4.3
202	37.1	.9	-45.6	2000.	17900.	1740.	7.9
203	35.3	5.3	-24.4	5340.	11800.	3860.	8
204	42.0	2.1	-51.0	1240.	18400.	1490.	2.4
205	60.2	0.	-71.1	1990.	20300.	1940.	14.4
206	60.2	- 1	-71.1	1990.	20300.	1940.	14.4
207	65.4		-84.5	850.	22300.	1460.	4.4
208	65.4		-84.5	850.	22300.	1460.	4.4
209	73.4		-90.8	980.	24100.	2080.	6
210	73.4		-90.8	980.	24100.	2080.	6
211	83.6	,	-93.3	1790.	29900.	4370.	-4.2
212	83.6		-93.3	1790.	29900.	4370.	-4.2
213	89.7	ľ	-94.3	2880.	34600.	8920.	-5.7
214	89.7	•	-94.3	2880.	34600.	8920.	-5.7

TABLE XIX.	PARAMETERS FOR STOPPED	-ROTOR ANALYSIS
	ROTOR	
	Blades 2	Radius 33.2 ft Chord 15 in.
Blade Segment (% R)	Beamwise Stiffness (10 ⁶ lb-in ²)	Weight/in. (lb/in.)
0-16.7	14000	15
16.7-33.3	2000	2.4
33.3-50.0	600	1.6
50.0-66.7	600	1.5
66.7-83.3	600	1.5
83.3-100.	600	1.5
	MAST	
Mast Segment (% Length from Base)	Bending Stiffness (10 ⁶ lb-in ²)	Length 8.3 ft Weight/ft (lb/ft)
0-33.3	80000	3
33.3-66.7	150	150
66.7-100.	100	3

TA	ABLE XX. PA	RAMETERS FOR TRA	ATTED DOTO	D ANA I	VCTC
	-BEE AK. PA		AILED-ROIC	- ANAI	
		ROTOR			
	oer of Blade	s 3	Radius Chord	230 21	
Blade Segment (% R)		Beamwise Stiffne (10 ⁶ lb-in ²)	ss		Weight/in. (lb/in.)
0-25		4500			4.07
25-50		1700			2.0
50-75		250			2.28
75-100		90			1.72
		WING			
lling			Span Chord	240 in 85.3	n. 73.3 in.
Wing Segment (% Semi- span) (1	Beamwise Stiffness 09 lb-in ²)	Torsional Stiffness (10 lb-in ²)	Weight/in(lb/in.)		Inertia (1b-in-sec ²)
0-16.7	13	9.8	13.7		122,000
16.7-33.3	11.3	8.6	12.5		106,000
33.3-50.0	8	6.8	11.5		91.000
50.0-66.7	5	5.1	10.4		76,000
66.7-83.3	3	4.0	9.8		68,000
83.3-100.	Rigid	Rigid	1576	L	+,990,000

APPENDIX III. GUST RESPONSE CASE RESULTS

	TA	BLE XXI			SE RESULTS R HELICOPT	
Case No.	Shape	Gust Ty Length (Ft)	ype Max Vel (Ft/Sec)	Osc Mome	ade Root ent Ratio ^M steady Chord	Max Flap Velocity (Deg/Sec)
	Semiri	gid Roto	r			
1	SUDV	0.	50.	0.86	1.80	58.1
2	ssqv	90.	1	1.67	3.15	25.6
3	SUDV	0.		0.63	1.54	60.1
4	ssqv	90.		1.38	2.64	27.7
5	SUDV	0.	į	0.79	1.79	59.5
6	SSQV	90.		1.64	3.05	25.8
7	SUDV	0.		0.57	1.46	61.3
8	ssqv	90.	ļ	1.28	2.50	27.7
9	SUDV	0.		0.74	2.40	61.0
10	ssqv	90.		1.58	3.57	26.3
11	SUDV	0.		0.50	1.73	63.0
12	ssqv	90.		1.11	2.57	27.9
13	SUDV	0.		0.71	2.57	62.5
14	ssqv	90.		1.29	3.34	27.3
15	SUDV	0.	ŧ	0.44	1.61	65.7
16	ssqv	90.		0.76	2.10	28.9
17	SUDV	0.		0.91	1.27	32.4
18	ssqv	90.		1.54	4.10	12.3
19	SUDV	0.		0.99	1.04	28.8
20	ssqv	90.		1.87	2.83	10.8
21	SUDV	0.		0.85	3.40	55.8
22	ssqv	90.		1.90	8.00	25.4
23	SUDV	0.		0.63	1.45	57.9
24	ssqv	90.	+	1.44	4.28	27.1

	Max		Gust-	
.	Rotor	Max Δn	Allev Factor	
Case No.	Thrust (Lb)	(g)	(K _g)	Comments
1	40500.	1.81		
2	29000.	0.98	.543	
3	39900.	1.77		
4	28300.	0.93	.524	
5	41000.	1.84		4
6	28900.	0.96	.529	
7	40400.	1.81		
8	28100.	0.92	.506	
9	41200.	1.87		
10	28700.	0.97	.516	
11	40500.	1.81		
12	28100.	0.92	.490	
13	40600	1.82		
14	28500.	0.94	.522	
15	39100.	1.73		
16	27700.	0.89	.519	
17	92700.	5.19		
18	51400.	2.39	.471	
19	98600.	5.61		
20	52700.	2.51	. 447	
21	42100.	1.91		
22	30000.	1.03	.547	
23	40400.	1.79		
24	29200.	0.98	.555	

TABLE XXI - Continued (PURE SINGLE-ROTOR HELICOPTER)

		Gust Ty		Max Blade Root Osc Moment Ratio		Max Flap
Case No.	Shape	Length (Ft)	Max Vel (Ft/Sec)	Mgust/M Beam	steady Chord	Velocity (Deg/Sec)
	Semiri	gid Roto	or (Cont'd)			
25	SUDV	0.	50.	0.83	1.10	35.4
26	ssqv	90.	Ì	1.50	3.53	12.0
27	SUDV	0.	i i	0.90	1.10	35.0
28	ssov	90.		1.84	3.56	9.8
29	SUDV	0.		0.88	3.92	60.9
30	ssov	90.		1.67	7.08	27.1
31	SUDV	0.		0.80	2.10	63.7
32	ssqv	90.		1.17	2.46	29.7
33	RMPV	90.		1.62	3.64	21.0
34	RMPV	90.		1.16	2.45	22.1
35	SUDH	0.		0.90	1.15	2.46
36	SSQH	90.		1.11	1.70	2.87
37	SUDH	0.		0.90	0.78	184
38	SSQH	90.	•	0.98	2.02	7.25
	•	lated Ro	tor			
39	SUDV	0.	50.	1.81	1.27	35.2
40	ssqv	90.	1	1.64	1.35	15.6
41	SUDV	0.		24.1	2.43	55.0
42	SSQV	90.		2.33	3.18	28.3
43	SUDV	0.		16.1	2.08	35.5
44	SSQV	90.		0.93	1.93	14.9
45	SUDV	0.		22.3	1.62	16.0
46	ssov	90.		3.59	2.38	26.7
47	SUDV	0.	1	13.2	2.28	34.6

Case No.	Max Rotor Thrust (Lb)	Max An (g)	Gust- Allev Factor (K _g)	Comments		
25	94100.	5.32				
26	50200.	2.33	.445			
27	96700.	5.43				
28	47200.	2.12	.393			
29	40300.	1.79				
30	28600	0.94	.531			
31	39800.	1.76				
32	28200.	0.91	.523			
33	27300.	0.90	.483	Kg obtained based on Case 9		
34	26700.	0.80	.441	Kg obtained based on Case 10		
35	10700.	-0.30		8		
36	18200.	0.20	.609			
37	9900.	-0.40				
38	18600.	0.22	.550			
39	93800.					
40	56700.		.521			
41	42400.	_				
42		1.07	.565			
43	94700.	5.30				
44	55100.	2.56	.492			
45	41500.	1.84	4*_			
46	29300.	0.96	.522			
47	95000.	5.31				

TABLE XXI - Continued (PURE SINGLE-ROTOR HELICOPTER)

				Max Bla	de Root	· · · · · · · · · · · · · · · · · · ·
		Gust Typ		Osc Mome	nt Ratio	Max Flap
Case		Length	Max Vel	M _{gust} /M	steady	Velocity
No.	Shape	(Fť)	(Ft/Sec)	Beam	Chord	(Deg/Sec)
	Articu	lated Ro	tor (Cont'	d)		
48	ssqv	90.	50.	1.17	3.12	12.6
49	SUDV	0.	1	20.9	1.82	59.6
50	ssqv	90.		4.61	2.60	25.9
	Rigid	Rotor				
51	SUDV	0.	50.	6.45	4.85	35.2
52	SSQV	90.	Ī	3.01	2.90	16.2
53	SUDV	0.		6.72	1.28	55.0
54	SSQV	90.		4.16	9.32	25.9
55	SUDV	0.	Í	4.74	2.69	35.5
56	SSQV	90.	•	1.36	2.47	14.3
57	SUDV	0.		6.56	7.06	60.0
58	SSQV	90.		4.21	4.28	19.8
59	SUDV	0.		66.2	5.24	34.6
60	SSQV	90.		2.24	2.09	13.1
61	SUDV	0.		7.20	6.92	59.6
62	ssqv	90.	•	1.83	5.25	26.8
	Articu	lated Ro	tor			
63	SUDV	0.	50.	12.3	1.52	40.3
64	SSQV	90.	1	1.12	1.79	18.1
65	SUDV	0.		17.2	1.22	60.6
66	ssqv	90.	į.	3.51	1.64	28.4
	Rigid	Rotor				•
67	SUDV	0.	50.	3.97	3.96	40.3
68	SSQV	90.		1.31	2.55	15.3

Case	Max Rotor Thrust (Lb)	Max Δn (g)	Gust- Allev Factor (K _g)	Comments
48	50000.	2.21	.425	
49	40400.	1.77		
50	28100.	0.88	.500	
51	93800.	5.22		
52	59000.	2.81	.551	
53	42400.	1.90		
54	30000.	1.02	.537	
55	94700.	5.30		
56	55000.	2.55	.491	
57	41500.	1.84		
58	26700.	0.81	.440	
59	94900.	5.31		
60	51600.	2.32	.447	
61	40400.	1.77		
62	28500.	0.91	.51.8	
63	86100.	4.67		
64	53400.	2.37	.525	-
65	40800.	1.79		
66	29000.	0.93	.526	
67	86100.	4.67		
68	50400.	2.18	.483	

TABLE XXI - Continued (PURE SINGLE-ROTOR HELICOPTER)

Case No.	Shape	Gust Typ Length (Ft)	Max Vel	Osc Mome	de Root ent Ratio steady Chord	Max Flap Velocity (Deg/Sec)
	Rigid	Rotor (C	ont'd)			
69	SUDV	0.	50.	3.70	2.33	62.1
70	SSQV	90.	↓	3.84	6.35	17.3
	Semiri	igid Roto	r			
217	SUDV	0.	50.	1.05	2.75	108.
218	ssqv	90.	50.	1.40	6.11	40.
	Rigid	Rotor				
219	SUDV	0.	50.	3.96	2.35	101.
220	SSQV	90.	50.	4.99	7.15	12.
	Articu	ılated Ro	otor			
221	SUDV	0.	50.	17.73	1.56	82.
222	ssqv	90.	50.	8.57	1.91	34.
	Semir	igid Roto	r			
235	ssqv	90.	50.	1.85	3.28	24.6
236]	2.40	2.85	17.7
237	\	\		1.75	2.62	18.8
243	SUDV	Ő.		1.34	2.67	47.5
244	SSQV	90.		2.61	4.35	16.9
245	SUDV	0.		1.79	2.95	31.2
246	SSQV	90.		1.95	4.35	6.2
247				1.55	4.25	48.0
248		♦		1.77	2.99	27.5
249	SUDV	0.		.82	2.33	94.8

Case No.	Max Rotor Thrust (Lb)	Max Δn (g)	Gust- Allev Factor (K _g)	Comments						
69	40800.	1 70								
70	24400.		.3 6							
. "	24400.	0.04	•30							
217	30300.	1.13								
218	22200.		.48	*						
219	29300.	1.05	*							
220	18200.	0.28	.27							
221	29100.	1.04								
222	23600.	0.62	.60							
235	28500.			$\delta_3 = 30^{\circ}$						
236	26100.		*.45	Pitch Cone Coupling Ratio=5						
237	26800.	0.84	*.45	Bob Weight ⇒ l D e g/g						
243	40300.	1.78								
244	29600.		.57							
245	40000.									
246	30400.	1.05	.61							
247	34800.		*.73	Pitch-Cone Coupling Ratio= .5						
248	29100.		*.53	δ3 = 0.						
249	40200.	1.85		$\delta_3 = 0.$, No Pitch-Jone Coupling						
*Base	*Based on case number 249.									

TABLE XXI - Continued (PURE SINGLE-ROTOR HELICOPTER)

				Max Bl	ade Root	
Case No.	Shape	Gust Typ Length (Ft)	e Max Vel (Ft/Sec)	Osc Mome	ent Ratio Steady Chord	Max Flap Velocity (Deg/Sec)
	Semiri	gid Roto	r (Cont'd)			
263	SUDL	0.	50.	1.04	.94	18.0
264	SSQL	90.	↓	1.08	1.88	4.7
	Rigid	Rotor				
265	SUDV	0.	5 0.	29.4	2.46	39.3
266	SSQV	90.		10.3	2.23	18.8
267	SUDV	0.		27.6	2.45	37.6
268	ssqv	90.	+	16.2	2.44	26.7
	Semiri	gid Roto	r			
270	SUDV	90.	50.	1.48	1.83	15.4
	Articu	lated Ro	tor			
278	SUDV	0.	-50.			66.0
279	SSQV	90.				17.1
280	1					14.5
281	↓	ļ				12.5
282	SUDV	0.				75.9
283	vçzz	90.				22.8
284						19.6
285	↓	↓				17.1
286	SUDV	0.				83.2
287	ssqv	90.				27.9
288	1	1				24.7
289	ļ	↓	↓			21.6

No.	Max Rotor Thrust (Lb)	Max Δn (g)	Gust- Allev Factor (K _g)	Comments
		\0/	 	
263	18900.	0.22		Horizontal Side Gust
264	18700.	0.21	.95	Horizontal Side Gust
265	29500.	2.58		Low Hub Spring, 1260 Ft-Lb/Deg
266	24300.	1.95	.76	Low Hub Spring, 1260 Ft-Lb/Deg
267	29400.	2.58		High Hub Spring, 3625 Ft-Lb/Deg
268	26400.	2.21	.85	High Hub Spring, 3625 Ft-Lb/Deg
270	23500.	1.84		
278	40500	1.78	-	Blade loads data not valid
279	30200	1.03	.58	for Cases 278-313 because of
280	31400	1.11	.62	resonance conditions.
281	32300	1.17	.66	
282	41000	1.81	_	
283	30100	1.02	.56	
284	31500	1.12	.62	
285	32600	1.19	.66	
286	41300	1.83	-	
287	29800	1.00	.55	
288	31500	1.11	.61	
289	32700	1.19	.65	

TABLE XXI - Continued (PURE SINGLE-ROTOR HELICOPTER)

			.	Max Blade Root	,
		Gust Typ	e	Osc Moment Ratio	Max Flap
Case No.	Shape	Length (Ft)	Max Vel (Ft/Sec)	Mgust/Msteady	Velocity (Deg/Sec)
10.	Bhape	(1-6)	(Ft/Sec)	Beam Chord	(Deg/Sec)
	Semiri	gid Roto	or		
290	SUDV	0.	-50.		65.3
291	ssqv	90.			18.4
292					15.5
293	†	\			13.4
294	SUDV	0.			77.2
295	ssqv	90.			24.1
296	1		ĺ		20.7
297	↓	•			18.3
298	SUDV	0.			84.7
299	ssqv	90.			29.2
300	Ī				25.6
301	. ↓	•			22.6
	Rigid	Rotor	•		
302	SUDV	0.	-50.		66.0
303	ssqv	90.]		17.1
304					14.4
305	↓	\rightarrow			12.5
306	SUDV	0.			75.9
307	ssqv	90.			22.8
308					19.6
309	\rightarrow	+			17.1
310	SUDV	0.			83.2
311	ssqv	90.			27.9
312					24.7
313	<u></u>	+	+		21.6

Case No.	Max Rotor Thrust (Lb)	Max Δn (g)	Gust- Allev Factor (K _g)	Comments
290	40000	1.75	-	
291	29900	1.02	.58	
292	31000	1.10	.63	
293	31900	1.16	.66	
294	41000	1.83	-	
295	29700	1.02	.56	
296	31200	1.11	.61	
297	32300	1.19	.65	
298	41200	1.85	-	
299	29400	0.99	.54	
300	31000	1.10	.60	
301	32200	1.19	.64	
302	40500	1.78	-	
303	30200	1.03	.58	
304	31400	1.11	.62	
305	323 00	1.17	.66	
306	41000	1.81	-	
307	30100	1.03	.57	
308	31500	1.12	.62	
309	326 00	1.19	.66	
310	41300	1.83	-	
311	29800	1.00	.55	
312	31 500	1.11	.61	
313	32700	1.19	.65	

TABLE XXII. GUST-RESPONSE CASE RESULTS, COMPOUND SINGLE-ROTOR HELICOPTER, NO. 1

		Gust Ty	7De	Osc Mome	ade Root ent Ratio	Max Flap
Case		Length	Max Vel		¹ steady	Velocity
No.	Shape	(Ft)	(Ft/Sec)	Beam	Chord	(Deg/Sec)
	Semiri	gid Rotor	•			
71	SUDV	0.	50.	1.25	0.79	40.9
72	SSQV	90.		2.99	2.81	16.3
73	SUDV	0.		1.29	.74	42.9
74	ssqv	90.		3.22	3.00	19.0
75	SUDV	0.		1.23	0.72	44.8
76	SSQV	90.		3.08	2.58	22.3
77	SUDV	0.		1.03	1.06	51.0
78	SSQV	90.		2.03	2.44	28.5
79	SUDV	0.		0.89	0.93	48.8
80	SSQV	90.		1.32	1.87	31.9
81	SUDV	0.	'	1.25	0.53	40.6
82	SSQV	90.		2.90	1.96	16.5
83	SUDV	0.		1.31	0.38	43.0
84	SSQV	90.		3.37	2.24	19.6
85	SUDV	0.		1.25	0.43	45.3
86	SSQV	90.		3.00	2.13	22.1
87	SUDV	0.	:	2.14	0.59	50.2
88	SSQV	90.		2.39	1.92	28.5
89	SUDV	0.		0.98	0.71	50.6
90	SSQV	90.		1.60	2.04	31.9
91	SUDV	0.		1.54	0.54	40.3
92	SSQV	90.		3.49	1.69	1.6.8
93	SUDV	0.		1.24	1.05	51.1
94	ssqv	90.	\	1.98	2.06	24.0

	Man.	V		Gu	st-Alle	viatio	n ,
	Max Rotor	Max Wing	Max		Fact	or	[∺] Aux Prop
Case	Thrust	Lift	Rotor	Wing	Rotor (Kg _r)	Wing (K _{g_})	
No.	(Lb)	(Lb)	(g)	(g)	6r	8	(Lb)
	25000	071.00	0 17	1 01	•		01.00
71	35800.	27400.	2.17		65	0.0	2480.
72	24400.	24700.	1.42		.65	.82	2480.
73	35900.	29800.	2.21				2970.
74	24700.	27000.	1.47		.66	.84	2970.
75	34600.	34400.	2.30	1.27			3650.
76	23400.	31300.	1.55	1.06	.68	.84	3650.
77	38200.	33200.	2.18	1.53			4950.
78	26700.	30000 -	1.41	1.31	.65	.86	4950.
79	41900.	32800.	2.09	1.79			7440.
80	29100.	29300.	1.24	1.55	.59	.87	7440.
81	35000.	29100.	2.25	1.02			2910.
82	23000.	26300.	1.44	0.83	.64	.81	2910.
83	35200.	30400.	2.24	1.13			3300.
84	23700.	27400.	1.47	0.94	.66	.83	3300.
85	35000.	34000.	2.32	1.27			3930.
86	23200.	30700.	1.54	1.05	.66	. 82	3930.
87	37000.	36900.	2.35	1.54			5290.
88	25300.	33400.	1.57	1.3	.67	.85	5290.
89	41100.	35200.	2.20	1.81			7480.
90	28200.	31500.	1.35	1.56	.61	.86	7480.
91	34500.	27600.	2.22	1.01	, , ,	•00	3330.
92	23400.	24800.	1.46	0.82	.66	.82	3330.
93	39400.	23600.		1.15	• 00	.02	3100.
94	27600.	20900.		0.96	.62	.84	3100.
	2,000	20,000	~ , ~ ./	3.70	.02	• 0 -	2100.
			_				

TABLE XXII - Continued
(COMPOUND SINGLE-ROTOR HELICOPTER, No. 1)

				Max Blade Root Osc Moment Ratio				
Case		Gust Typ Length	Max Vel		M steady	Max Flap Velocity		
No.	Shape	(Ft)	(Ft/Sec)	Beam	Chord	(Deg/Sec)		
	Semiri	gid Rotor	(Cont'd)					
95	SUDV	0.	50.	1.26	0.72	51.4		
96	ssqv	90.	1	2.11	2.03	25.9		
97	SUDV	0.		1.11	0.77	51.5		
98	ssqv	90.		1.77	1.74	27.9		
99	SUDV	0.	}	0.94	0.73	49.2		
100	ssqv	90.		1.28	1.67	29.8		
101	SUDV	0.		1.76	1.00	41.3		
102	ssqv	90.		2.44	1.35	16.7		
103	SUDV	0.		1.56	0.96	44.9		
104	ssqv	90.		2.22	1.38	20.0		
105	SUDV	0.		1.43	0.85	47.5		
106	ssqv	90.		1.99	1.34	23.3		
107	SUDV	0.		1.22	0.83	53.2		
108	SSQV	90.		1.88	1.45	29.4		
109	SUDV	0.		1.02	0.81	48.7		
110	ssqv	90.		1.33	1.55	30.2		
111	SUDV	0.		1.01	1.22	28.8		
112	SSQV	90.		1.80	2.44	12.2		
113	SUDV	0.	1	0.98	1.36	30.0		
114	SSQV	90.		1.49	2.69	12.7		
115	SUDV	0.		1.05	0.83	26.7		
116	ssqv	90.		2.07	3.53	10.28		
117	SUDV	0.		1.01	3.14	49.8		
118	ssqv	90.	1	2.50	5.74	15.2		
119	SUDV	0.	•	0.77	1.61	52.9		

				Gu	st-Alle	viati	on A	
	Max Rotor	Max Wing	Max		Faci	LOI	Dwan	
Case	Thrust	Lift	Rotor	Wing	Rotor	Wing (K)		
No.	(Lb)	(Lb)	(g)	(g)	(K _g ,	(Kgw)	(Lb)	
95	39600.	25700.	2.06	1.28			4170.	
96	28000.	22700.		1.08	.62	.84	4170.	j
97	36300.	35600.	2.22	1.55			6320.	
98	24700.	31900.	1.44	1.30	.65	.84	6320.	
99	39900.	34800.	2.11	1.82			9110.	
100	27500.	30600.	1.29	1.54	.61	.85	9110.	
101	357 0 0	27600	2.21	1.03			3800.	
102	24200.	24600.	1.44	0.82	.65	.80	3800.	
103	35800.	29400.	2.20	1.15			4500.	
104	24600.	26200.	1.45	0.94	.66	.82	4500.	
105	33800.	34200.	2.25	1.29			5620.	
106	22800.	31600.	1.52	1.12	.67	.87	5620.	
107	34500.	37500.	2.24	1.55			7230.	
108	23600.	33600.	1.52	1.29	. 67	.83	7230.	
109	37800.	35500.	2.05	1.82			10400.	1
110	26800.	31400.	1.31	1.54	.64	.85	10400.	
111	96900	16600.	5.62	0.99			2000.	
112	51300.	10300.	2.57	0.56	.46	. 57	2000.	:
113	93500.	17200.	5.33	1.11			3000.	ı
114	52300.	10100.	2.59	0.64	.48	. 58	3000.	ļ
115	97600.	15900.	5.72	0.86			1400.	
116	48900.	10300.	2.47	0.49	.43	. 57	1400.	
117	41700.	17900.	1.95	1.01			1400.	
118	27800.	15600.	1.03	0.79	.53	.78	1400.	
119	46200	17600.	2.11	1.14			1700.	

TABLE XXII - Continued
(COMPOUND SINGLE-ROTOR HELICOPTER, No. 1)

					ade Root ent Ratio	
Case		Gust Ty Length	pe Max Vel		steady	Max Flap Velocity
No.	Shape	(Ft)	(Ft/Sec)	Beam	Chord	(Deg/Sec)
	Semiri	gid Rotor	(Cont'd)			
120	SSQV	90.	50.	1.96	3.27	24.8
121	SUDV	0.		1.16	2.39	44.6
122	SSQV	90.	!	2.39	0.90	14.1
123	SUDV	0.		0.09	1.22	32.6
124	SSQV	90.		1.34	2.97	10.7
125	SUDV	0.		0.92	1.21	31.7
126	SSQV	90.		1.49	2.38	12.4
127	SUDV	0.		0.88	1.21	26.6
128	SSQV	90.		1.90	2.00	9.22
129	SUDV	0.		1.08	3.30	51.0
130	SSQV	90.		2.07	7.93	18.7
131	SUDV	0.		0.98	3.27	58.8
132	S SQV	90.		1.61	6.08	26.8
133	SUDV	0.		1.24	2.80	46.5
134	SSQV	90.	\	2.27	7.51	46.5
	Articu	lated Rote	or			
135	SUDV	0.	50.	23.5	0.84	28.2
136	SSQV	90.	1	5.76	1.63	13.9
137	SUDV	0.		30.2	1.69	50.1
138	s s q v	90.		6.87	3.14	24.4
139	SUDV	0.		10.8	1.52	32.1
140	ssqv	90.		1.86	1.84	12.5
141	SUDV	0.		32.7	1.54	56.3
142	SSQV	90.		2.55	1.07	28.4
143	SUDV	0.	į.	10.2	4.00	31.1

		Max	Max		Gu	st-Alle			
١		Rotor	Wing	Max		Fact	Wing	Aux	
	Case No.	Thrust (Lb)	Lift (Lb)	Rotor (g)	Wing (g)	(Kgr)	(K	(Lb)	
ł	110.	(LU)	(20)	10/	\6/_	<u> </u>	- OW	\207	
	120	28600.	14000.	0.93	0.9	.44	.79	1700.	
١	121	40900.	17200.	1.99	0.88			1200.	
	122	28000.	14000.	1.13	0.67	. 57	.76	1200.	
ĺ	123	93600.	18100.	5.48	0.99			1800.	
	124	44200.	13500.	2.19	0.68	.40	.69	1800.	
,	125	91500.	20400.	5.39	1.12			3000.	
	126	45400.	14900.	2.31	0.75	.43	.67	3000.	
	127	89900.	20100.	5.49	0.87			1500.	
ļ	128	36100.	15500.	1.90	0.57	.35	.65	1500.	
	129	39400.	19200.	1.89	1.01			1500.	
ĺ	130	26500.	16200.	1.03	0.81	. 54	.80	1500.	
1	131	39700.	19000.	1.77	1.15			2000.	
	132	27200.	16800.	0.90	1.00	. 53	.87	2000.	
l	133	39200.	17600.	1.90	0.88			1200.	
١	134	26400.	14900.	1.05	0.70	.55	.79	1200.	
l	135	98600.	16700.	5.63	0.98			3000.	
	136	56200.	12000.	2.81	0.67	.50	.68	3000.	
l	137	42200.	16300.	1.86	1.01			1400.	
	138	29700.	14000.	1.02	0.85	.55	.85	1400.	ŀ
l	139	102600.	17400.	5.95	0.99			3000.	
	140	52100.	12800.	2.58	0.68	.43	.69	3000.	
	141	40900.	15500.	1.70	1.01			1800.	3
	142	29800.	13400.	0.79	0.98	.48	.86	1800.	
	143	97200.	15100.	5.42	0.99			2500.	
									7.
L									

TABLE XXII - Continued)

(COMPOUND SINGLE-ROTOR HELICOPTER, No. 1)

		Gust T		Osc Mome	ade Root ent Ratio	Max Flap
Case No.	Shape	Length (Ft)	Max Vel (Ft/Sec)	Mgust/N	steady Chord	Velocity (Deg/Sec)
			tor (Cont'd		<u> </u>	(208/000/
144	ssqv	90.	50.	2.31	2.59	12.1
145	SUDV	0.	1	23.4	1.72	52.5
146	ssqv	90.		5.54	2.60	22.1
	Rigid	Rotor	•			
147	SUDV	0.	50.	11.6	2.07	28.2
148	ssqv	90.	§ .	4.06	4.35	14.2
149	SUDV	0.		1.04	3.14	49.1
150	SSQV	90.		0.97	5.40	19.9
151	SUDV	0.	ł	5.40	1.53	32.2
152	ssov	90.		2.05	2.42	12.5
153	SUDV	0.		8.51	5.58	56.3
154	ssqv	90.		4.98	5.07	25.4
155	SUDV	0.		10.8	3.53	30.8
156	SSQV	90.		2.30	2.58	12.1
157	SUDV	0.		8.34	3.02	53.3
158	SSQV	90.		2.39	4.55	22.4
	Articu	lated Ro	tor			
159	SUDV	0.	50.	8.6	2.2	35.8
160	SSQV	90.	1	1.0	3.0	16.3
161	SUDV	Э.		7.5	3.1	54.6
162	SSQV	90.		4.6	2.9	26.2
163	SUDV	0.		20.3	.8	38.9
164	SSQV	90.		7.1	1.7	15.4
165	SUDV	0.		22.7	1.1	59.0
166	SSQV	90.		1.9	2.6	24.6
169	SUDV	0.		20.8	1.3	78.2
170	SSQV	90.	· ·	5.1	2.2	28.4

	Max	Max		(Gust-Al		tion
	Rotor	Wing		Δn		ctor	Aux
Case No.	Thrust (Lb)	Lift	Rotor		Roto (Kgr) (Kg	no -
110	(LU)	(Lb)	(g)	(g)	\.\\&r	, , , , ,	(Lb)
144	50400.	11800.	2.29	0.77	.42	.78	2500.
145	39900.	17500.	1.78	1.01			1500.
146	27100.	15200.	0.93	0.86	.52	.85	1500.
147	98500.	16700.	5.63	0.99			3000.
148	57300.	12200.		0.68	.51	.69	3000.
149	41600.	18300.		1.01	•31	•03	1500.
150	27600.	15000.		0.79	. 53	.78	1500.
151	102400.	17600.		0.99	• 55	./0	
152	52600.	13100.	2.64	0.69	.44	.79	3000. 3000.
153	40900.	15600.	1.7	1.01	•	•/ >	1800.
154	28800.	13600.	0.9	0.88	.53	.87	1800.
155	96600.	15700.		0.99	• 33	.0/	2500.
156	50400.	12000.		0.74	.43	.75	
157	39900.	17500.	1.78	1.01	• 10	• / 3	2500.
158	27500.	15200.	0.95	0.86	•53	.85	1500. 1500.
159	99900.	19400.	5.71	1.23			5500
160	53400.	13100.	2.60	0.82	1,6		5500.
161	40900.	21700.	1.85	1.28	.46	.66	5500.
162	27700.	19300.	0.97	1.12	FO	0.7	4000.
163	95200.	26100.	5.85	1.12	. 52	.87	4000.
164	51400.	20100.	2.92	0.79	. 50	6.6	5500.
165	41900.	24800.	2.14	1.28	• 30	.66	5500.
166	28800.	21400.	1.27	1.05	50	0.0	3500.
169	39900.	22700.	1.87	1.03	. 59	.82	3500.
170	27000.	19800.	1.01	1.02	Ę.).	9.0	3000.
				00	. 54	.80	3000.

TABLE XXII - Continued

(COMPOUND SINGLE-ROTOR HELICOPTER, No. 1)

					ade Root ent Ratio	
		Gust T	ype		steady	Max Flap
Case No.	Shape	Length (Ft)	Max Vel (Ft/Sec)	Beam	Chord	Velocity (Deg/Sec)
	Rigid	Rotor				
171	SUDV	0.	50.	3.9	1.8	35.9
172	SSQV	90.	1	1.7	2.6	15.4
173	SUDV	0.	ĺ	7.8	3.1	54.6
174	ssqv	90.		4.6	3.5	26.3
175	SUDV	0.		10.4	1.3	38.9
176	SSQV	90.		4.7	5.7	15.8
177	SUDV	0.		6.1	2.7	59.0
178	ssqv	90.		4.2	6.3	19.6
181	SUDV	0.	1	6.9	4.2	78.1
182	SSQV	90.	+	2.8	3.5	28.5
	Semiri	gid Roto	r			
223	SUDV	0.	50.	1.1	2.0	58.5
224	ssqv	90.	1	1.6	2.8	24.1
225	SUDV	0.	1	. 3	2.0	60.5
226	SSQV	90.	į.	.89	2.0	26.6
	Rigid	Rotor				:
227	SUDV	0.	50.	7.6	16.8	46.4
228	SSQV	90.	1	7.1	18.8	18.7
229	SUDV	0.	İ	2.8	1.5	57.5
230	ssqv	90.	*	3.0	4.3	26.3
	Articu	lated Ro	tor			
231	SUDV	0.	50.	22.2	2.2	55.8
232	ssqv	90.		9.6	2.5	28.0
233	SUDV	0.		11.6	1.4	69.3
234	ssqv	90.	+	5.6	1.8	28.8

	Max	Max		Gu	st-All		on
	Rotor	Wing	Max		Fact Rotor	Wing	Aux
Case	Thrust	Lift (Lb)	Rotor (g)	Wing (g)	(Kgr)	(K,)	
No.	(Lb)	(LU).	(8)	(8)	or_	OW.	(Lb)
171	99400.	19400.	5.68	1.23			5500.
172	53700.	13500.	2.64	0.84	.46	.68	5500.
173	40900.	21800.	1.85	1.28	• 40	•00	4000.
174	27700.	19400.	0.98	1.12	. 53	.87	4000.
175	95200.	26100.	4.85	1.28	,	••,	5500
176	53000.	20400.	3.03	0.81	. 52	.68	5500.
177	41900.	24800.	2.15	1.28	•	• • • •	3500.
178	28200.	11200.	1.24	1.03	. 58	.81	3500.
181	39900.	22800.	1.87	1.28			3000.
182	27400.	19800.	1.0	1.02	.56	.79	3000.
223	25400.	20700.	1.03	1.03			1400.
224	20100.	18400.	0.67	0.88	.66	.85	1400.
225	26700.	21000.	0.88	1.30			3500.
226	23200.	18600.	0.65	1.14	.73	.88	3500.
İ							
227	26400.	17500.	0.86	1.10			1400.
228	19800.	16600.	0.41	0.97	.49	.94	1400.
229	26200.	21900.	0.93	1.30			3200.
230	22500.	22100.	0.68	1.31	.73	1.01	3200.
231	25800.	17500.	0.82	1.03			1400.
232	20600.	17200.	0.47	1.02	. 57	.98	1400.
233	25600.	22000.	0.89	1.30			3200.
234	22100.	22400.	0.65	1.33	.74	1.02	3200.
L							

TABLE XXIII. GUST-RESPONSE CASE RESULTS, COMPOUND SINGLE-ROTOR HELICOPTER, NO. 2

Case		ust Type Length	Max Vel	Osc Mom	ade Root ent Ratio	Max Flap Velocity
No.	Shape	(Ft)	(Ft/Sec)	Beam	Chord	(Deg/Sec)
0.00		id Rotor	1.0	1 07	0.10	125
238	ssqv	60.	40.	1.87	9.10	13.5 8.8
239		40.	30.	1.31	5.54	
240	CHDY	27.	20.	.97	2.43	6.8
250	SUDV	0.	50.	1.21	3.00	54.7
251	SEDV	0.		.98	1.02	21.5
252	SUDV	0.		2.71	1.78	55.6
253	SEDV	0.		2.42	1.53	21.7
254	ssqv	90.	1	2.50	59.0	17.1
255	RMPV	27.	20.	1.29	2.56	6.2
256	RMPV	90.	50.	2.34	21.0	12.9
257	ssqv	120.		1.71	64.0	13.2
258	RFTP	90.		.92	114.	12.8
259	ssqv	90.		2.14	11.7	1.3.7
260		90.		1.92	10.5	16.5
261		90.		1.92	8.72	16.5
262	SUDV	0.		1.22	2.78	55.5
269	SEDV	0.		2.25	7.75	23.7
275	ssqv	90.		2.33	7.42	17.6
276				2.00	7.50	17.9
277	+	\rightarrow	\rightarrow	2.29	8.75	20.9

Case No.	Max Rotor Thrust	Max Wing Lift	Max An	Gust-Ali Factor (Kg)	r
NO.	(Lb)	(Ľb)	(g)	, g	Comments
238	13700.	1800.	0.84		
239	12700.	1600.	0.69		
240	11000.	1400.	0.44		
250	18500.	2400.	1.54		Steady, no aero- elastic feedback
251	15000.	2300.	1.02		250 with penetration
252	15900.	2400.	1.24		Nonsteady, aero- elastic feedback
253	14400.	2200.	1.02		252 with penetration
254	13800.	1900.	0.88	.57	
255	11700.	1300.	0.54		
256	13300.	1800.	0.80		
257	13500.	1800.	0.81	.65	
258	13300.	1800.	0.80		Ramp up and down
259	13400.	1800.	0.83	.64	$\delta_3 = -300$
260	14000.	1900.	0.89	.72	No aeroelastic feedback
261	14000.	1900.	0.89	.58	Steady, no aero- elastic feedback
262	15900.	2400.	1.24		
269	12950.	2291.	.8 6		
275	14000.	2100.	0.88		Pitch-link softness 0. deg/(106 inlb)
276	14000.	2100.	0.89		Pitch-link softness 10. deg/(106 inlb)
277	14200.	2100.	0.91		Pitch-link softness 100. deg/(10 ⁶ inlb)

TABLE XXIV. GUST-RESPONSE CASE RESULTS, TANDEM-ROTOR HELICOPTER

				Fwd Rote	Fwd Rotor		Aft Rotor	
					Max		Max	
0		Gust T		Max Flap	Rotor	Max Flap	Rotor	
Case No.	Shape	(Ft)	Max Vel (Ft/Sec)		Thrust (Lb)	Velocity (Deg/Sec)	Thrust (Lb/Sec)	
	Aft C		W					
183	SUDV	0.	50.	57.	39900.	42.	40600.	
184	SSQV	90.	1	105.	51800.	122.	57600.	
185	SUDV	0.		105.	17600.	96.	17400.	
186	ssqv	90.		56.	16800.	60.	19100.	
187	SUDV	0.		61.	37700.	45.	38700.	
188	SSQV	90.		127.	51600.	138.	60500.	
189	SUDV	0.		108.	16600.	94.	16500.	
190	SSQV	90.	t	48.	15700.	57.	18000.	
	Neutra	al CG			•			
272	ssqv	90.	50.	36.3	16894.	54.	17400.	
	Forwar	rd CG		5				
274	ssqv	90.	50.	37.0	14700.	42.6	14300.	

Case No.	Max Δ n (g)	Gust-Alleviation Factor (Kg)	Comments
183	4.37		
184	4.97	1.14	Adverse fuselage pitching
185	1.35		Active reactage precining
186	1.04	•77	
187	4.09		
188	4.56	1.12	Adverse fuselage pitching
189	1.22		noverse inserage pitching
190	0.91	•74	
272	0.96	-	
274	0.89	-	

TABLE XXV. GUST-RESPONSE CASE RESULTS, SIDE-BY-SIDE HELICOPTER

		Gust	Туре	- AND STREET	
Case No.	Shape	Length (Ft)	Max Vel (Ft/Sec)	Mast Tilt At Gust (Deg)	Max Flap Velocity (Deg/Sec)
	Helicopt	er Mode			
199	SSQV	90.	50.	o.	11.8
200	SSQV	į.	•	•	19.2
	Transiti	on Mode			
201	SSQV	90.	50.	30.	- 13.7
202	SSQV			60.	- 31.3
203	ssqv			30.	- 27.6
204	SSQV	ŧ	•	60.	- 36.2
	Airplane	Mode			
205	SUDV	0.	50.	90.	41.1
206	SSQV	90.		ľ	15.8
207	SUDV	0.			40.9
208	ssqv	90.			18.1
209	SUDV	0.			61.6
210	SSQV	90.			- 28.4
211	SUDV	0.			109.0
212	SSQV	90.			- 125.1
213	SUDV	0.			142.0
214	ssqv	90.		<u> </u>	1741.0

Case No.	Max Thrus Per Rotor (Lb)	t Max r Wing Lift (lb)	Max t Δn (g)	Gust-Alle Factor (Kg)	comments
					- Onabeli Co
199	16300.	15100.	1.16		
200	16500.	16900.	1.24		
201	9700.	23200.	0.90		
202	6102.	26200.	0.54		
03	10800.	31600.	1.37		
04	5000.	37300.	1.02		
05	4000.	32500.	0.79		
06	3400.	30300.	0.64	.81	
07	1900.	35000.	0.90	•01	
08	1600.	37200.	0.80	0.0	
09	1500.	52800.	1.69	.89	
LO	1400.	51400.		04.	
11	2100.	75000.	1.42	.04	
.2	2000.	74100.	2.60	0.0	
.3	2800.	10100.	2.14	.82	
4	44.1		3.55 16.44	2 62	1.5
		-33700.	10,44	3.83	Flapping instability at high speed

APPENDIX IV. ROTOR DESCRIPTIVE INFORMATION

TABI	LE XXVI. ROTOR	STIFFNESS AND WE	EIGHT PARAMETERS
Pu	re and Compound	Single-Rotor He	licopter
1	Number 6017 Loading 7.0	Number Radius Chord	of Blades 4 26.1 Ft 35.6 In.
Blade Segment (% R)	Beamwise EI/10 ⁶ (Lb-In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight/Inch (Lb/In.)
0-5	77.	1022.	4.890
5-10	3065.	1022.	8.290
10-15	4645.	15138.	8.080
15-20	1460.	16306.	3.570
20-25	470.	11107.	1.560
25-30	329.	9346.	1.280
30-35	252.	8067.	1.110
35-40	231.	7334.	1.050
40-45	208.	6550.	0.990
45-50	181.	6058.	4.134
50-55	159.	5553.	0.870
55-60	154.	5304.	0.850
60-65	154.	5042.	0.850
65-70	154.	5042.	0.850
70-75	154.	5042.	0.850
75-80	154.	5042.	0.850
80-85	154.	5042.	0.850
85-90	154.	5042.	0.850
90-95	154.	5042.	0.850
95-100	154.	5042.	0.850

	TABLE XXV	I - Continued	
	Pure and Compound	Single-Rotor	Helicopter
	r Number 6057 Loading 7.0	Number Radius Chord	of Blades 4 26.1 Ft 89.0 In
Blade Segment (% R)	Beamwise EI/106 (Lb-In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight/Inch (Lb/In.)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 4Q-45 45-50 50-55 55-60 60-65 65-70 70-75	1453. 5402. 8285. 3784. 2376. 2174. 2064. 1628. 1603. 1572. 1931. 1922. 1922.	27248 . 27248 . 27248 . 29834 . 17392 . 27804 . 40335 . 39554 . 39050 . 38318 . 37845 . 75226 . 74767 . 74314 . 74314 .	8.417 12.857 12.587 6.697 4.011 3.705 3.484 3.405 3.328 3.264 3.172 3.145 3.145 3.145
75-80 80-85 85-90 90-95 95-100	1922. 1922. 1922. 1922. 1922.	74314. 74314. 74314. 74314. 74314.	3.145 3.145 3.145 3.145 3.145

	TA	BLE XXVI	- Continued		
	Pure and	Compound	Single-Rotor	Helicopter	-
	Rotor Number Disc Loading C_{T}/σ		Number Radius Chord	of Blades	4 34.5 Ft 26.9 In
Blade Segment (% R)	EI	mwise (/106 (In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight (Lb/	t/Inch In.)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 40-45 45-50 50-55 55-60 60-65 65-70 70-75 75-80	10° 16° 5. 1°	27. 93. 48. 18. 57. 17. 39. 82. 74. 55. 55.	4096. 4096. 6156. 6633. 4501. 3585. 3281. 2967. 2661. 2449. 2255. 2142. 2040. 2040. 2040.	5. 2. 1. 0. 0. 0. 0. 0.	290 570 430 400 050 861 747 707 666 632 586 504 572 572
80-85 85-90 90-95 95-100		55. 55. 55.	2040. 2040. 2040. 2040.	0.	572 572 572 572

· · · · · · · · · · · · · · · · · · ·						
	TABLE XXV	I - Continued				
	Pure and Compound	Single-Rotor Hel	icopter			
	r Number 6042 Loading 4.0	Number of Redius Chord	Blades 4 34.5 Ft 67.1 In			
Blade Segment (% R)	Beamwise EI/10 ⁶ (Lb-In. ²)	Chordwise EI/106 (Lb-In. ²)	We ight/Inch (Lb/In.)			
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 40-45 45-50 50-55	436. 17420. 26130. 8272. 2668. 1863. 1428. 1306. 1177. 1030. 900.	57900. 57900. 87090. 94380. 63950. 53690. 46470. 42090. 37720. 34840. 31930.	12.240 20.750 20.220 8.933 3.903 3.203 2.778 2.627 2.477 2.352 2.177			
55-60 60-65 65-70 70-75 75-80 80-85 85-90 90-95 95-100	874. 874. 874. 874. 874. 874. 874.	30480. 29030. 29030. 29030. 29030. 29030. 29030.	2.127 2.127 2.127 2.127 2.127 2.127 2.127 2.127			
Tip Weight			32.200 Lb			

TABLE XXVI - Continued Pure and Compound Single-Rotor Helicopter Rotor Number 6022 Number of Blades Disc Loading 10.0 Radius 21.8 Ft C_T/σ .05 Chord 42.5 In. Blade Beamwise Chordwise EI/10 Segment EI/106 Weight/Inch $(Lb-In.^2)$ (% R) $(Lb-In.^2)$ (Lb/In.) 0-5 11560. 88. 6.380 5-10 4016. 11560. 10.820 10-15 5248. 17460. 10.550 15-20 1658. 19010. 4.660 20-25 535. 12960. 2.034 25-30 374. 10700. 1.670 30-35 288. 9400. 1.450 35-40 262. 8470. 1.370 40-45 237. 7638. 1.290 45-50 206. 6955. 1.230 50-55 181. 1.140 6384. 55-60 175. 6110. 1.110 60-65 175. 5780. 1.110 65-70 1.110 175. 5780. 70-75 175. 5780. 1.110 75-80 175. 5780. 1.110 80-85 175. 5780. 1.110 85-90 175. 5780. 1.110 90-95 175. 5780. 1.110 95-100 175. 5780. 1.110

TABLE XXVI - Continued

Pure and Compound Single-Rotor Helicopter

Rotor Number 6069 Number of Blades 4 Disc Loading 10.0 Radius 21.8 Ft $C_{\rm T}/\sigma$.02 Chord 106.2 In

Blade Segment (% R)	Beamwise EI/106 (Lb-In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight/Inch (Lb/In.)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 40-45 45-50 50-55 55-60 60-65 65-70 70-75	369. 570. 1944. 2097. 1541. 1455. 1405. 1123. 1114. 1098. 909. 904. 777. 777.	36090. 36090. 26400. 28510. 41130. 35940. 32400. 30120. 28050. 26570. 12540. 12220. 11820. 11820. 11820.	9.382 13.822 13.552 7.662 5.036 4.690 4.449 4.370 4.293 4.229 4.137 4.110 4.110
75-80 80-85 85-90 90-95 95-100	777 • 777 • 777 • 777 • 777 •	11820. 11820. 11820. 11820.	4.110 4.110 4.110 4.110 4.110

	TABLE XXV	/I - Continued		
	Pure Single	-Rotor Helicopt	er	
	Number 8065 loading 4.69	Number o Radius Chord	f Blades	4 24.0 Ft 21.0 In.
Blade Segment (% R)	Beamwise EI/106 (Lb-In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight/ (Lb/In	Inch .)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 40-45 45-50 50-55 55-60 60-65 65-70 70-75 75-80 80-85 85-90 90-95	24. 399. 480. 823. 332. 75. 32. 30. 28. 28. 28. 28. 28. 28. 28. 28	6663. 3260. 1203. 1103. 2498. 3049. 2523. 2259. 2001. 1751. 1522. 1289. 1099. 950. 940. 1020. 1000. 950.	2.700 3.500 4.350 4.800 3.120 0.980 0.725 0.630 0.617 0.591 0.570 0.562 0.557 0.557 0.557 0.557	
95-100 Sip Weight	9.	910.	0.463 2.750	Lb

TABLE XXVI - Continued Compound Single-Rotor Helicopter Rotor Number 0166 Number of Blades 22.0 Ft Disc Loading 5.6 Radius 27.0 In. .064 C_T/σ Chord Blade Beamwise Chordwise EI/106 EI/106 (Lb-In.²) Weight/Inch Segment $(Lb-In.^2)$ (% R)(Lb/In.) 0-5 4287. 14. 3.326 5-10 507. 6.900 5804. 10-15 694. 6088. 6.875 15-20 6144. 2.432 261. 95. 20-25 4117. 0.941 25-30 0.759 66. 3695. 30-35 3270. 0.661 50. 35-40 46. 0.624 2922. 2638. 40-45 42. 0.593 45-50 37. 2380. 0.557 50-55 33. 2172. 0.516 55-60 33. 2026. 0.617 60-65 36. 2028. 1.116 65-70 36. 2028. 1.116 70-75 33. 2010. 0.649 75-80 32. 2005. 0.505 80-85 32. 2005. 0.505 85-90 32. 2005. 0.505

2005.

2005.

1.659

2.240

32.

32.

90-95

95-100

	TABLE XX	IVI - Continued	
	Tandem	Helicopter	
	Rotor Number 6081 Disc Loading 7.0 C_T/σ .05	Number of Radius Chord	Blades 4 18.35 Ft 23.0 In.
Blade Segment (% R)	Beamwise EI/10 ⁶ (Lb-In. ²)	Chordwise EI/10 ⁶ (Lb-In. ²)	Weight/Inch (Lb/In.)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40	31. 4849. 6448. 1894. 483. 282. 172.	8303. 8303. 15950. 17320. 9776. 7215. 5364. 4268.	5.683 10.150 9.883 3.993 1.366 1.021 0.780 0.701
40-45 45-50 50-55 55-60 60-65 65-70	109. 71. 39. 31. 31.	3173. 2434. 1712. 1350. 973.	0.624 0.560 0.468 0.441 0.441
70-75 75-80 80-85 85-90 90-95 95-100	31. 31. 31. 31. 31.	973. 973. 973. 973. 973.	0.441 0.441 0.441 0.441 0.441

	TABLE XXV	I - Continued	
	Tander	n Helicopter	
	r Number 6071 Loading 7.0	Number of Radius Chord	Blades 4 18.35 Ft 57.6 In
Blade Segment (% R)	Beamwise EI/106 (Lb-In. ²)	Chordwise EI/106 (Lb-In. ²)	Weight/Inch (Lb/In.)
0-5 5-10 10-15 15-20 20-25 25-30 30-35 35-40 40-45 45-50 50-55	374. 5317. 6888. 2349. 935. 734. 624. 594. 561. 523. 491.	24240. 24240. 31900. 33670. 25250. 22450. 20900. 19550. 18370. 17830. 16840. 16840.	6.902 11.340 7.812 5.142 2.556 2.210 1.969 1.890 1.813 1.749 1.657
55-60 60-65 65-70 70-75 75-80 80-85 85-90 90-95 95-100	483. 483. 483. 483. 483. 483. 483. 483.	16380. 16380. 16380. 16380. 16380. 16380. 16380.	1.630 1.630 1.630 1.630 1.630 1.630 1.630

TABLE XXVI - Continued Side-By-Side Helicopter Rotor Number D215 Number of Blades Disc Loading Radius 19.25 Ft 9.87 .105 20.0 In. Chord C_T/σ Beanwise EI/106 (Lb-In.²) Chordwise EI/10⁶ (Lb-In.²) Blade Weight/Inch (Lb/In.) Segment (% R) 0 - 54222. 3510. 5.800 5-10 690. 690. 3.400 10-15 1321. 1741. 2.500 2068. 15-20 999. 1.850 20-25 439. 2616. 0.800 245. 25-30 2107. 0.760 30-35 158. 1887. 0.610 35-40 1798. 0.600 138. 40-45 0,600 127. 1708. 45-50 0.600 116. 1310. 50-55 104. 1588. 0.810 55-60 92. 1519. 0.780 60-65 81. 1467. 0.750 65-70 70-75 71. 1390. 0.720 60. 1339. 0.690 75-80 52. 1290. 0.660 1249. 1278. 44. 80-85 0.630 85-90 0.600 36. 90-95 29. 1178. 0.570 95-100 24. 1148. 1.405

APPENDIX V. SELECTED STABILITY-DERIVATIVE RESULTS

TR WINGLAS TO WOM.F/A TH MOW.LAT WA MUNIEZA WA MOMILAT TR MOMIEZA TA WUMILAT -1.97 -555.41 -3.67 12.52 13.04 141.47 11.73 4.14 MR MAMALAT TR MON.F/A 75.21 -70.95 -214.05 1.17 3.65 124.63 1.52 -151.37 1.92 10.27 200 CAUTS 200 # \$ 3TS 15.54 -77.59 -277.41 0.39 3.69 200 KILLS ANALYTICAL STUDY JE HELICUPTER GUST RESPONSE SUUDEN VERTICAL GLST - 2 BLADFJ # .lo 4 # .9 HIGID RITHR 2003 ANALYTICAL STUDY OF MELICOPTER GUST RESPONSE
SUDDEN VERTICAL GUST 2 MLADED
7 TC = 0.16 M = .9 SEMMRIGIO ROTOR 200 ANALYTICAL STUDY OF MELICUPTE - GUST MESPUNSF SUPDEM VEHTICAL GLST - 1 MLADED - 15 - 4 - 9 ARTICULATE) OCTOP - 200 MR 40%-LAT -1165.00 -769.30 937.42 276.55 197.37 \$\$\$\$.05 \$\$\$\$.05 \$\$\$\$.05 \$\$\$.25 \$\$\$.75 \$\$\$.75 54631.46 17999.47 1443.62 279.54 541.78 541.78 ROLL WON. 42 404.F/A אוון אוא. אי אוא דיים 6254.96 25826.54 -12.75 72.30 70.13 29140.63 45293.71 544.31 254.20 1311.92 15914.64 73276.04 193.43 36.63 1395.63 STASILITY PARTIAL DERIVATIVE MATRIA STABILITY PARTIAL DERIVATIVE MATRIX STABILITY PARTIAL DEPIVATIVE MATRIX ROLL 404. 1112.99 7132.95 33.29 -259.70 -2013.43 -717.97 -7155.52 3C.70 -264.54 -6AC. 37 -162C.90 19C7.20 7646.56 21.23 -253.61 -124.09 TC = .10 4 = .9 YAH MUN. PITCH WUY. -1160.83 -16457.8C 1765.67 61.69 -31.39 -554.53 Z-FIJRCE YAN MGN. PITCH 434. PITCH 434. 752.67 -14795.90 1072.15 99.44 -10.75 -22.66 7 -15287.22 144.04 53.86 -2.43 TC * .15 1 = 10 A SPH 7 -4994.37 -4553.75 -97967.55 -434.93 1990.21 PSKH YAM MUM. 10587.11 7876.17 -83643.94 -386.26 2161.91 -2121.45 -5282.42 -94000.37 -393.05 1757.08 1 = 10 7 = 70 4150219 4150217 Z-FURCE 4150221 Z-FUACE -3916.67 -770.31 -229.63 12.37 -6#5.15 -75.03 -4.65 -24.01 -343.14 14.00547 477.34 -4.57 -4410.04 -343.27 147.02 11.41 -70.01 -14.51 2225.37 10.31 -72.18 7499.15 16.56 -54.46 -13.65 -130.44 Y-FURCE -429.93 Y-FURCE -246.43 210.59 Y-FURCE 26.29 -19.57 -0.30 21.98 -5.42 -20.01 1.64 5.95 139.21 -1.23 172.93 145.11 -24.91 K-FUACE X-FURCE

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4643>3

BELL HELICOPTER 15M 360/ PROGRAM C91-11 HELICOPTER RIGID BJOY DYNAMICS ANALYSIS COMPILE? 4-19-67

ECCDDA

0 (7 (C)> 3

	KNOTS
STICAL GUST 4 BLADED	SEMIRIGIO ROTOR 200
SUDDEN VE	TC = 0.2 M = .9
CSRH	0 = 10
	CSRH SUDDEN VERTICAL GUST 4 BLADED

STABILITY PARTIAL DERIVATIVE MATRIX

							1	1	*	•			
ļ	X-FORCE	Y-FUACE	Z-FiJRCE	YAN MOM.		PITCH NOM.	ROLL MOM.		MR MOM.F/A MR	MOM.LAT TR	MOM .F/A	Œ	MO4.LAT
a 0	184.30	-282.81	-2548.83	8709.14	7	-261.76	-1035.06	214		34336.21	24.79	9 '	164.26
, ~	50.95	2193.68	-47.63	-82198-00		-814.20	67.00	2616	PC-05-	1388.76	-300-67	145	97-17
: >	-18.23	9.74	-19.99	-311-07		40-46	29.84	, 1		145.30	0.39	•	0.65
>	-1.08	-64.16	-6.72	2056.39		37.14	-215.48	14	410.74	88.50	9.82	1	13.44
3	24.28	-10.03	-694.13	102.35		-570.81	-53.67	41 -	98.641-	1 394.64	-0-11		3.51
		•	. 16.31		•								
		-	77961.		CSKH UL = 7	AMALTICAL S 7 TC = 0.2	ŝ	SUDDEN VERTICAL	ICAL GUST REGID KOTOR	I KESPUASE I 4 BLADED DIGA	c		
				ST	STABILITY	PARTIAL	DERIVATIVE MATHIX	F YATE	X I X				
_	X-FORCE	E Y-FU3CE		Z-FJRCE Y	YAM MON.	. PITCH 4014.	401	M.J.4.	MR MOM.F/A	A MK MON-LAT	T TR 40M.F/A TR	F/4 T	R MOM.LAT
	6.0°	•			-2299.11	437.12	1	-522.00	553,25	28309.83	19101		39.35
	-		-10		1909.17	-16474.64		954.10	29872.86	-4039.34	119.50		-126.21
		2		ı	92173.50	-650.61	2	7663.32	28.37	•	-195.36		-620.39
	•				-422.53	71.80		33.75	-47.19		1.51	_	-1.70
					1976.40	÷6.07		-213.59	544.79		•	ic	11.67
-		'	-045.44	†	20.65	00.816-		-36.35	-301.76	16.7661	10.0	_	06.1
		_	4150231		NA HOND	ALYTICAL	ANALYTICAL STUDY OF HELICOPTER	HELICO	PTER GUST	RESPONSE			
				_	7 = 10	TC = 0.2		# = .9		4	TED ROTOR		
				ST	ABILITY	PARTIAL	STABILITY PARTIAL DERIVATIVE MATRIX	E MATR	XIX				
	X-FURCE	E Y-FORCE		2-FURCE Y	YAW MOM.	PITCH MON.	ROLL	MOM. M	MR MOM.F/A	X.	MOM.LAT TR MOM.F/A		TR MOM.LAT
٩	-91.46	07.496- 94	70 -3538.28		-212.50	1607.69	9 -1603.30	30	. 50 3R . 34	41407-06	26. 95		150-28
0					3334.38	-17996-66		505	22117.79	-1266.09	-41-20		23.31
~		~		7	04257.00	358.77		. 88	-166.08	-2995.39	-170.27	ı	685.84
D	-27.41				-389.66	64.03		30.78	0.64	269.98	14.0		22.20
> :		57 -83.72			2547.86	2.96	•	6.5	698.97	52.65	7.05		18.09
¥	-11.84		05 -634.90		19.67-	-696.31	87.8/-	87.	-543.64	12.6262	24-2-		3.47

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			STABILITY PARTIAL	PARTIAL DES	DERIVATIVE WAI	MATRIX			
X-FORCE	Y-FORCE	Z-FURCE	YAH HOM.	PITCH HOM.	401 HON.	MR MOM.F/1	MR WOW-LAT	TR HOM.F/A	TR HOM.LAT
-185.18	10.702-	-3760.00	1	2211.49	-2203.13	5778.80	32999.25	69-01	87.65
50.20	-145.63	-897.27		-19735.44	-1105.08	20339.89	-894.37	-51.88	-26.82
4.52	2980.96	350.74-	=	1056-94	9155.86	-549.33	-2861.47	-154.32	-761.40
-34.31	13.85		-523.44	41.25	41.04	9.72	194.03	0.56	-3.96
-1.21	01-16-		2564.75	-16.51	-345.97	727.29	144.32	7.85	17.22
-26.45	-10.07	-763.57	113.87	-614.76	-123.89	-195.59	1344.92	-3.51	3.39
	7	\$050259		ANAL YT FCAL		OF HELICOPT	STUDY OF HELICOPTER GUST BE ROOMS	SONCE	
			C = 10) 1		SUDDEN VERTICAL GUST	CUST 4 BL	BLADED 259 KNOTS	
			STABIL ITY	STABILITY PARTIAL DERIVATIVE MATRIX	IVATIVE WAT	*			
T-FCRCE	V-FORCE	Z-F JRCE	YAU MOM.	PITCH MOM.	ROLL MOM.	WR 4CH.F/A	HR MOM.LAT	HR HOW.LAT TR MOM.F/A TR HOM.LAT	TR HOM-LAT
-43.94	-394.81	-3502-14	512.50	1518.95	-1730.27	77 (137	23.28.7 80	24.50	140 24
74.66	-92.76	-668.36		-19434. 62	-411.70	12415.00	-94.71	-30.54	13.77
14.87	2937.33	195.31-1	C	343.56	9001.90	-149.73	-1644-79		741.42
- 1	86.71	66.64	76.11.37	11.13	39.13	25.95	156.21		-2.12
71.0		65.00	16.856.7	-10.28	-315-46	487.07	64.86	*	18.95
•				-569.63	-47.73	96.671-	1945.76	-2.09	3.31
	1	5050233	.33	AMAINTICAL		ested to so yours	,		
			C SR H	=	9	SUDDEN VERTICAL GUST	T T	3 8LA0ED R 250 KNOTS	
			STABILITY	STABILITY PARTIAL DERIVATIVE MATRIX	RIVATIVE MA	TRIX			
X-FORCE	Y-FORCE	Z-FORCE	YAN HOM.	PITCH MOM.	ROLL MOM.	*	HOM.F/A HR HOM.LAT	TR MOM.F/A	I TR MCM.LAT
-61.08	-330.47	-3600.78	-718.75	1439.66	-1438.06	4703-31	45	46.29	128.35
10 01	2000	45 - 1 B Z -		-20084. 70	576.68	1818.35		2.42	-17.64
-30.05	17.05	187-45-	=	139.47	9000 54	-117.13	~	-162.69	-745.89
0.71	-83.67	3.73	2527.17	16.18	39.35	105.47		22.0	-2.00
-9.79	-18.19	-696.56	26.42	-711.19	-119.33	-901-30	140-13	7.42	18.36
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13. ABSTRACT			
An analytical study of helicopte speeds is presented. A digital-includes rigid-body aircraft mot representation of two rotors. T describe all general configurati sidered, as well as compounding propulsion. Various maneuvers m jecting the aircraft to gust dis	computer propions in space he rotors can ons. Various by the use of ay be simulated	gram is and is an and is an and is an and is an analysis and an analysis and is an analysis and is an analysis and is an analysis and is an analysis and is an analysis and is an analysis and an analysis and an analysis and an analysis and an analysis and an analysis and an analysis and an analysis analysis and an analysis and an analysis analysis and an analysis and an analysis analysis and an analysis analysis and an analysis and an analysis analysis and an analysis analysis and an analysis analys	s described that the aeroelastic ositioned to r types are con- s and auxiliary
Results cover a wide range of fo loadings, and advancing blade-ti number on gust response is inclugust shape, gradual penetration, alleviation devices are discusse	p Mach number ded. The re- nonsteady as	rs. T Lative	he effect of Lock importance of

A simple empirical expression is given that will adequately predict the rotor gust-load increase for a wide range of helicopter and compound designs.

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